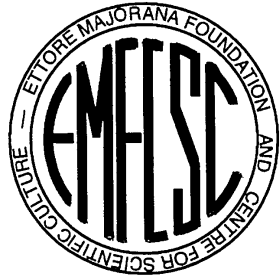


Cosmic rays at the knee

Results and implications



«ETTORE MAJORANA» FOUNDATION AND CENTRE FOR SCIENTIFIC CULTURE

INTERNATIONAL SCHOOL OF COSMIC-RAY ASTROPHYSICS
«MAURICE M. SHAPIRO»

22nd Course: “From cosmic particles to gravitational waves: now and to come”
30 July – 7 August 2022

PRESIDENT AND DIRECTOR OF THE CENTRE: PROFESSOR A. ZICHICHI

DIRECTORS OF THE COURSE: PROFESSORS J.P. WEFEL, T. STANEV, J.R. HÖRANDEL



Nikhef



Cosmic rays at the knee

Results and implications

energy density

$$\rho_E = \frac{4\pi}{c} \int \frac{E}{\beta} \frac{dN}{dE} dE \approx 1 \frac{\text{eV}}{\text{cm}^3}$$

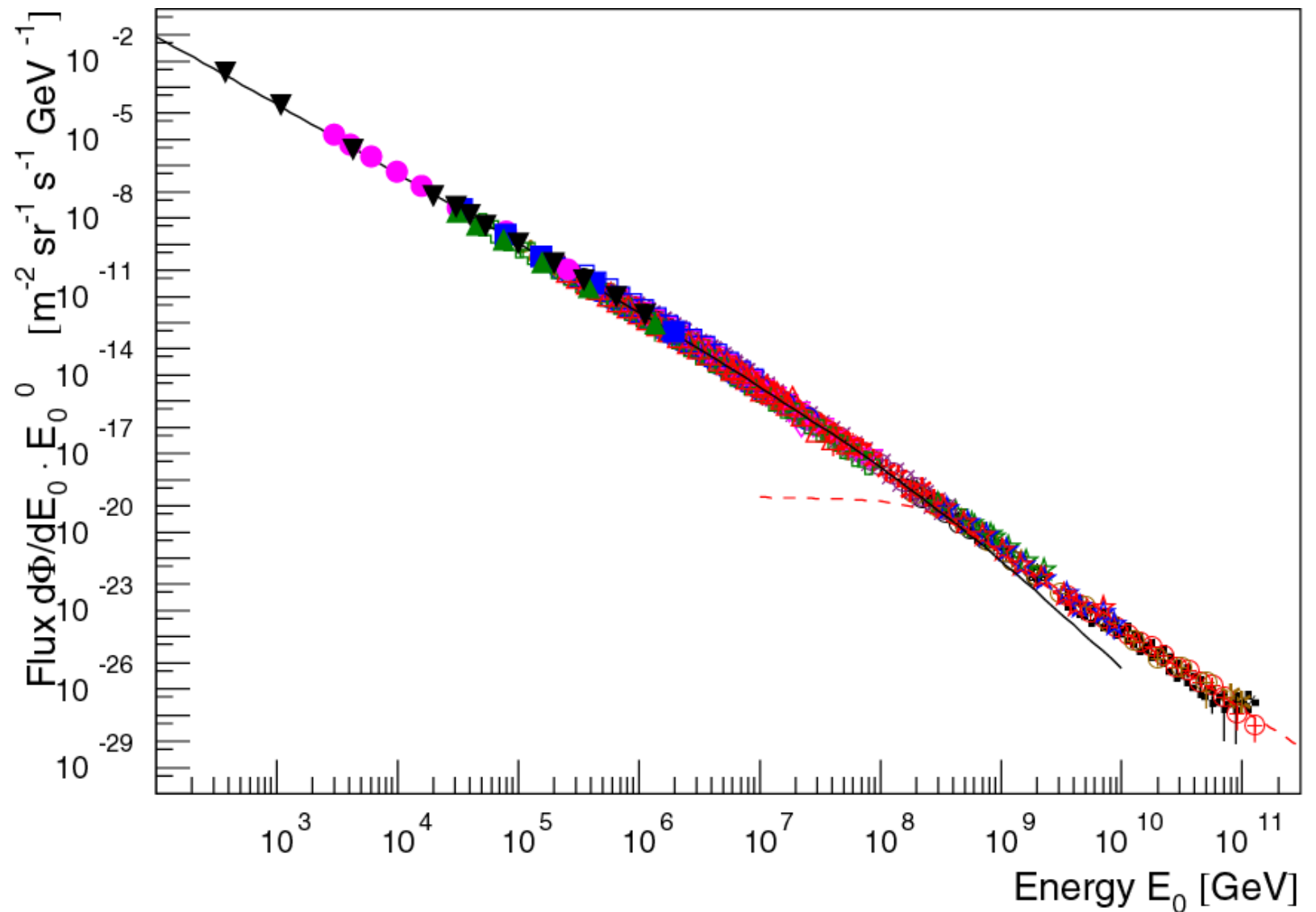
for comparison:

$$\rho_B = \frac{B^2}{2\mu_0} \approx 0.25 \text{ eV/cm}^3$$

$$\rho_{SL} \approx 0.3 \text{ eV/cm}^3$$

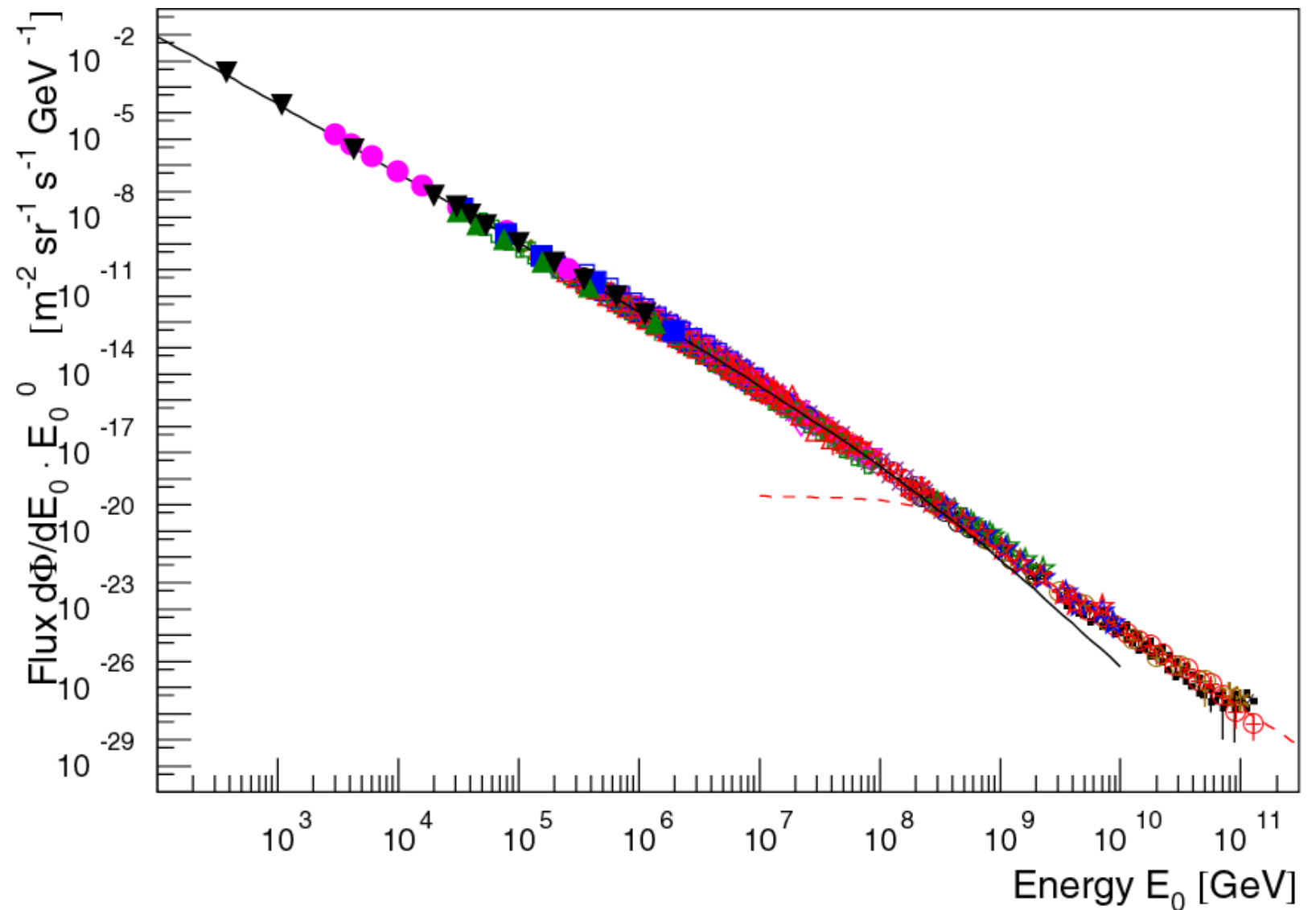
$$\rho_{IR} \approx 0.4 \text{ eV/cm}^3$$

$$\rho_{3K} \approx 0.25 \text{ eV/cm}^3$$



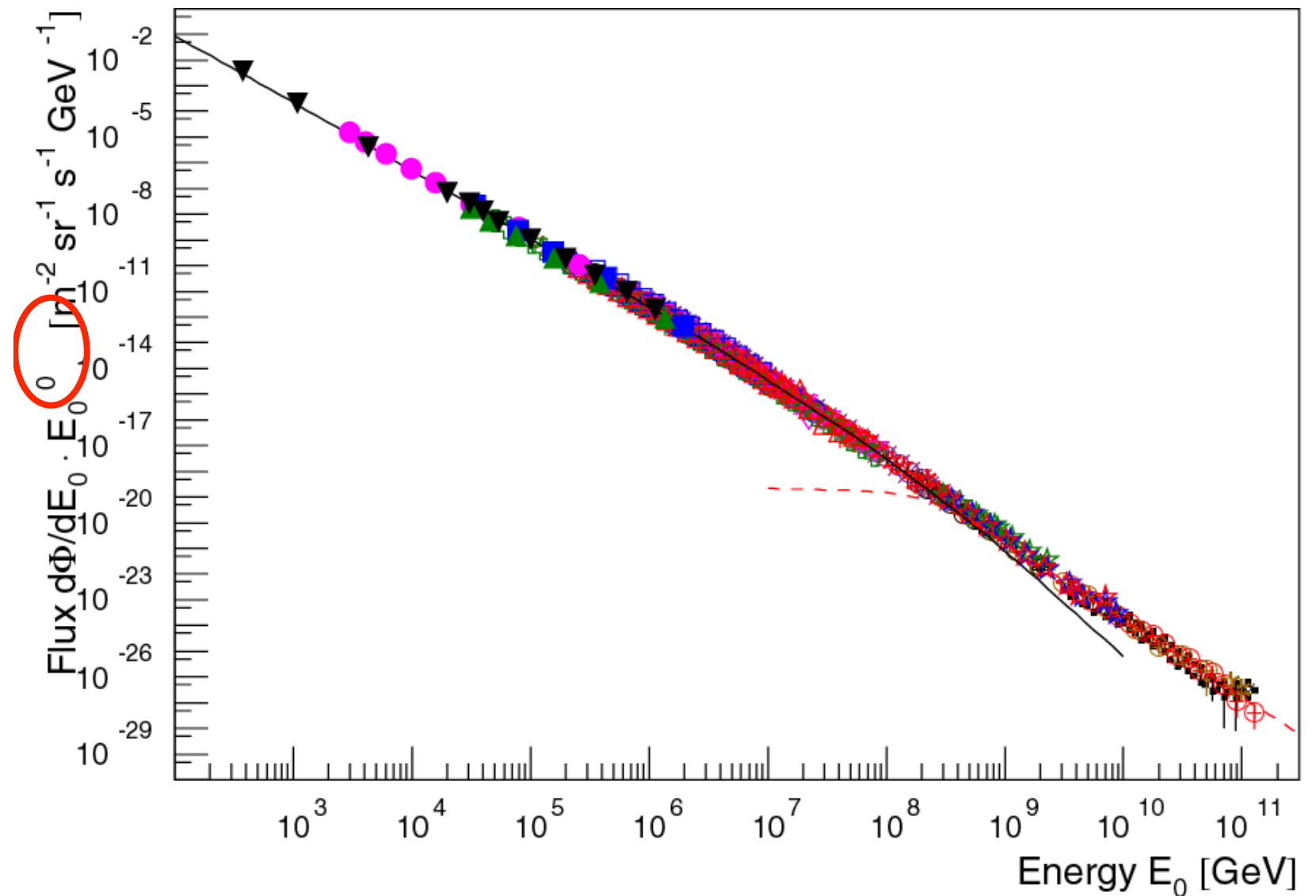
Cosmic rays at the knee

Results and implications



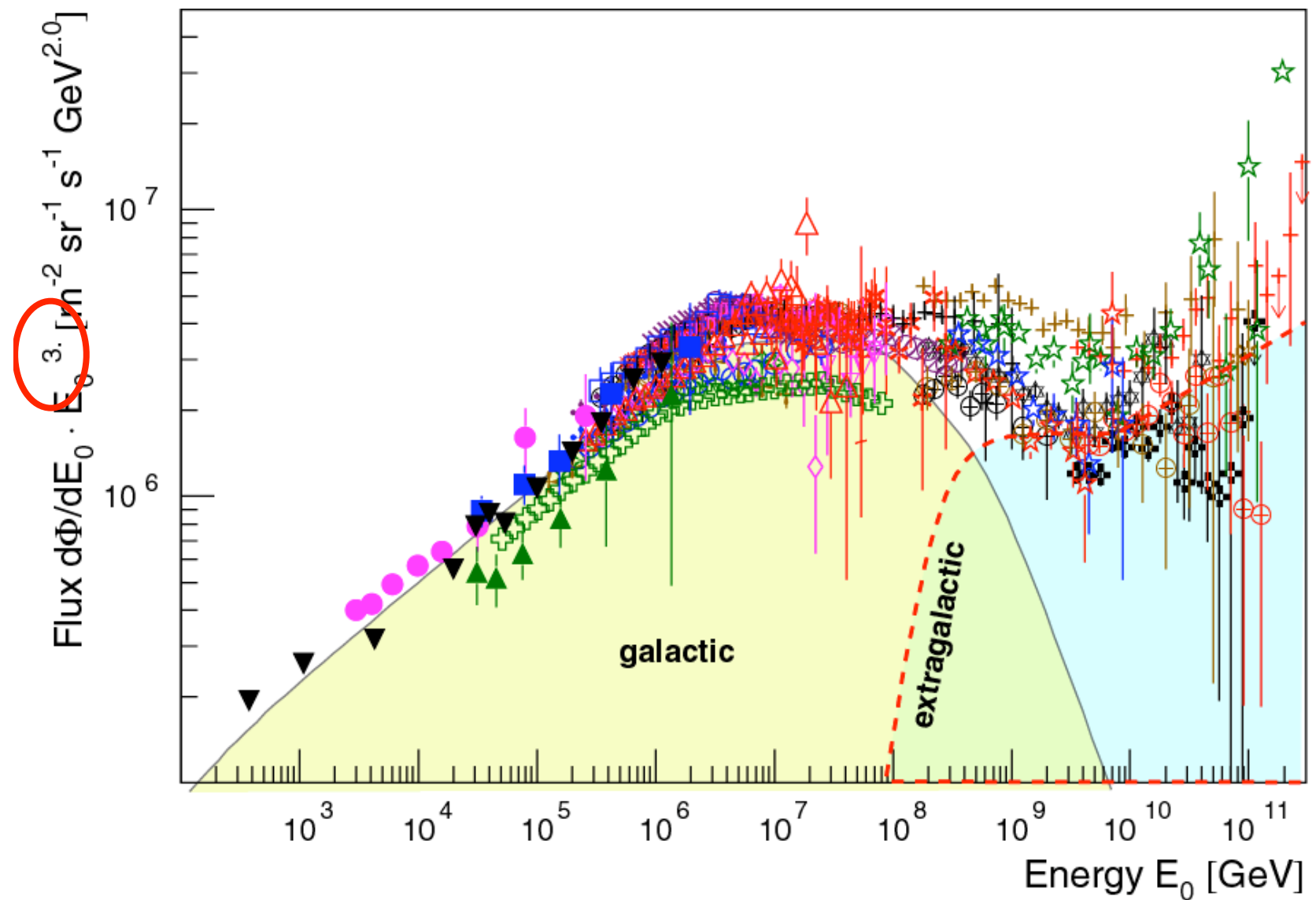
Cosmic rays at the knee

Results and implications



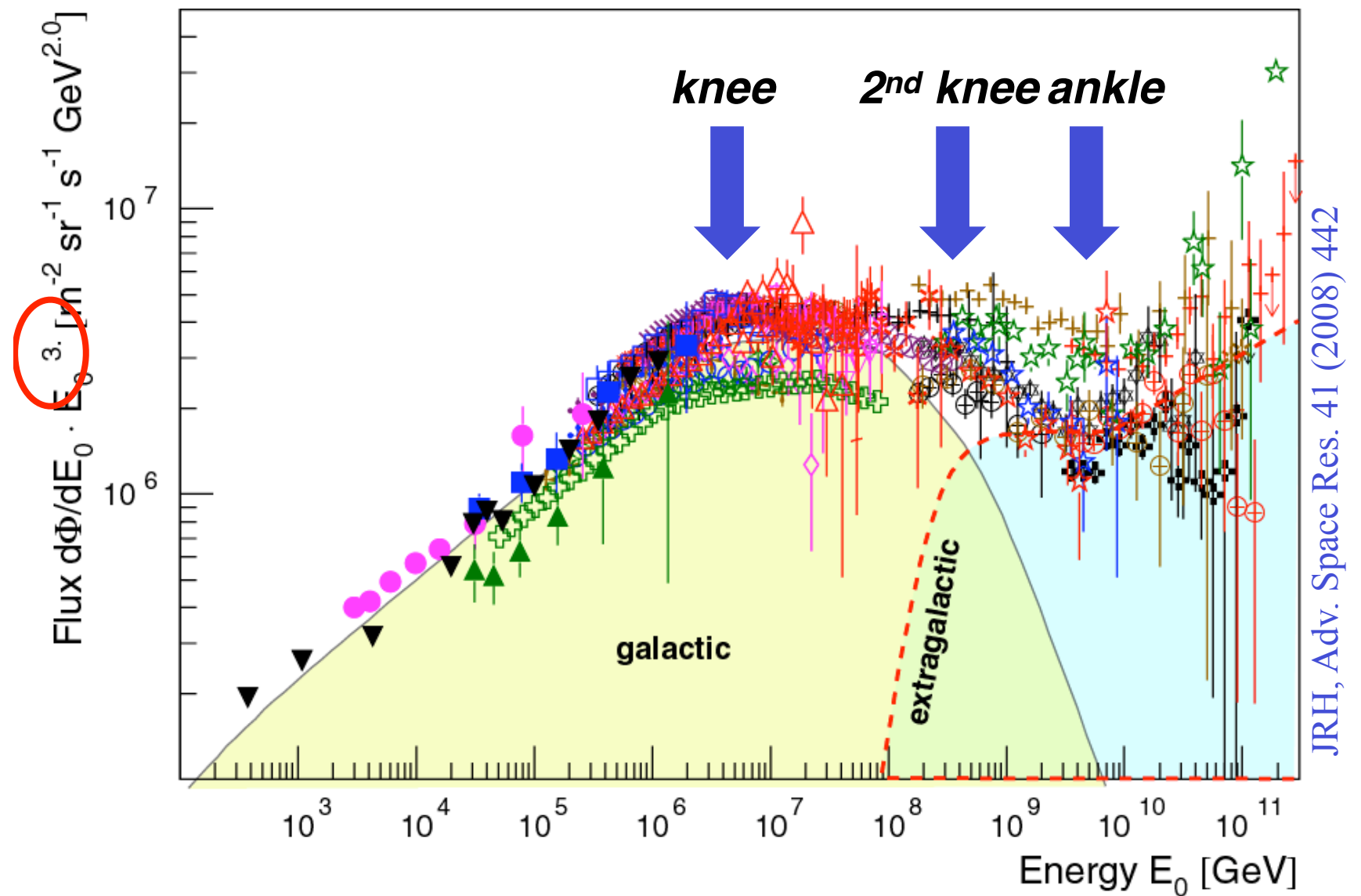
Cosmic rays at the knee

Results and implications



Cosmic rays at the knee

Results and implications

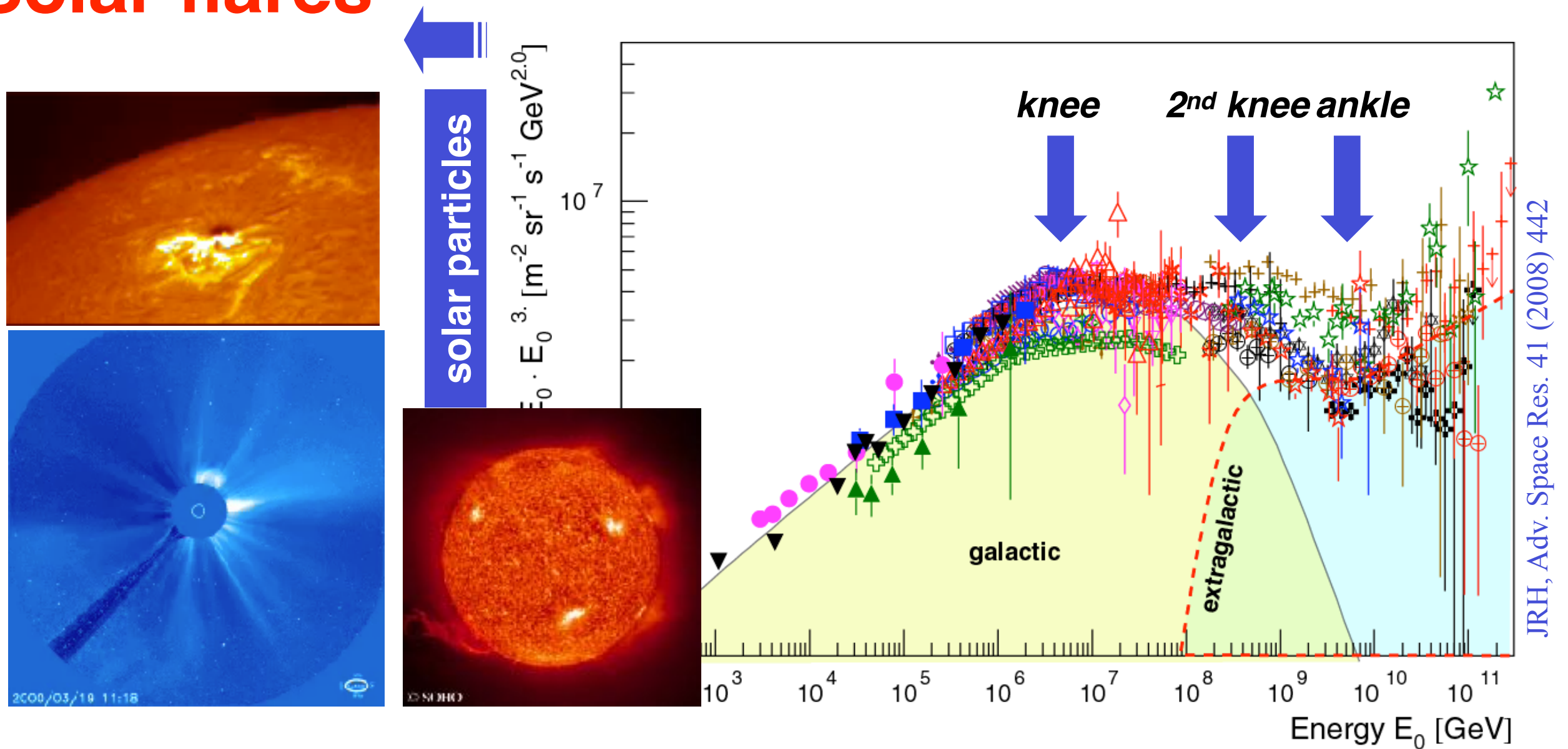


JRH, Adv. Space Res. 41 (2008) 442

Cosmic rays at the knee

Results and implications

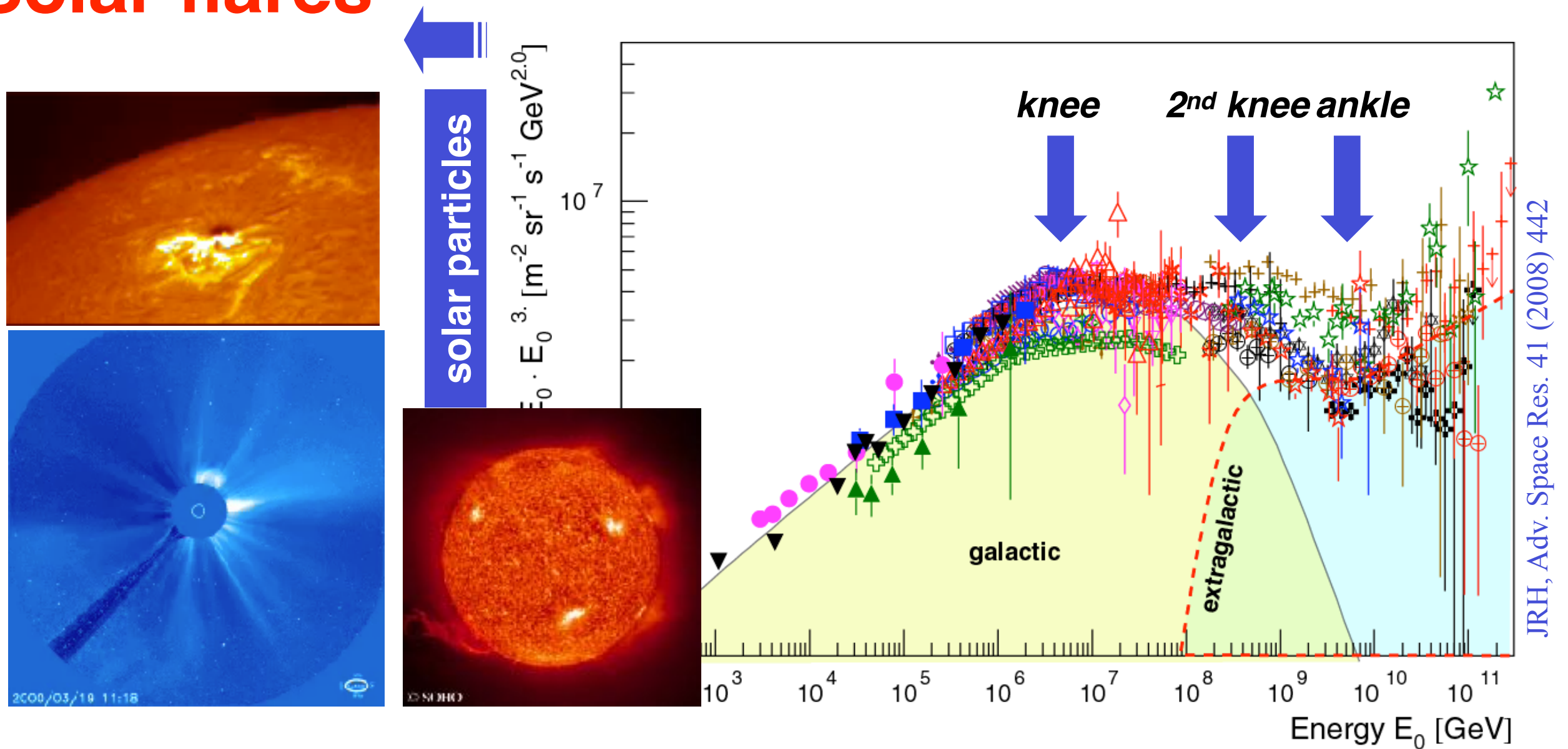
Solar flares



Cosmic rays at the knee

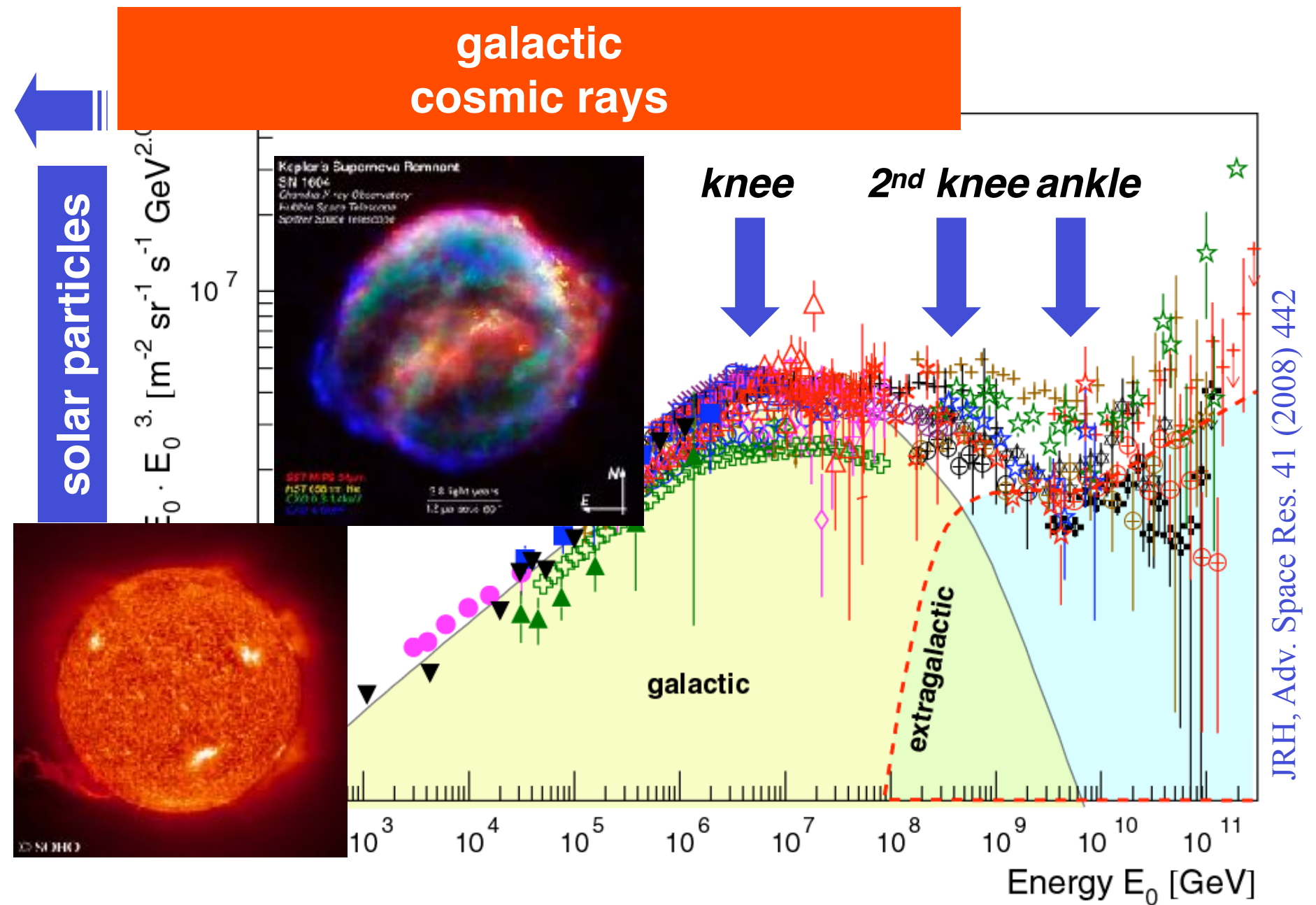
Results and implications

Solar flares



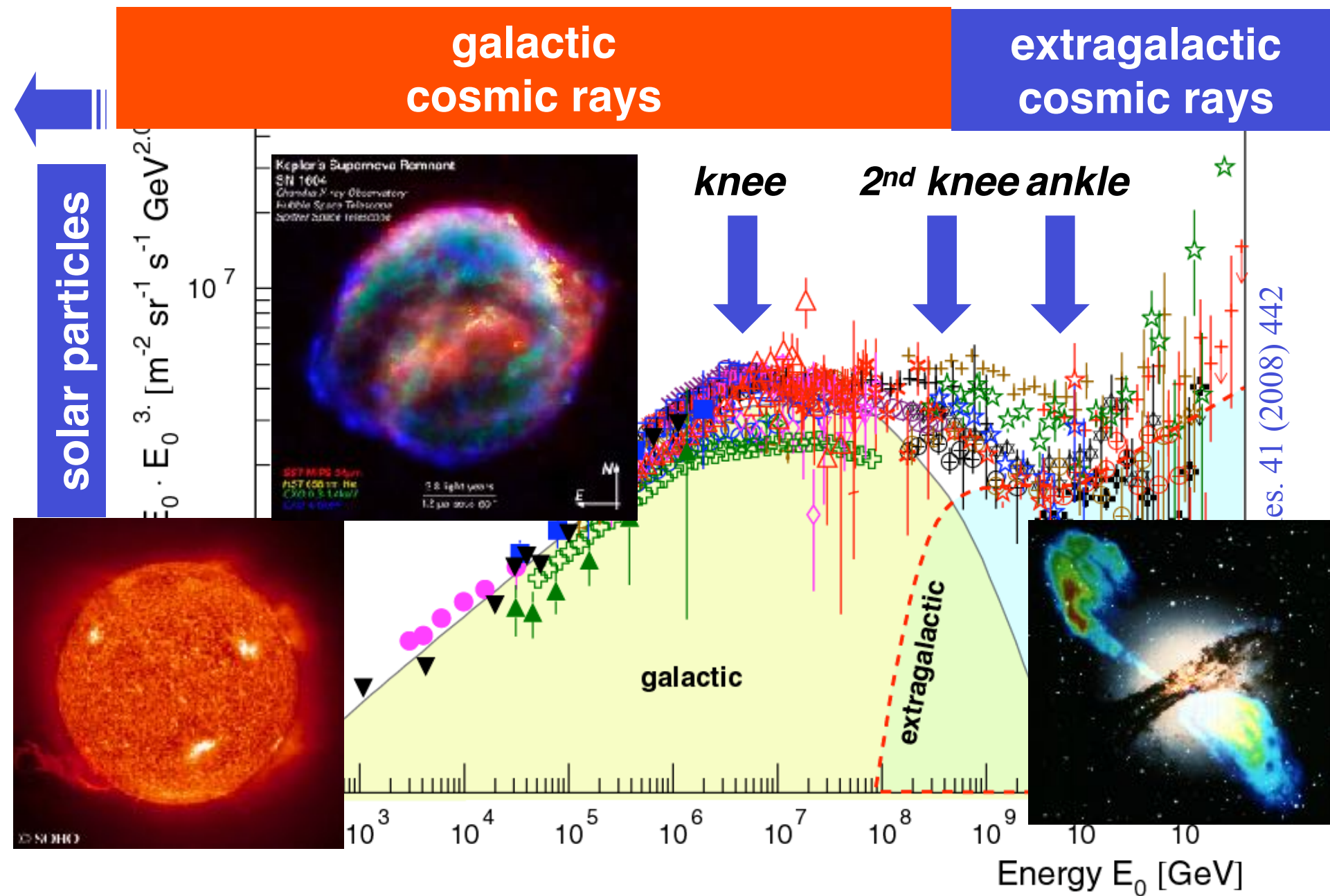
Cosmic rays at the knee

Results and implications



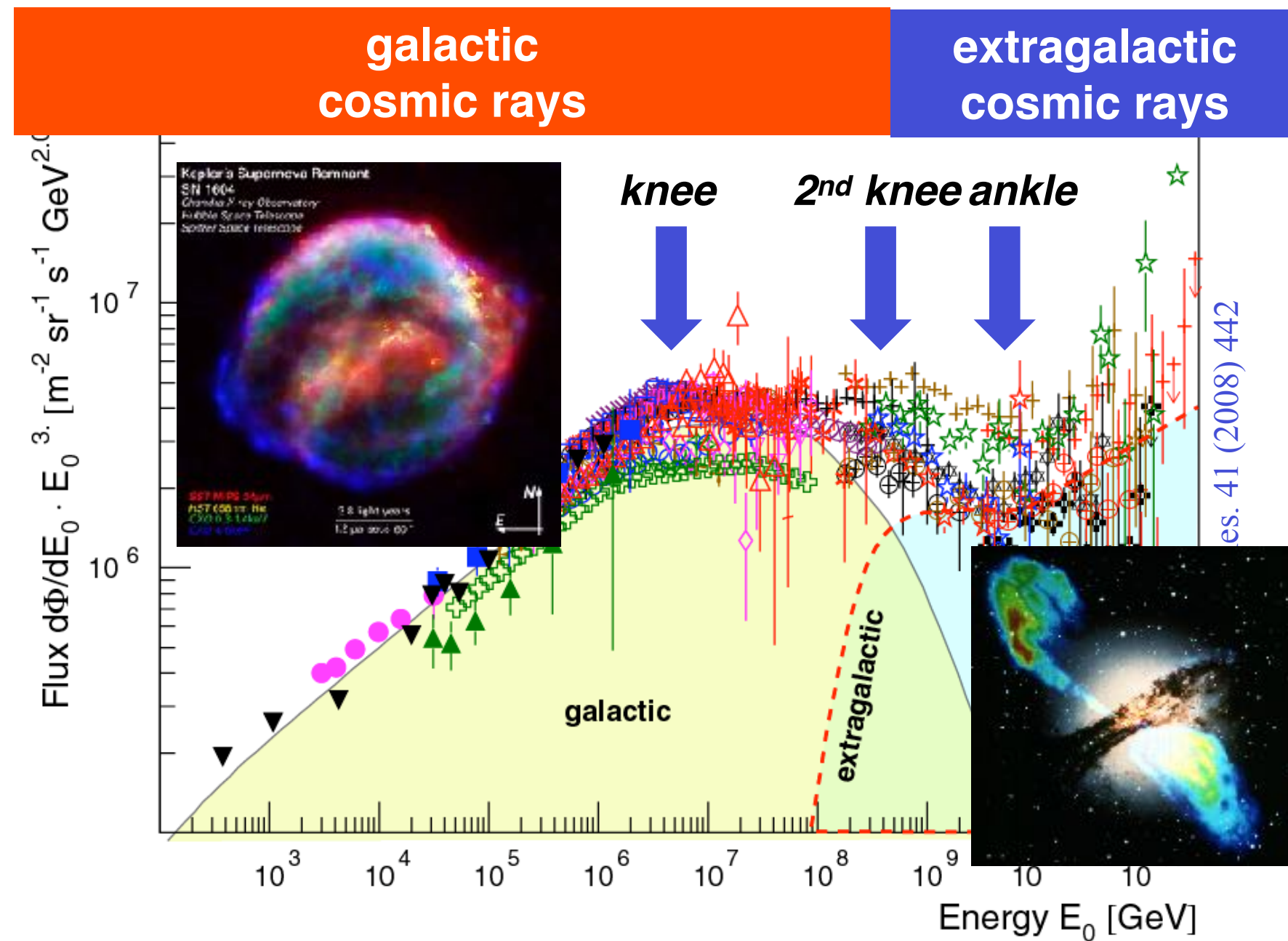
Cosmic rays at the knee

Results and implications



Cosmic rays at the knee

Results and implications

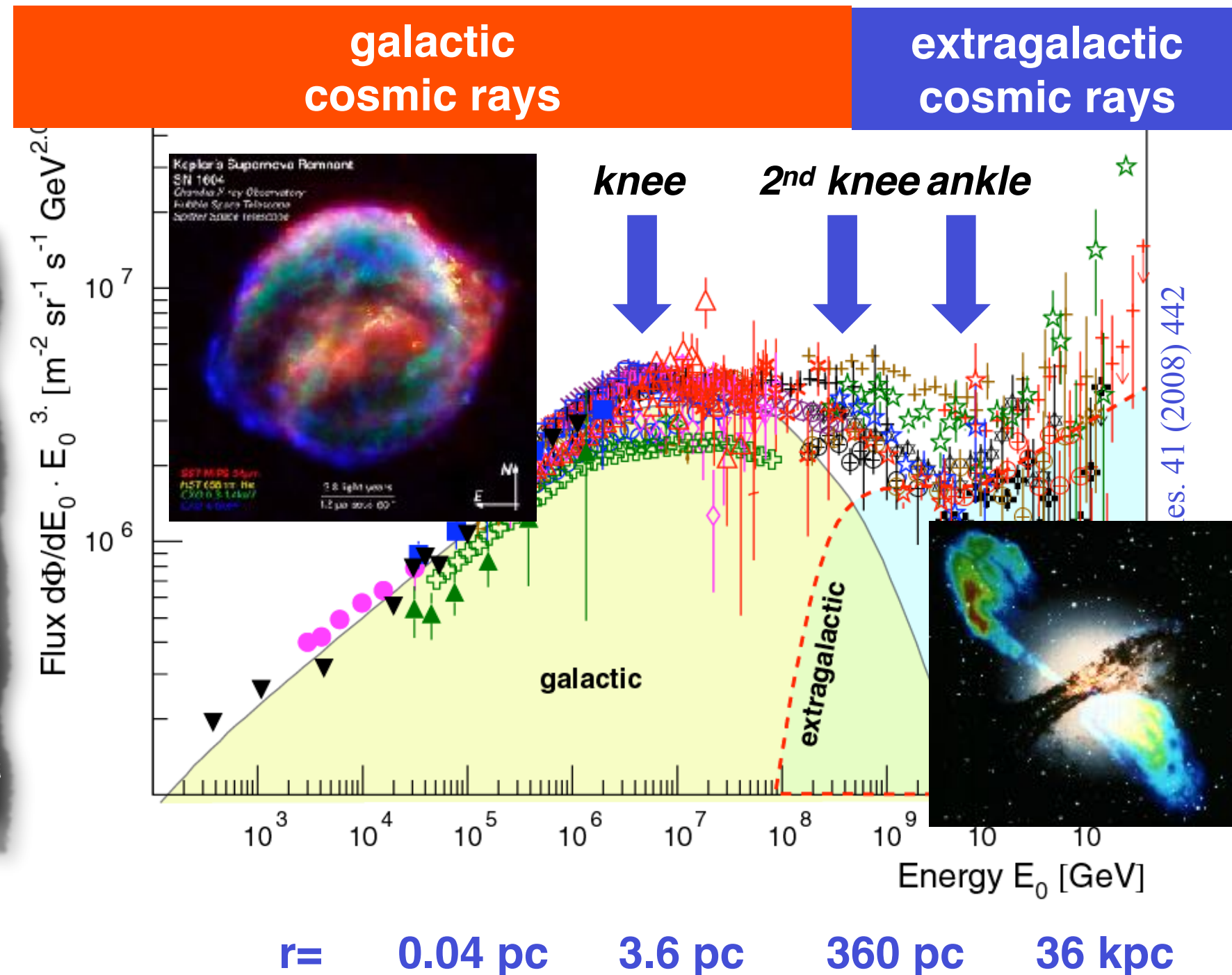


Cosmic rays at the knee

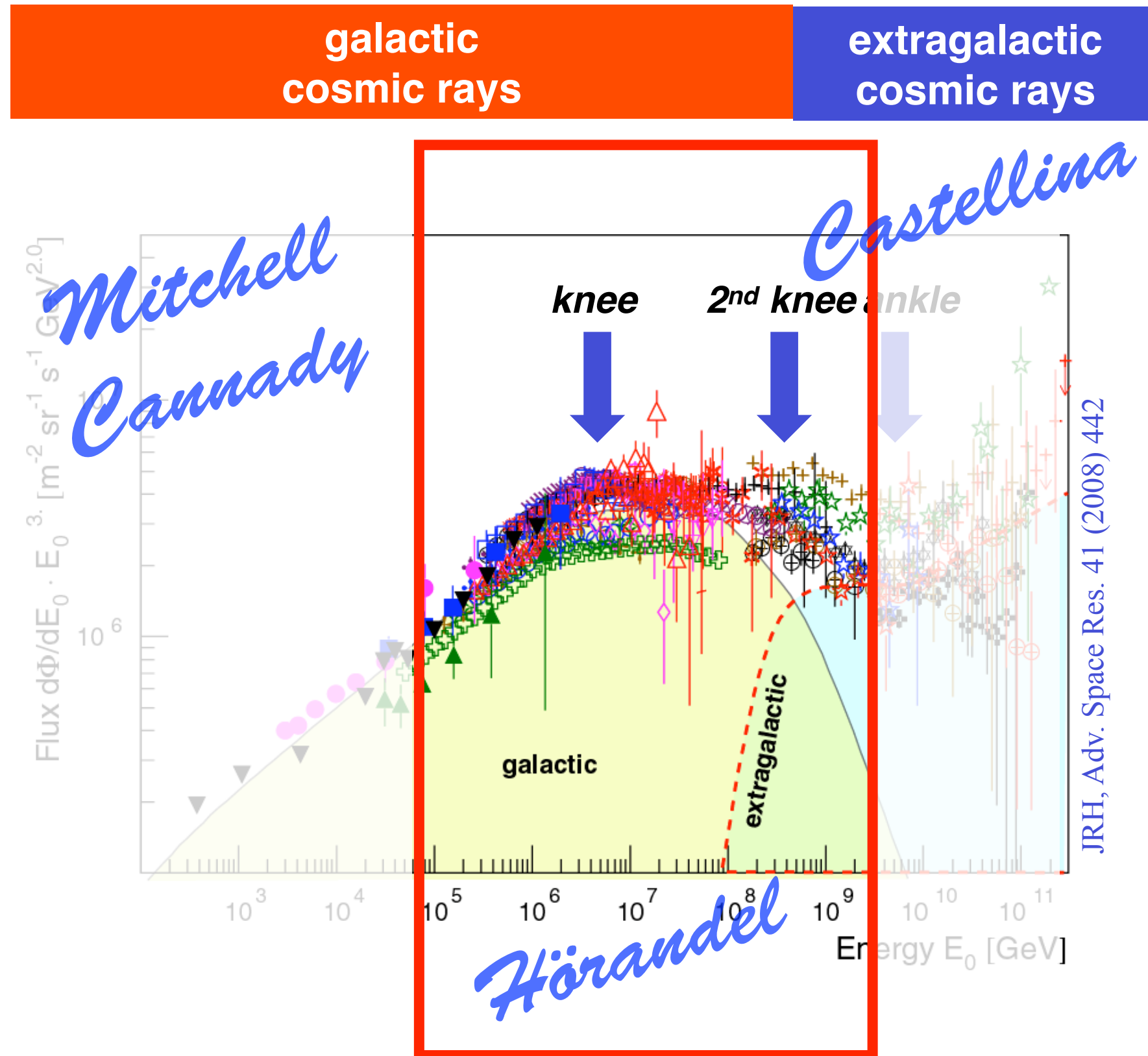
Results and implications

Radius of particle
in magnetic field

$$r = \frac{p}{ZeB} \quad r[\text{pc}] = 1.08 * \frac{E [\text{PeV}]}{B [\mu\text{G}]}$$



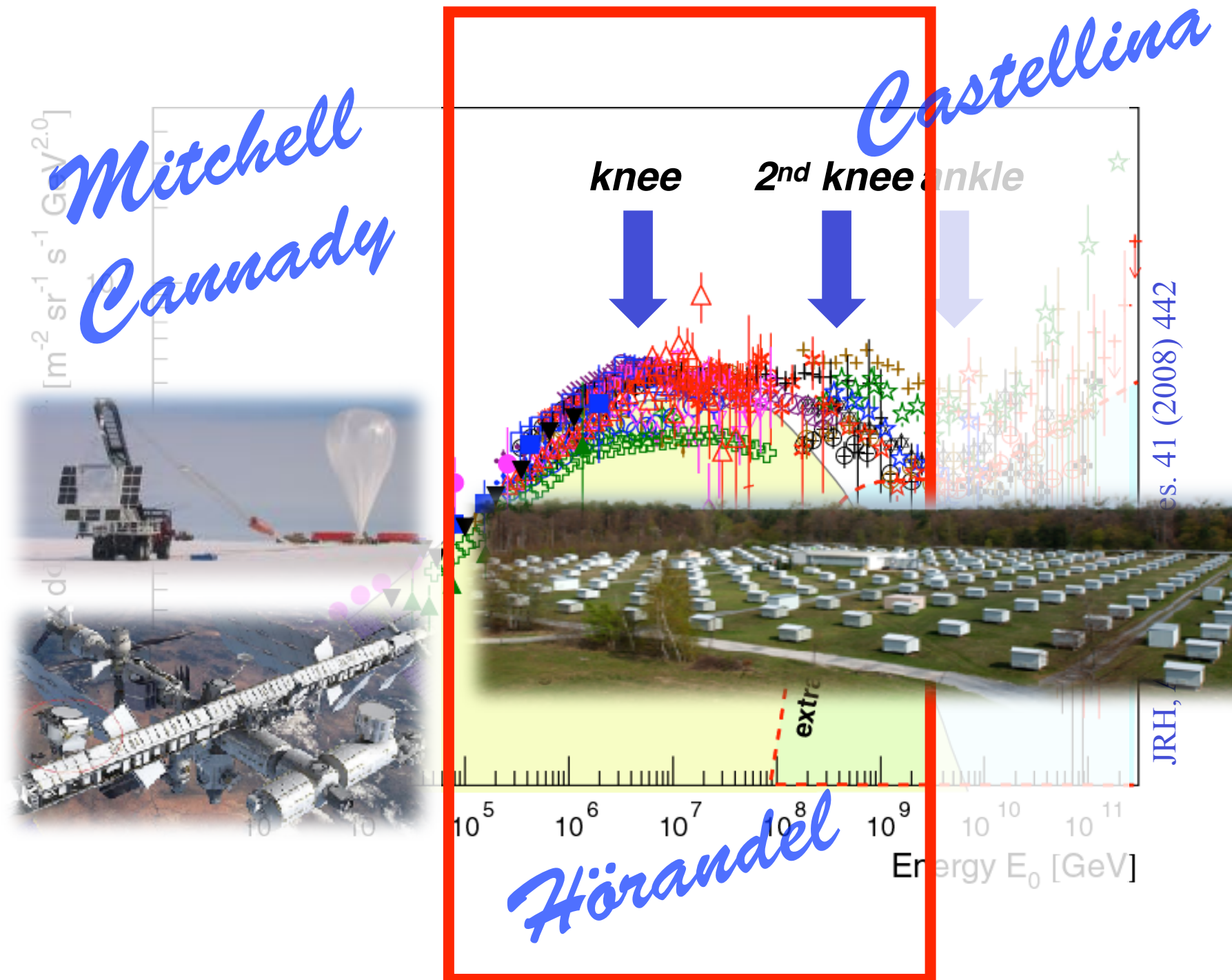
Cosmic rays at the knee



Cosmic rays at the knee

galactic
cosmic rays

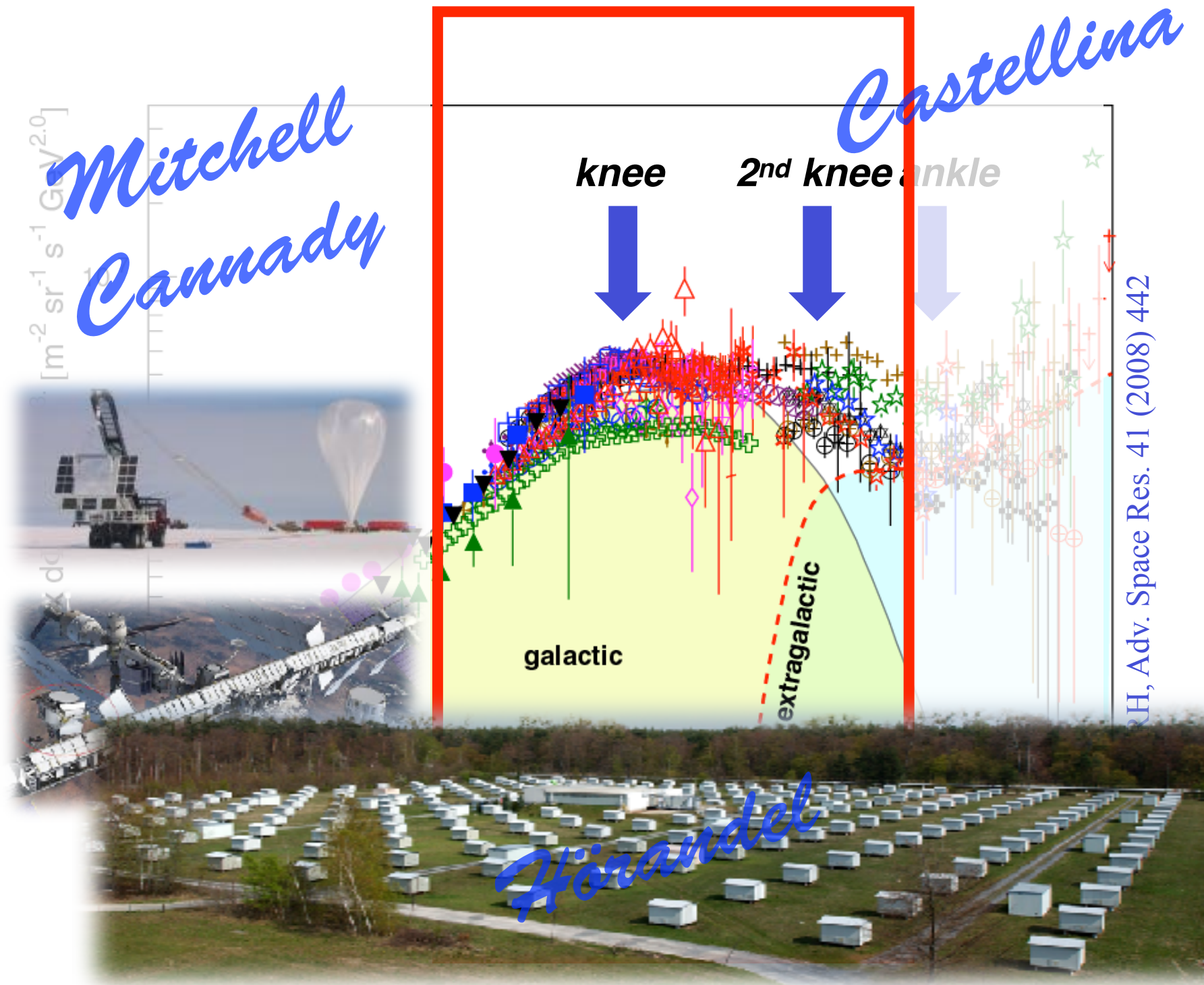
extragalactic
cosmic rays



Cosmic rays at the knee

galactic
cosmic rays

extragalactic
cosmic rays



Extensive Air Showers

electromagnetic hadronic muonic
shower component

~ 98%

< 1%

~2%



Extensive Air Showers



electromagnetic hadronic muonic
shower component

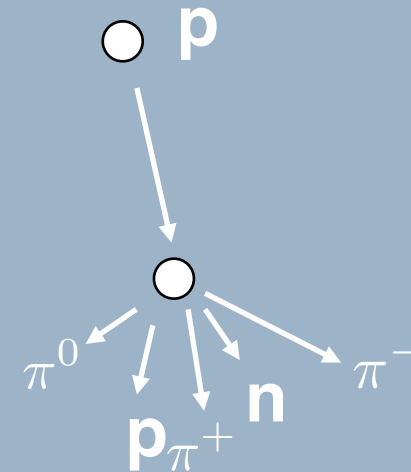
~ 98%

< 1%

~2%



Extensive Air Showers



electromagnetic **hadronic** **muonic**
shower component

$\sim 98\%$

$< 1\%$

$\sim 2\%$



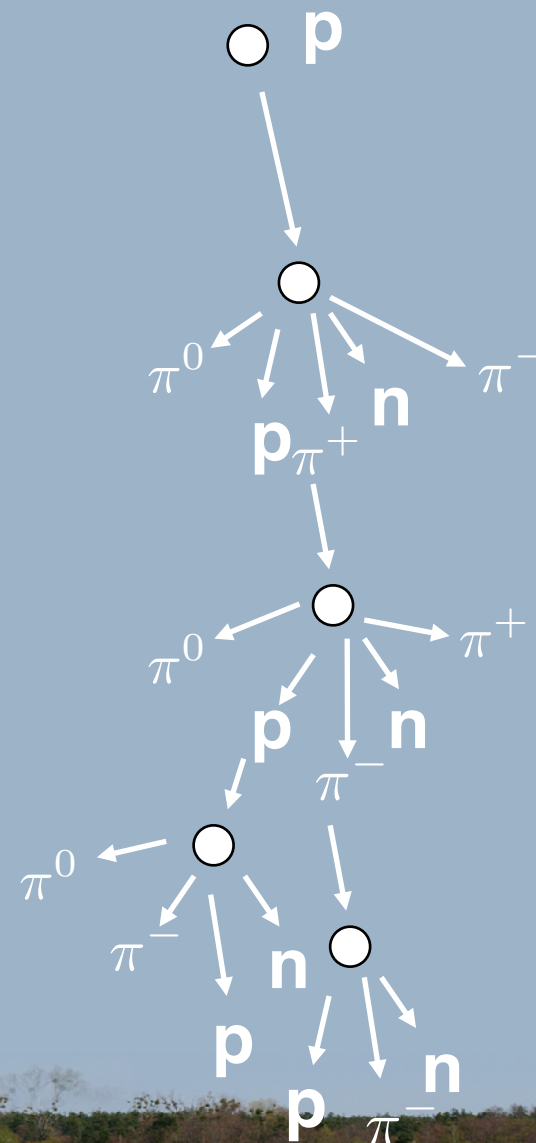
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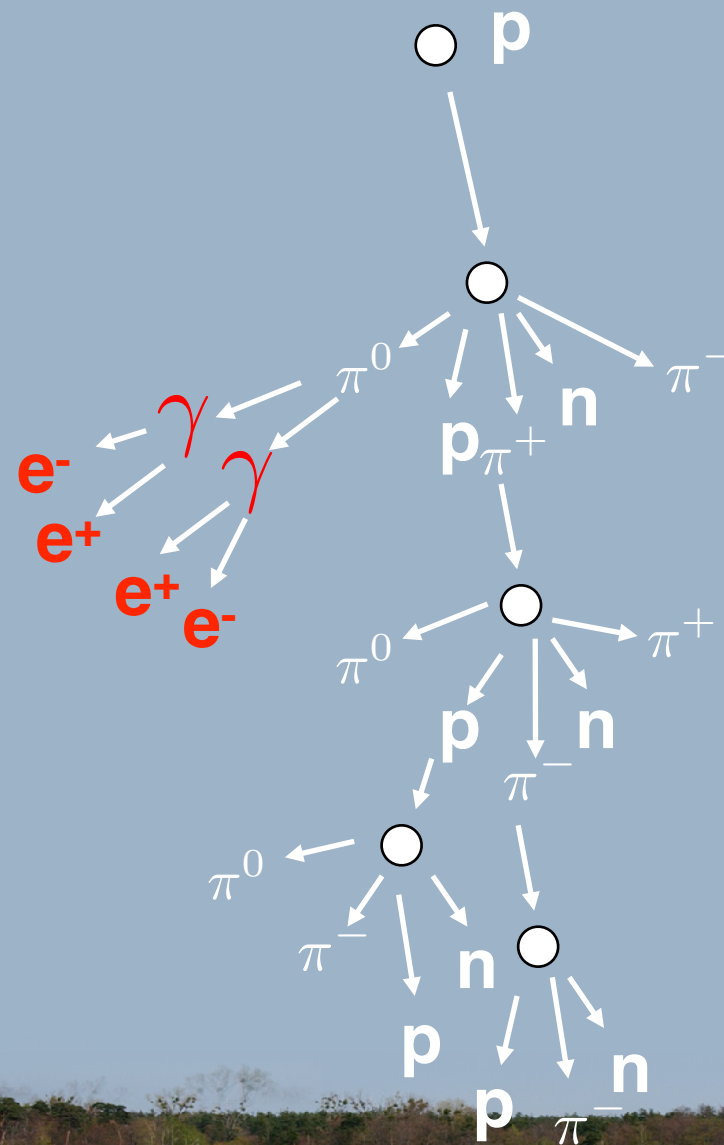
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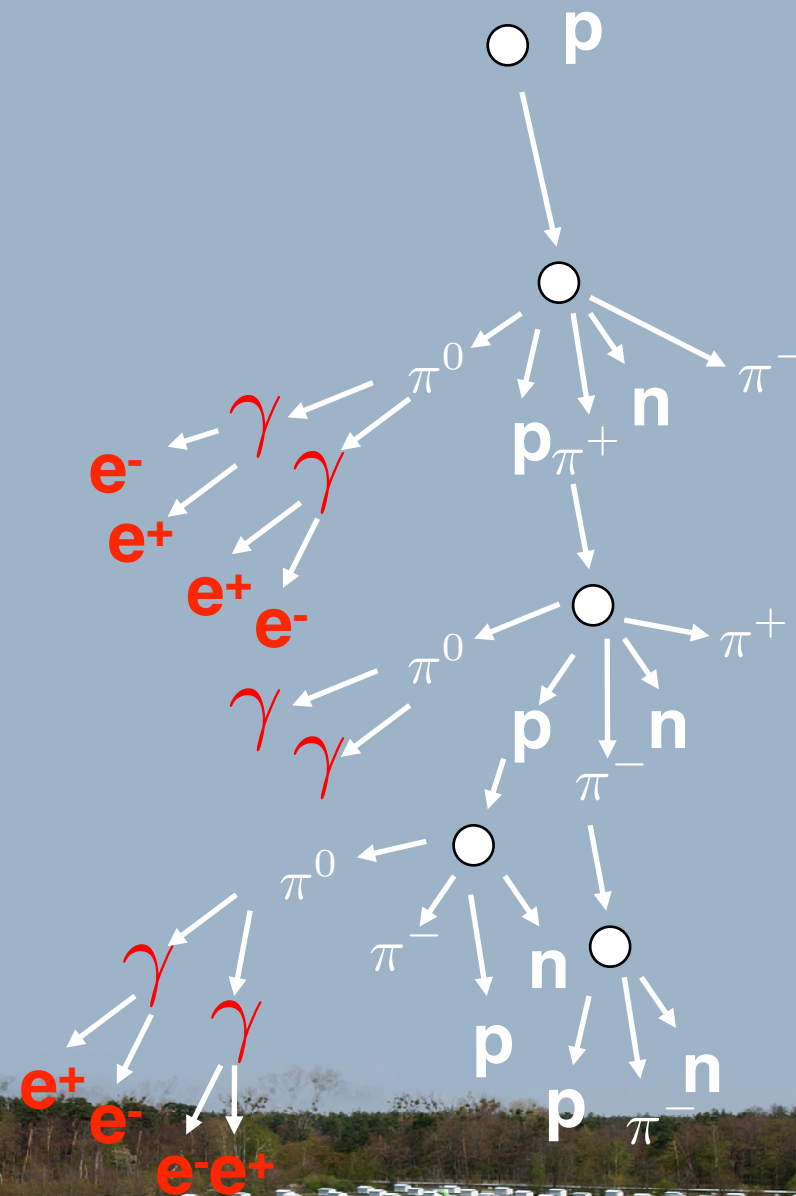
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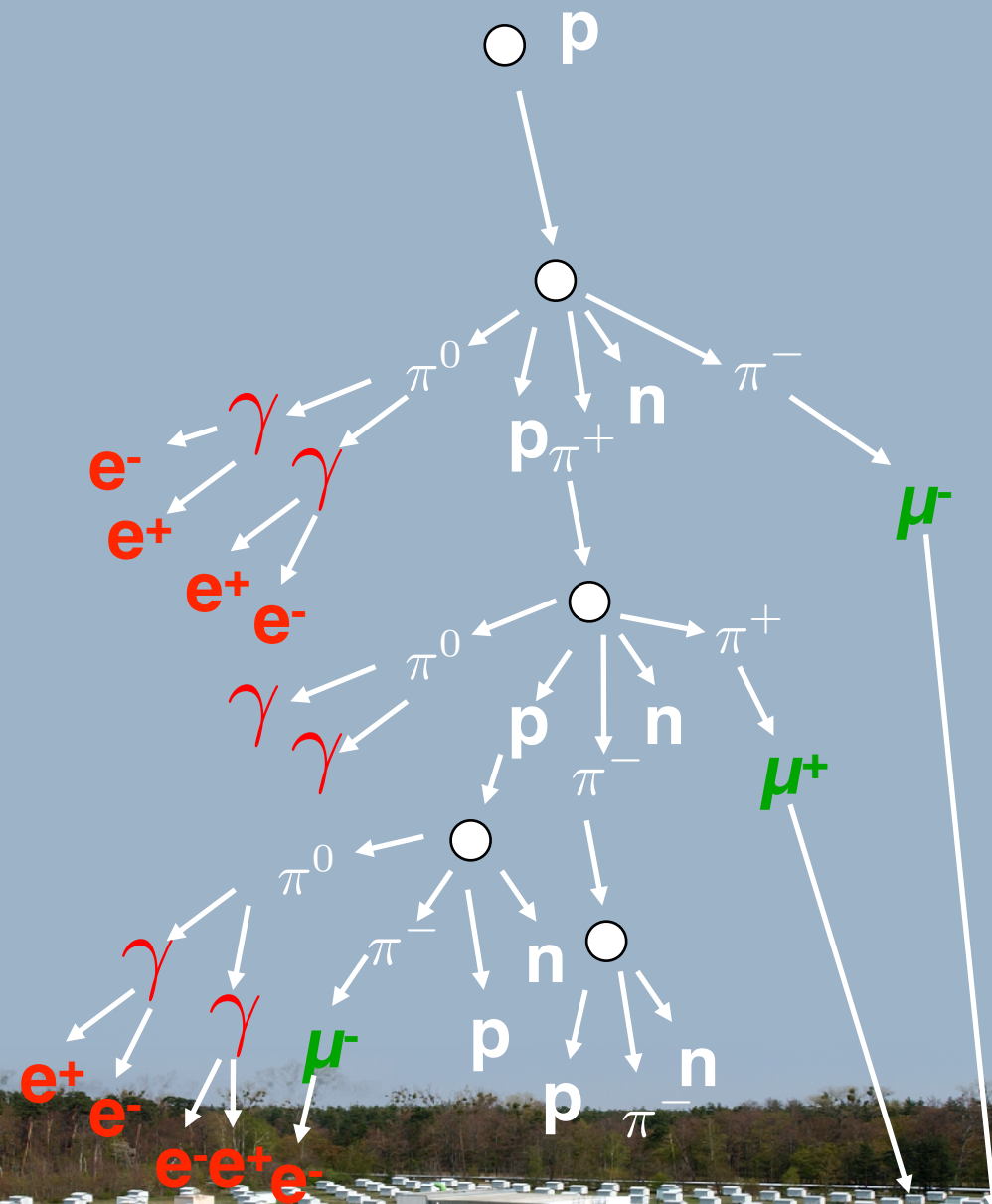
Extensive Air Showers

electromagnetic **hadronic** **muonic**
shower component

~ 98%

< 1%

~2%



A Matthews Heitler Model – mass resolution in EAS measurements

depth of shower maximum

$$X_{\max}^A = X_{\max}^p - X_0 \ln A$$

radiation length $X_0=36.7$ g/cm²

electron-muon ratio

$$\lg(N_e/N_\mu) = C - 0.065 \ln A.$$

A Matthews Heitler Model – mass resolution in EAS measurements

depth of shower maximum

$$X_{\max}^A = X_{\max}^p - X_0 \ln A$$

radiation length $X_0=36.7$ g/cm²

typical uncertainty

$$\Delta X_{\max} \approx 20 \text{ g/cm}^2$$

electron-muon ratio

$$\lg(N_e/N_\mu) = C - 0.065 \ln A.$$

$$\Delta \frac{N_e}{N_\mu} \approx 16\% - 20\%$$

A Matthews Heitler Model – mass resolution in EAS measurements

depth of shower maximum

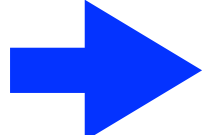
$$X_{\max}^A = X_{\max}^p - X_0 \ln A$$

radiation length $X_0=36.7 \text{ g/cm}^2$

typical uncertainty

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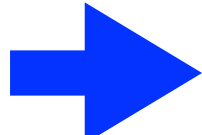
expected mass resolution


$$\Delta \ln A \approx 0.8 - 1$$

electron-muon ratio

$$\lg(N_e/N_\mu) = C - 0.065 \ln A.$$

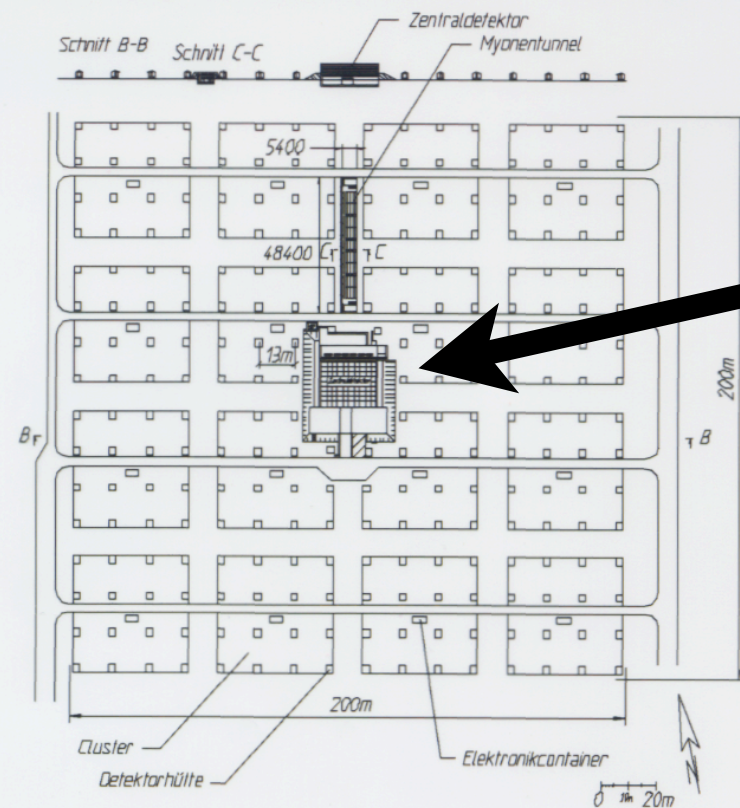
$$\Delta \frac{N_e}{N_\mu} \approx 16\% - 20\%$$



4 to 5 mass groups
p, He, CNO, (Si), Fe

The KASCADE Array

200 m



Array

200 m

252 stations with

□ e/γ detectors: 4 cm liquid scintillator ($\approx 3.1 \text{ m}^2$)

□ muon detectors: 3 cm plastic scintillator ($\approx 3.2 \text{ m}^2$)

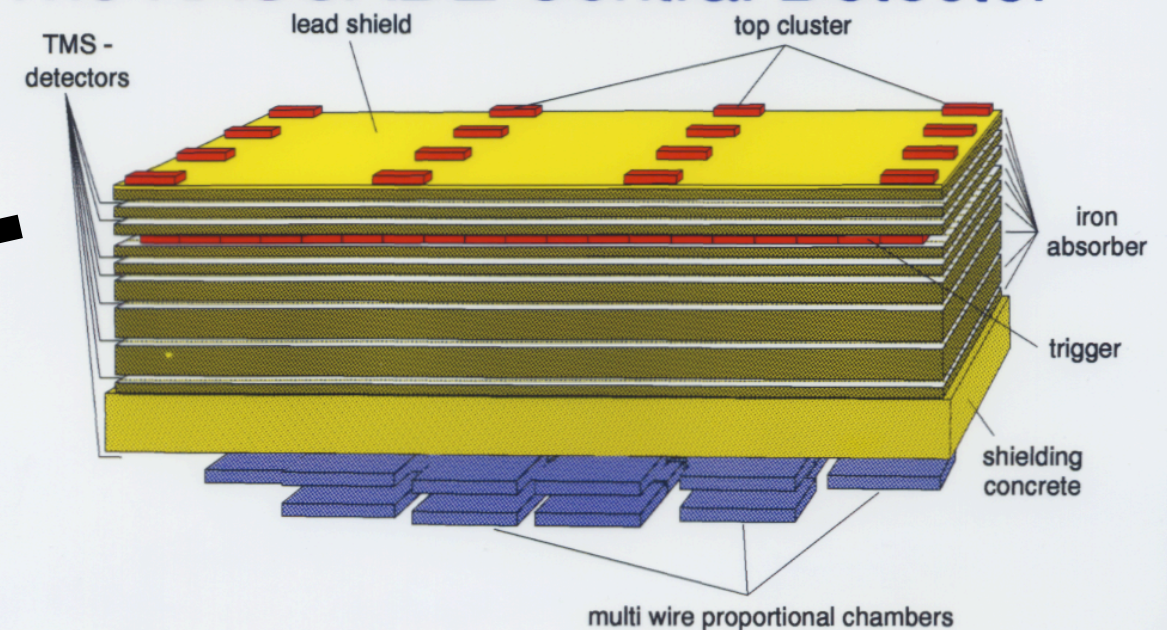
shield 10 cm Pb + 4 cm Fe $\rightarrow 20 X_0$

⇒ $E_\mu > 300 \text{ MeV}$

→ measurement of particle densities and arrival times

JRH 06/96

The KASCADE Central Detector



4 different detector systems:

□ Top array $32 \times 0.45 \text{ m}^2$ scintillation counters (14 m^2)

□ Trigger layer $456 \times 0.45 \text{ m}^2$ scintillation counters (206 m^2)

□ 32 Multiwire proportional chambers ($2 \times 150 \text{ m}^2$) $E_\mu > 2 \text{ GeV}$

□ Iron sampling calorimeter ($16 \times 20 \text{ m}^2$)

8 active layers $\rightarrow 10\,000$ liquid ionisation chambers

40 000 electronic channels

separation of individual hadrons by a fine segmentation

depth $\approx 11 \lambda_i \rightarrow$ hadrons up to 10 TeV 95% contained

JRH 06/96

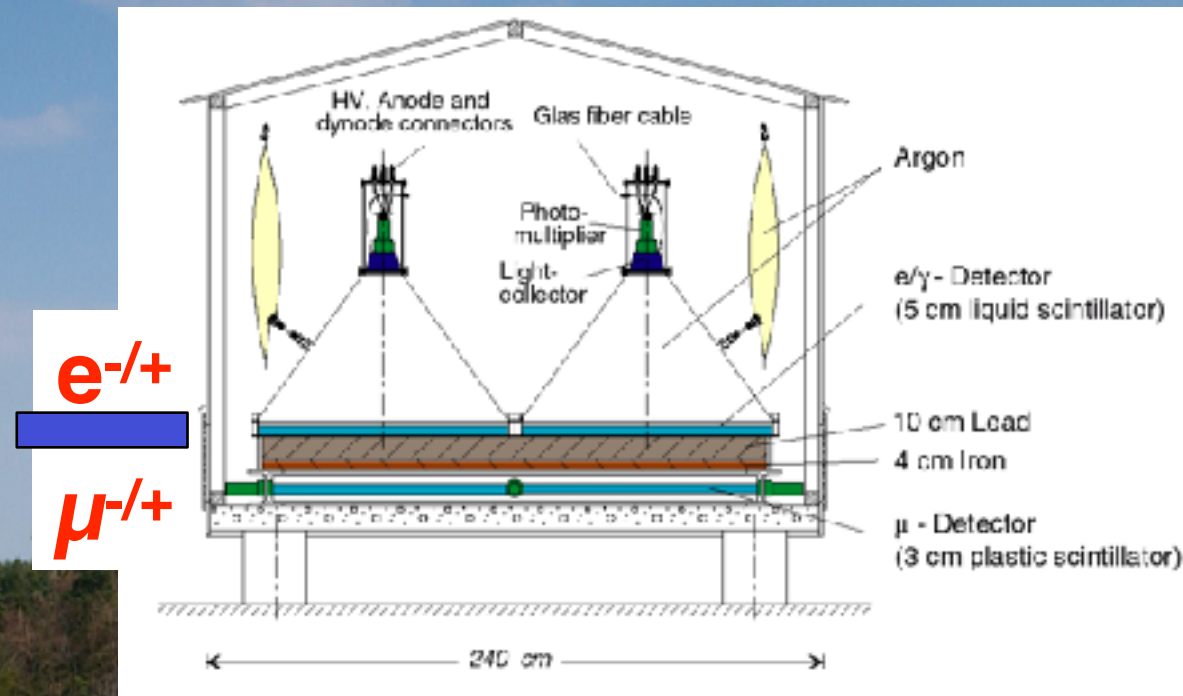
KArlsruhe Shower Core and Array DEtector

**Simultaneous measurement of
electromagnetic,
muonic,
hadronic
shower components**



KArlsruhe Shower Core and Array DEtector

Simultaneous measurement of
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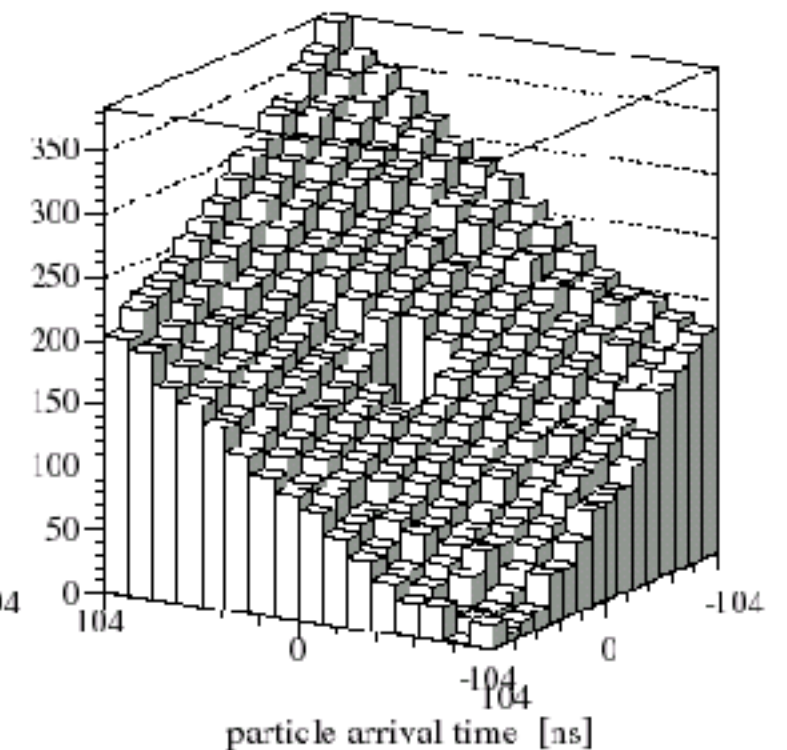
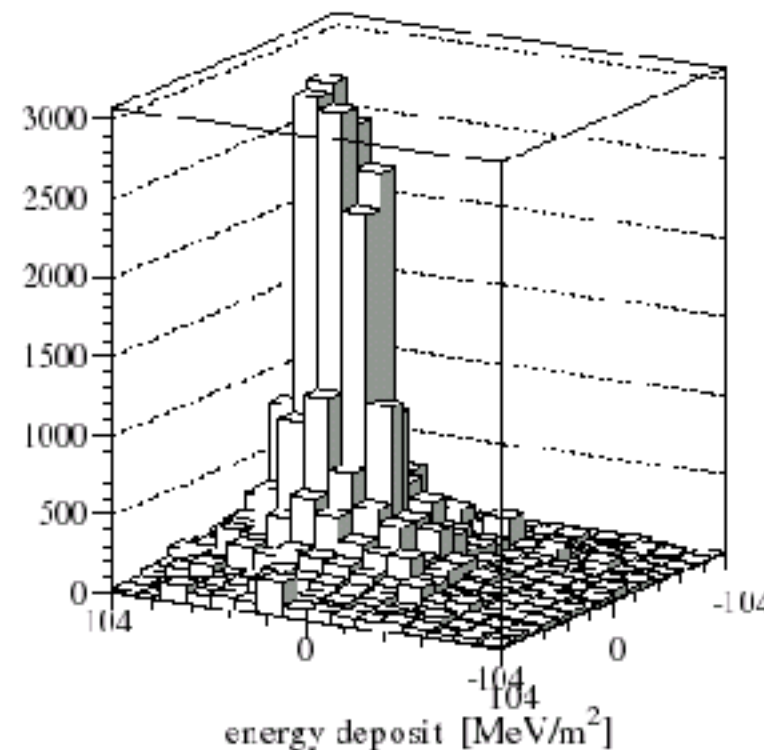
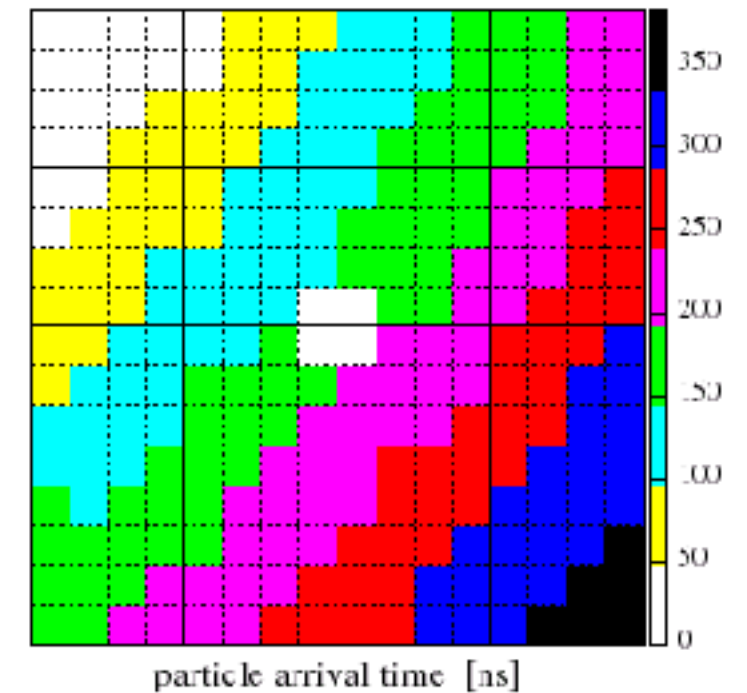
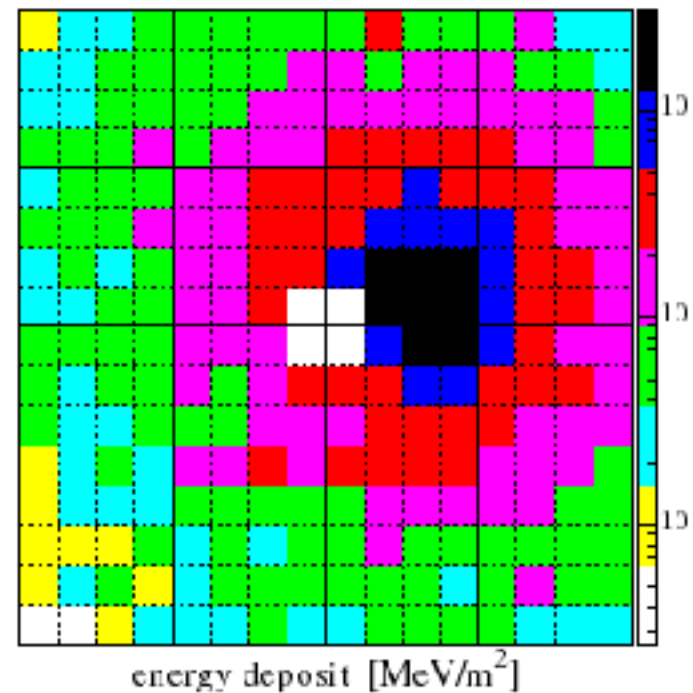


Event reconstruction in the scintillator array

electromagnetic component

shower core	$\Delta r = 2.5 - 5.5 \text{ m}$
shower direction	$\Delta\alpha = 0.5^\circ - 1.2^\circ$
shower size	$\Delta N_e/N_e = 6 - 12 \%$

e/ γ -Detectors, Run 1, Event 71089, 96-03-05 22:07:48.956078



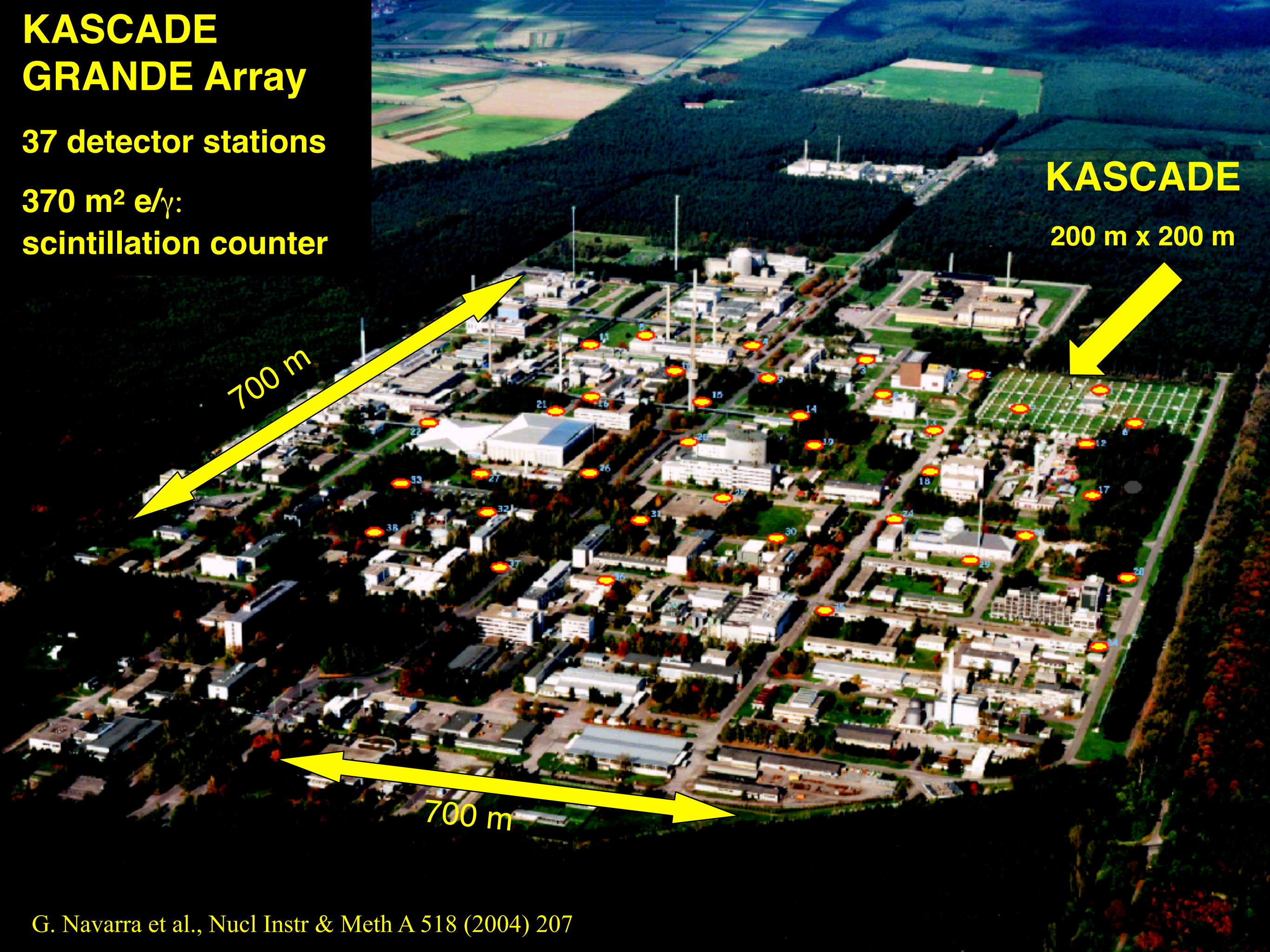
KASCADE GRANDE Array

37 detector stations

370 m² e/ γ :
scintillation counter

KASCADE

200 m x 200 m



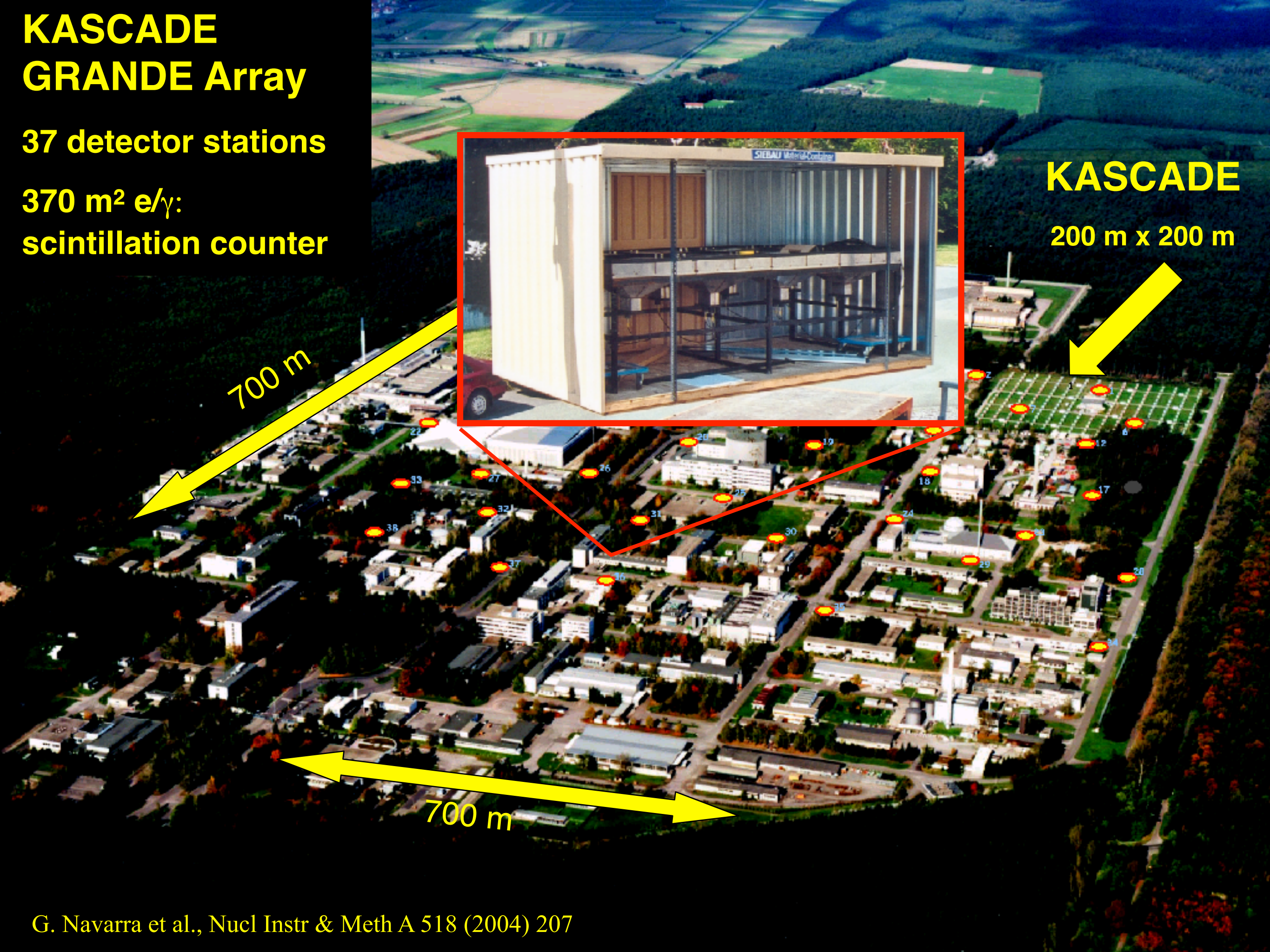
KASCADE GRANDE Array

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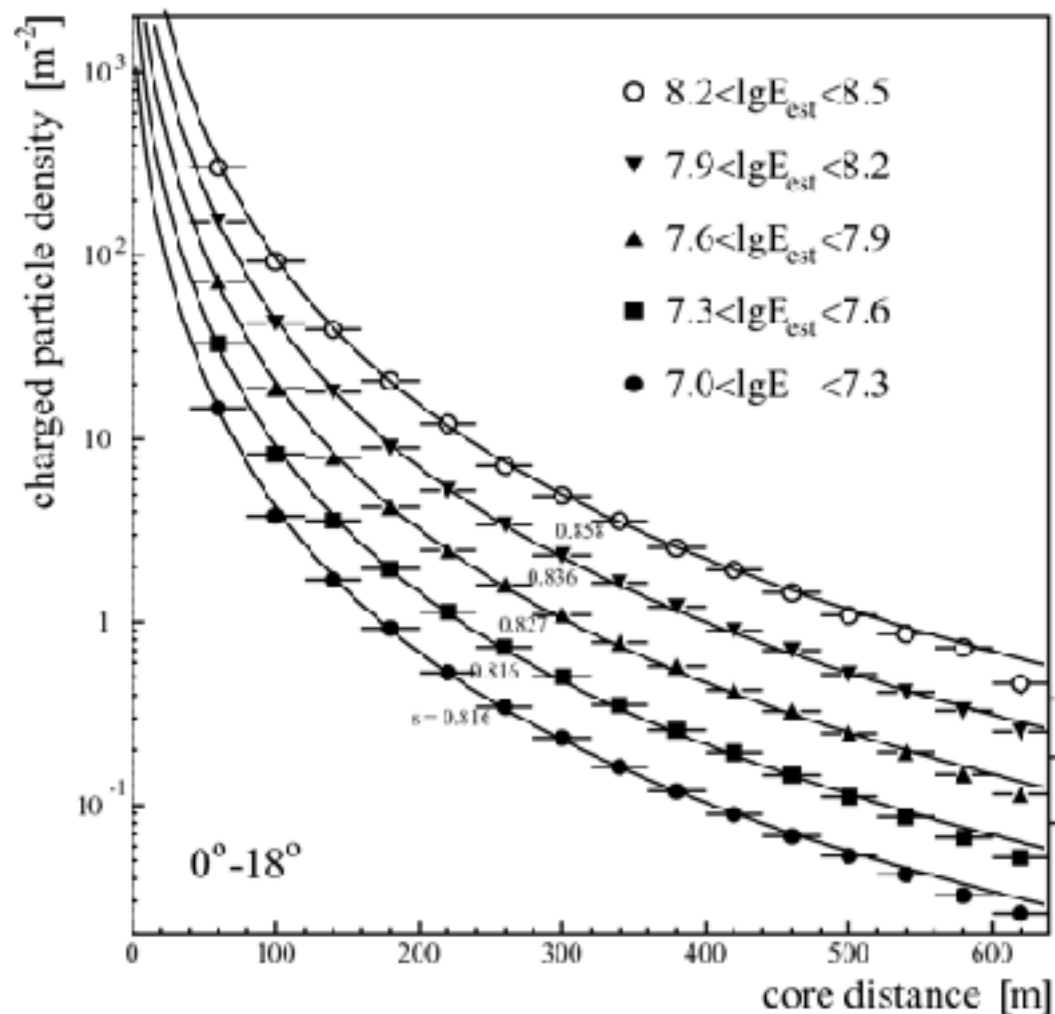
KASCADE

200 m x 200 m

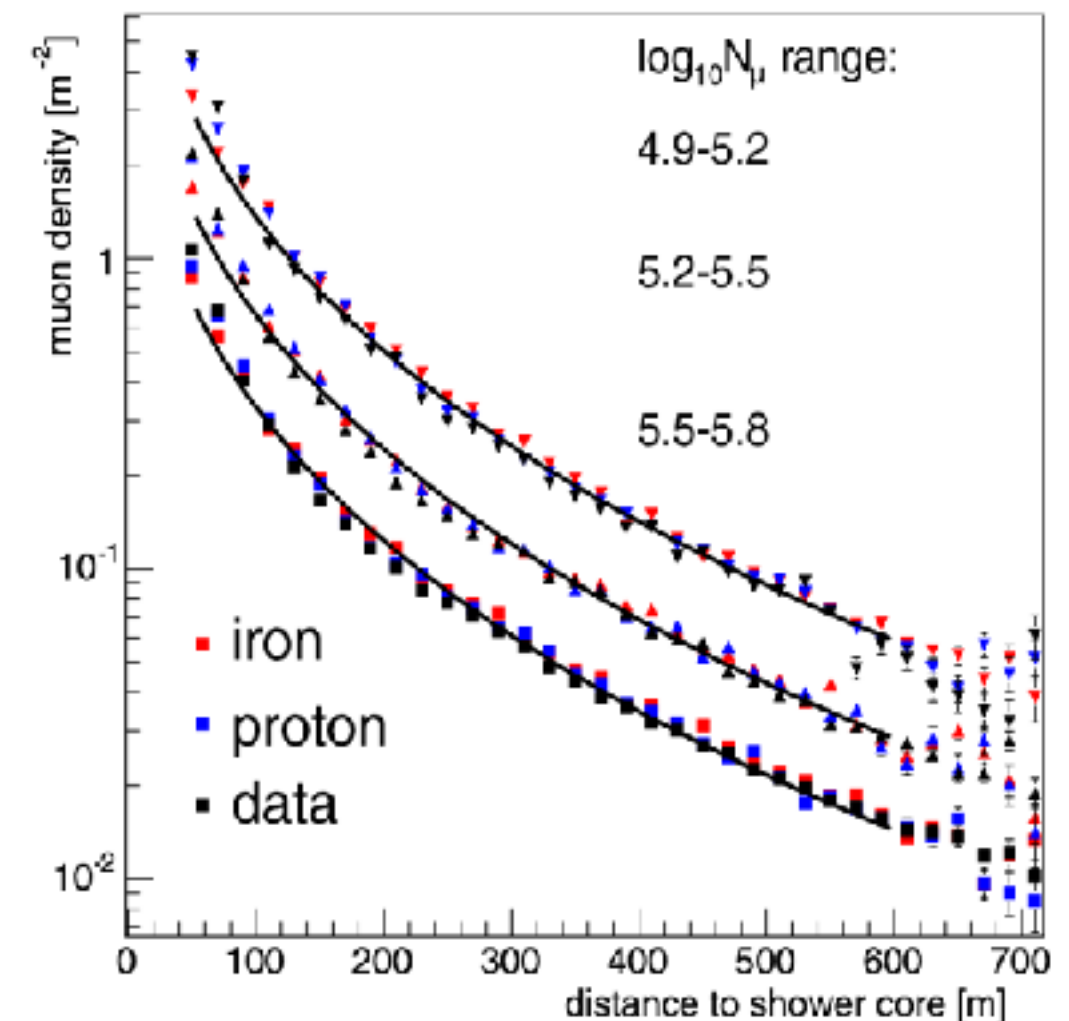


KASCADE-Grande – Lateral distributions

Electromagnetic component



Muons



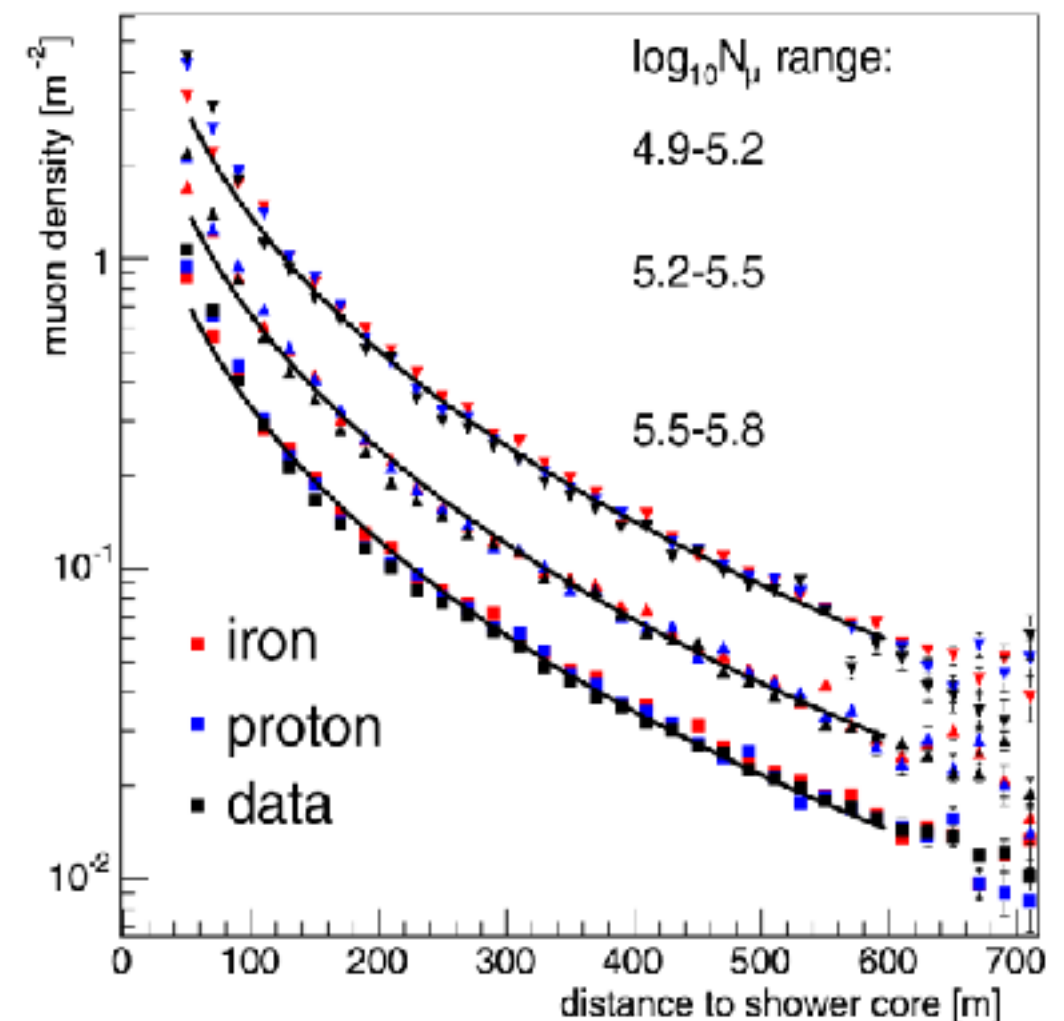
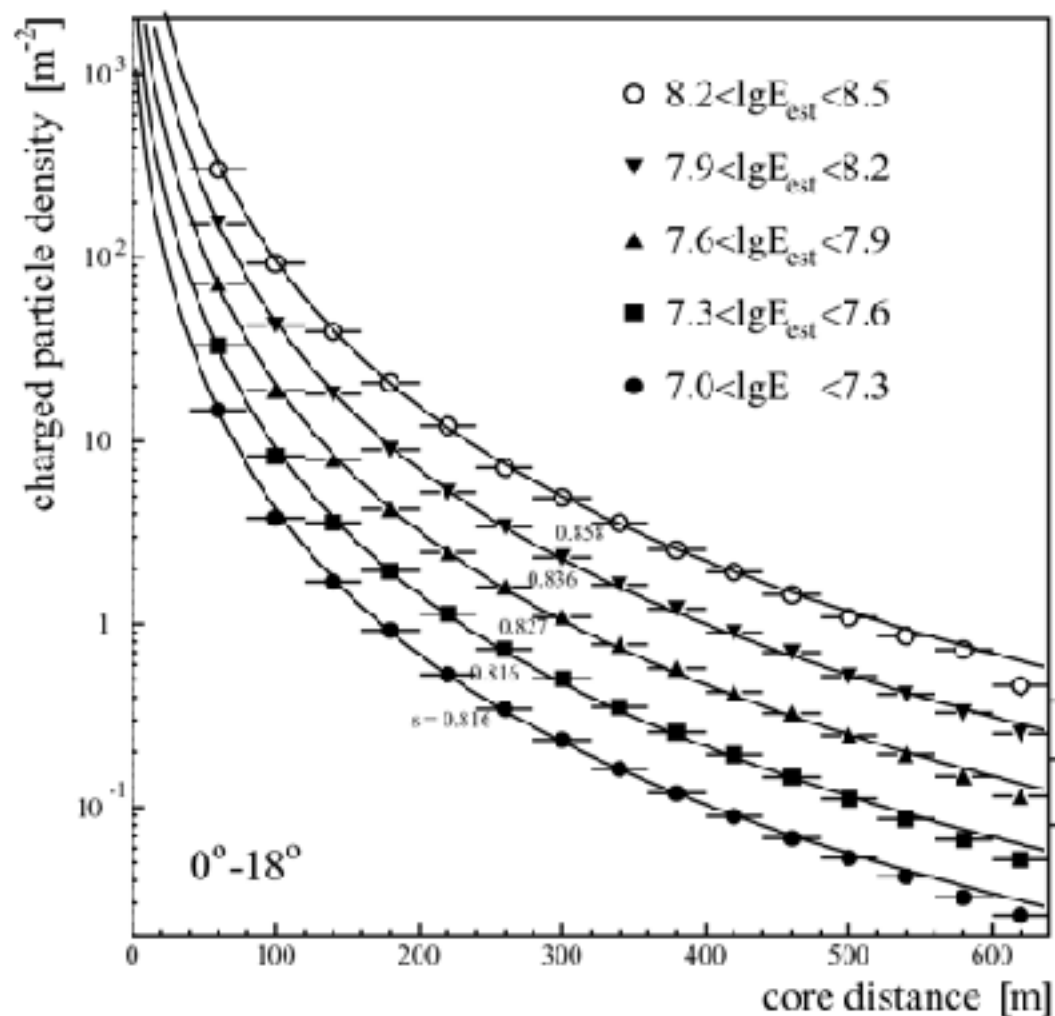
KASCADE-Grande – Lateral distributions

Electromagnetic component

Muons

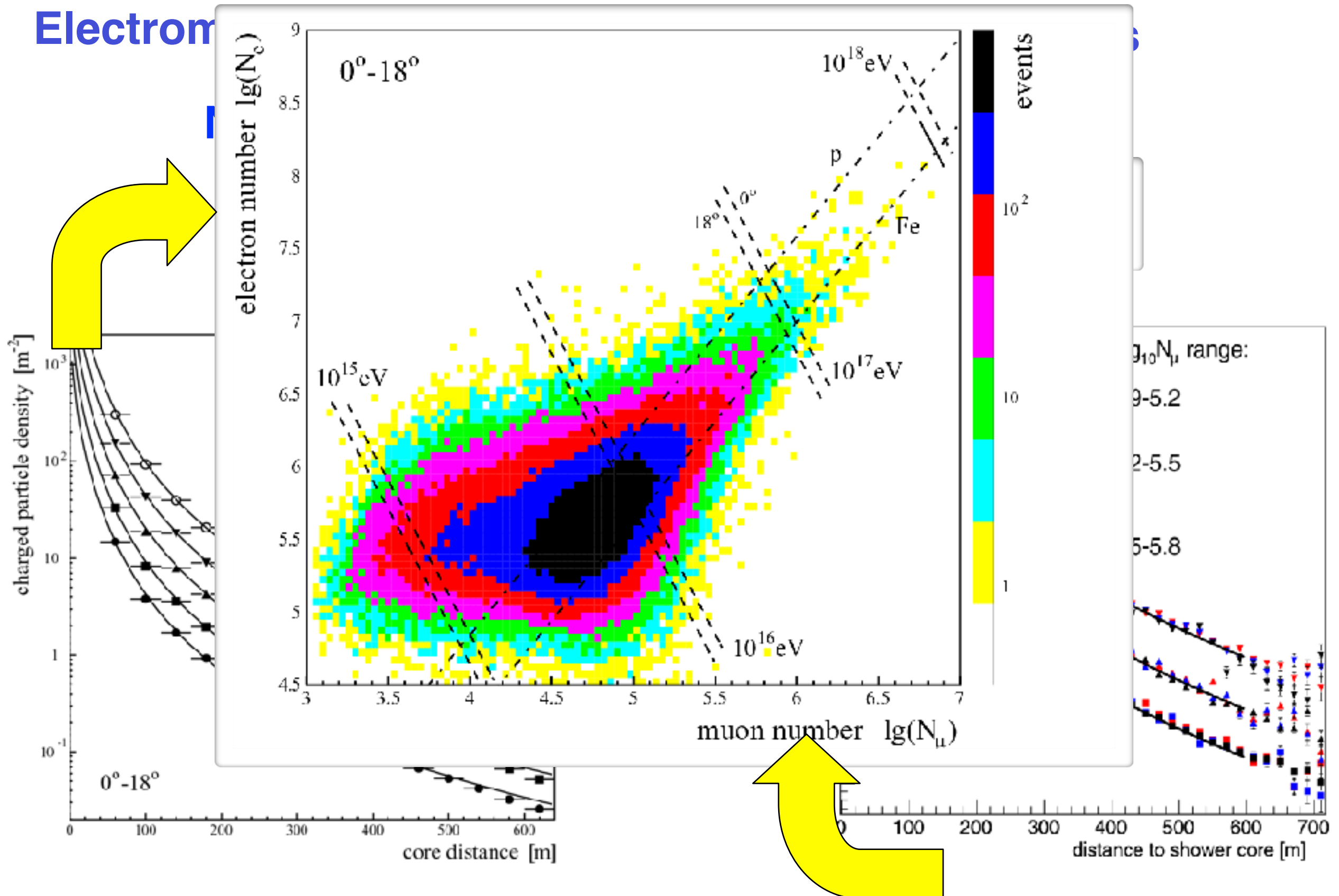
NKG function

$$\rho(r, s, N_e) = \frac{N_e}{r_M^2} \frac{\Gamma(4.5 - s)}{2\pi\Gamma(s)\Gamma(4.5 - 2s)} \left(\frac{r}{r_M}\right)^{s-2} \left(1 + \frac{r}{r_M}\right)^{s-4.5}$$

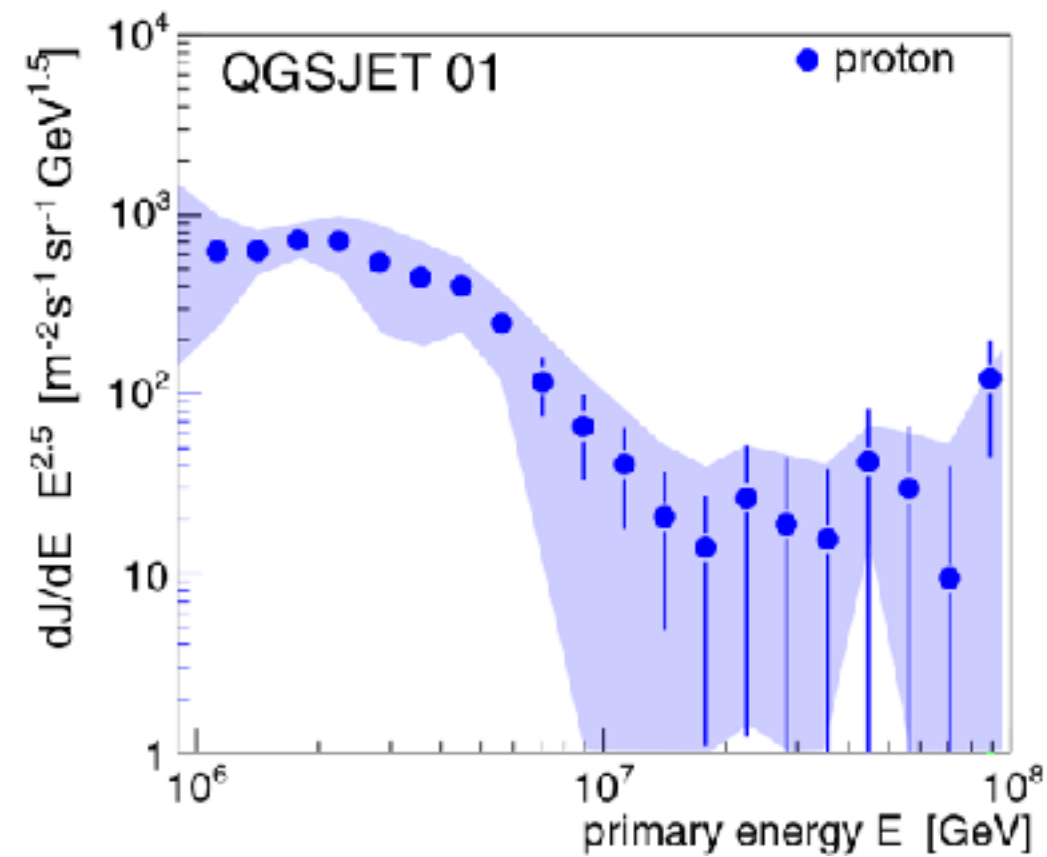


KASCADE-Grande – Lateral distributions

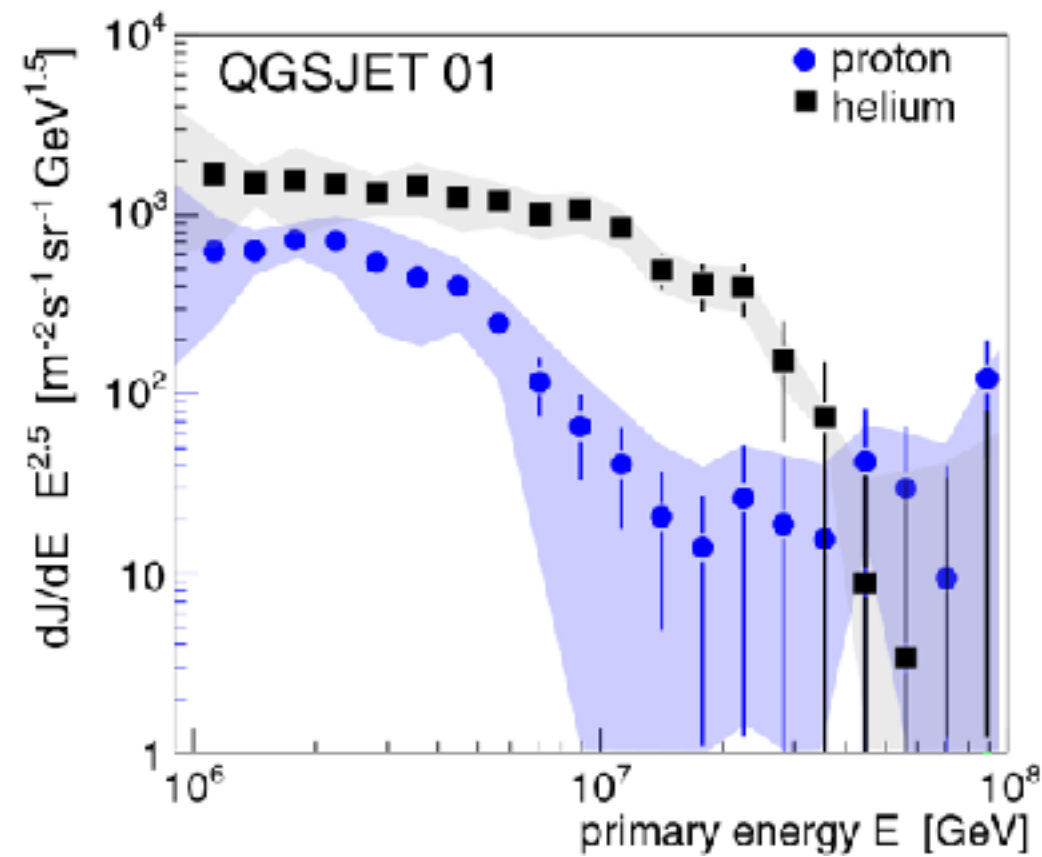
Electromagnetic



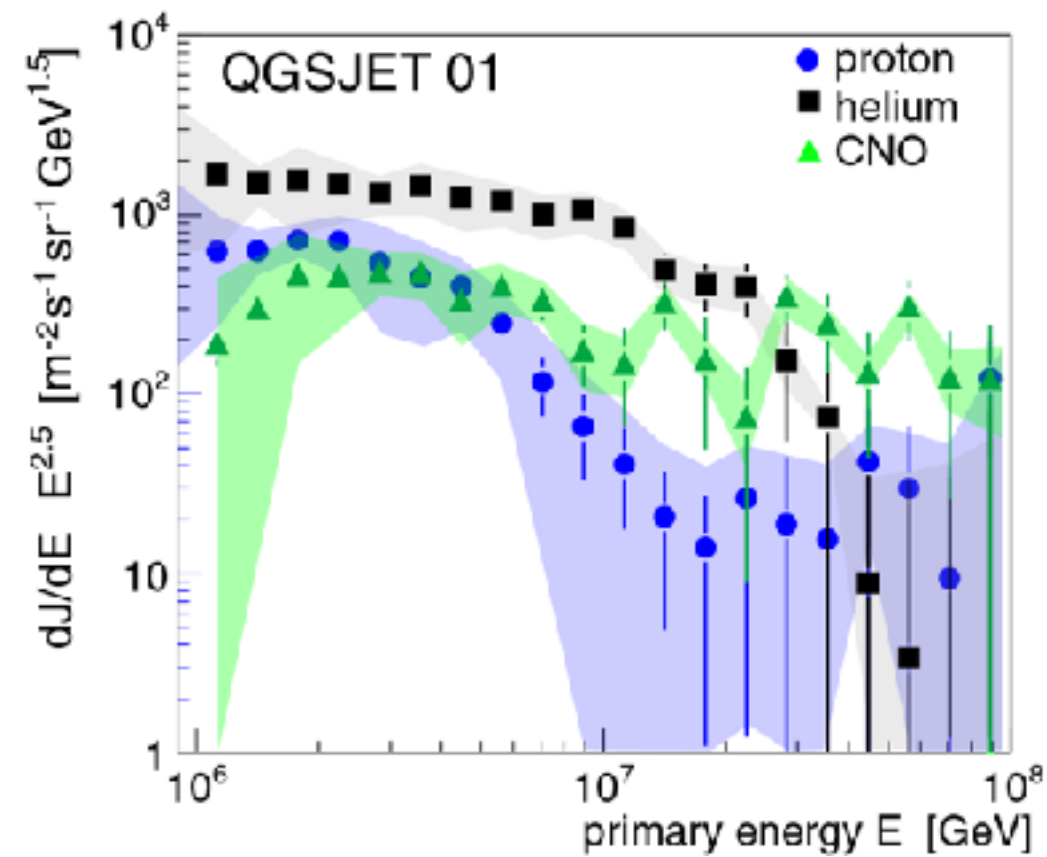
KASCADE: Energy spectra for elemental groups



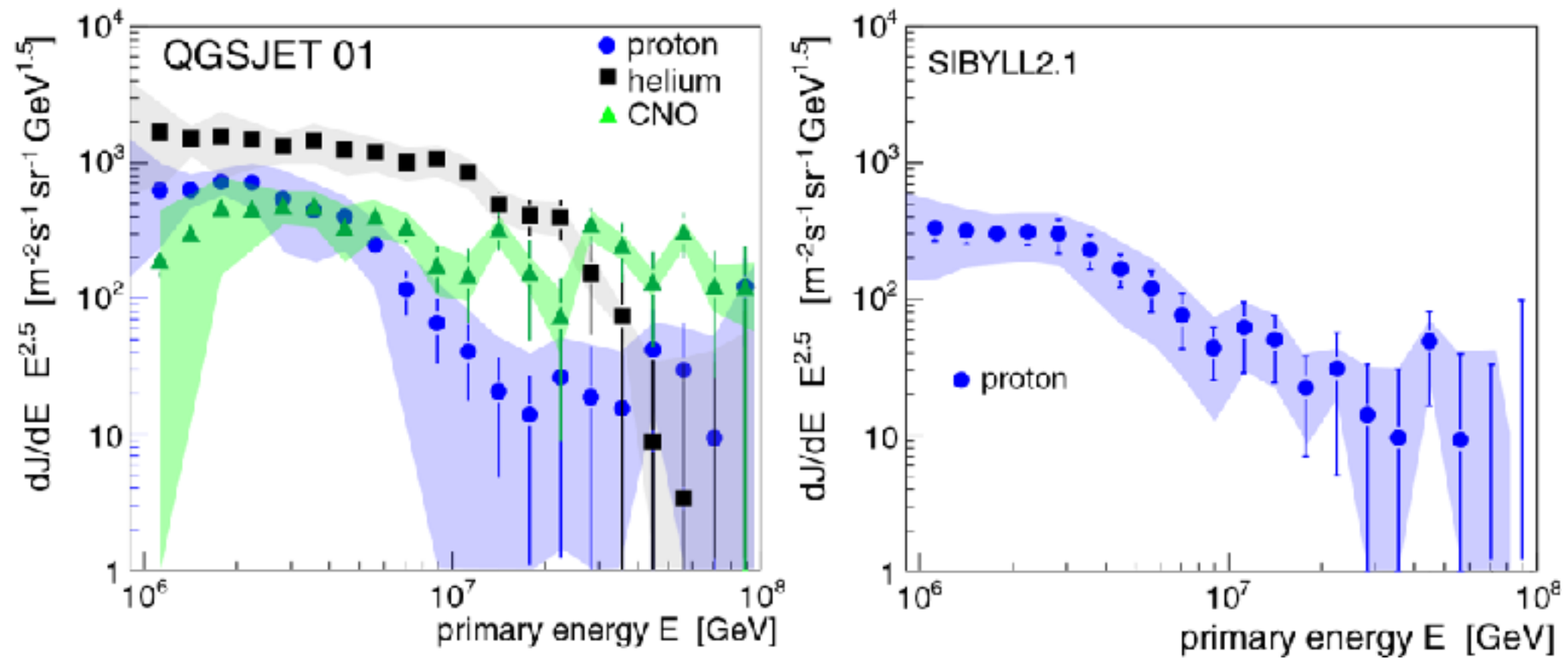
KASCADE: Energy spectra for elemental groups



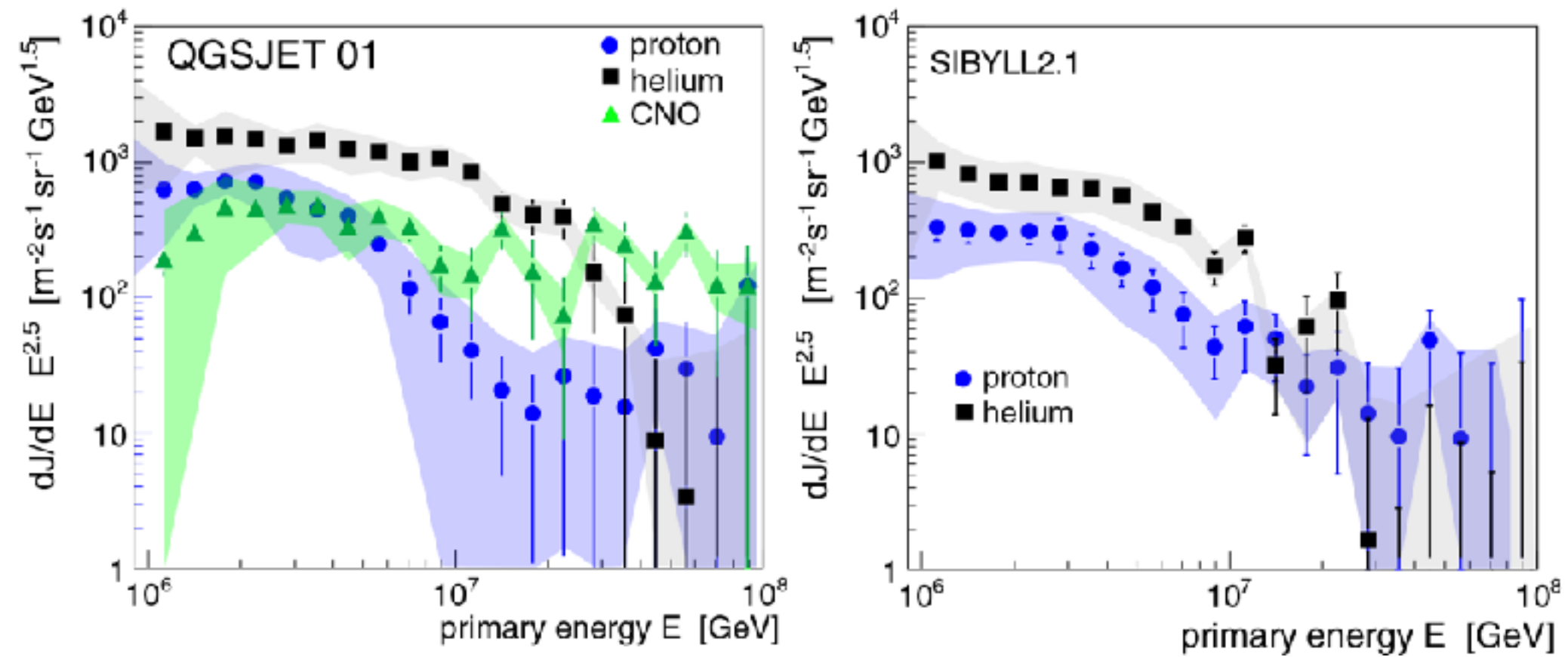
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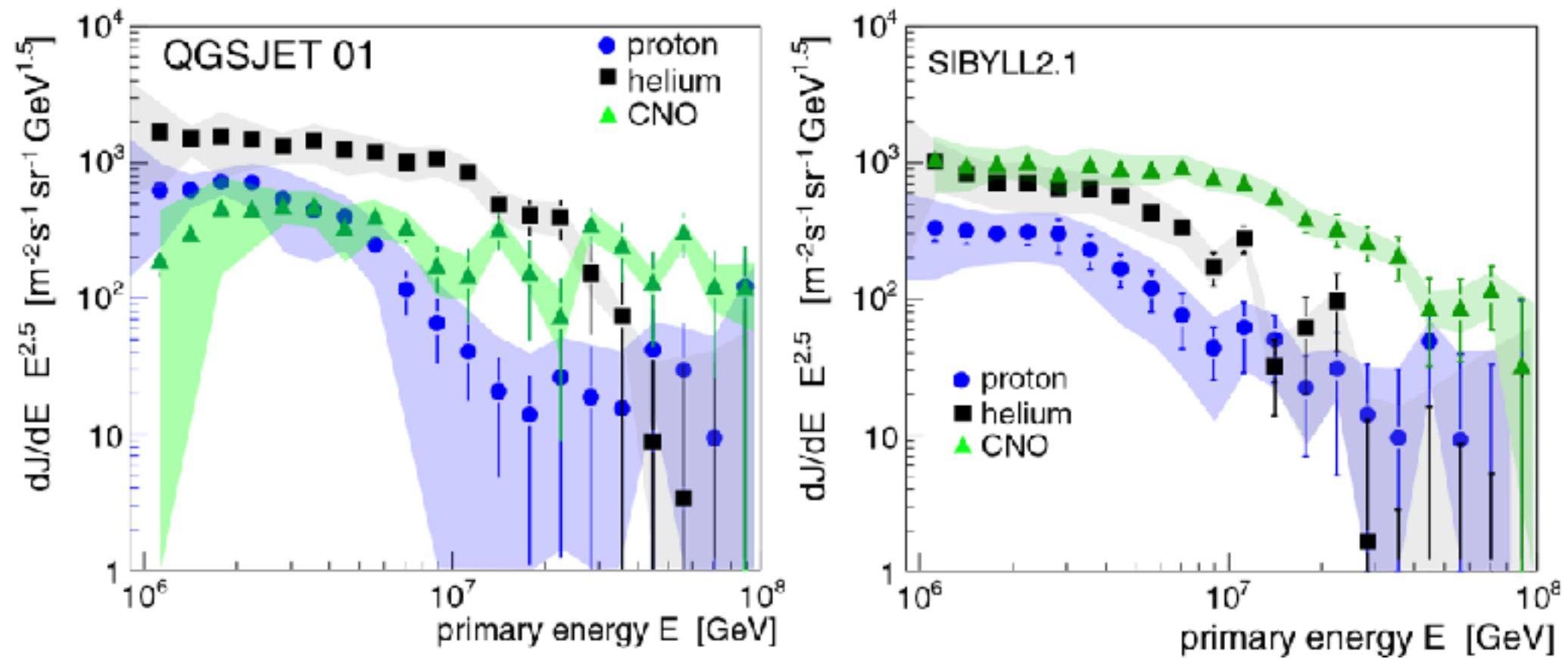
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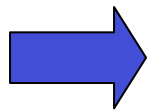
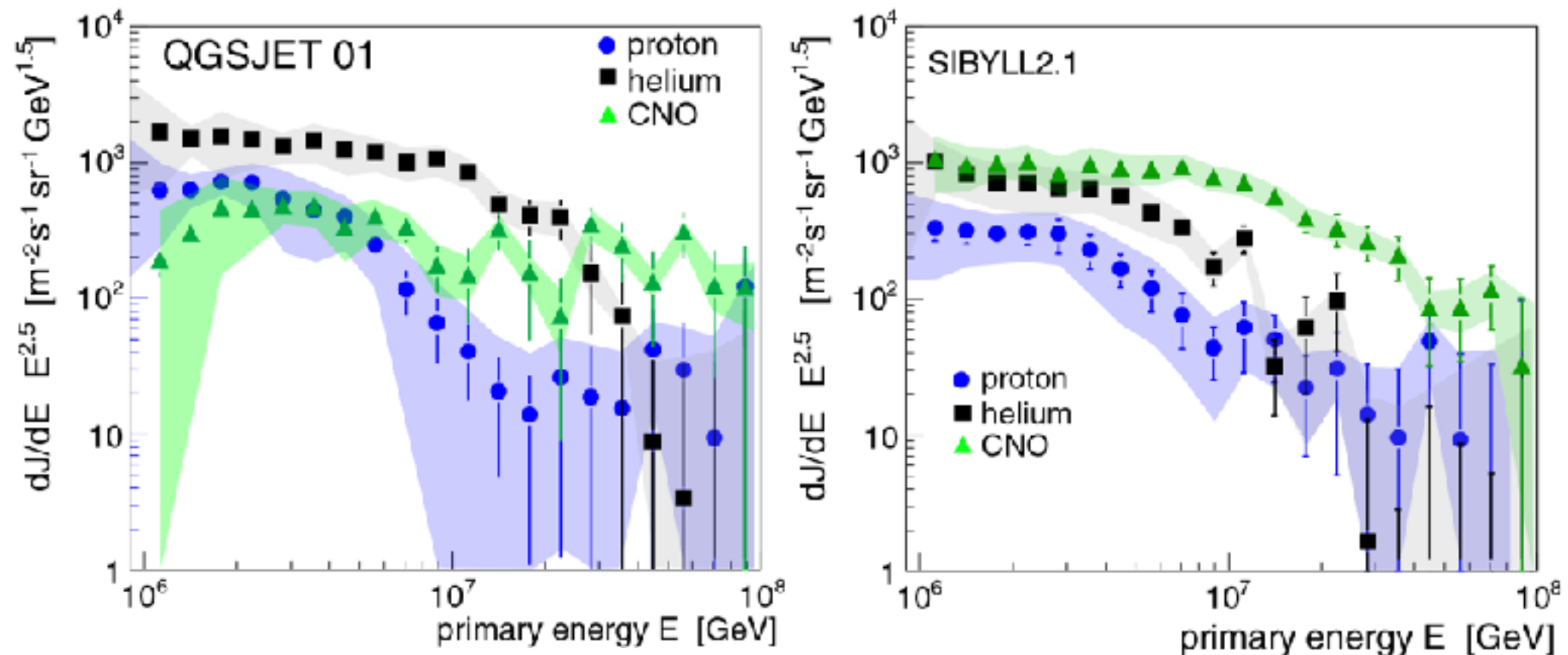
KASCADE: Energy spectra for elemental groups



KASCADE: Energy spectra for elemental groups



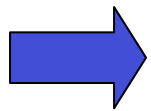
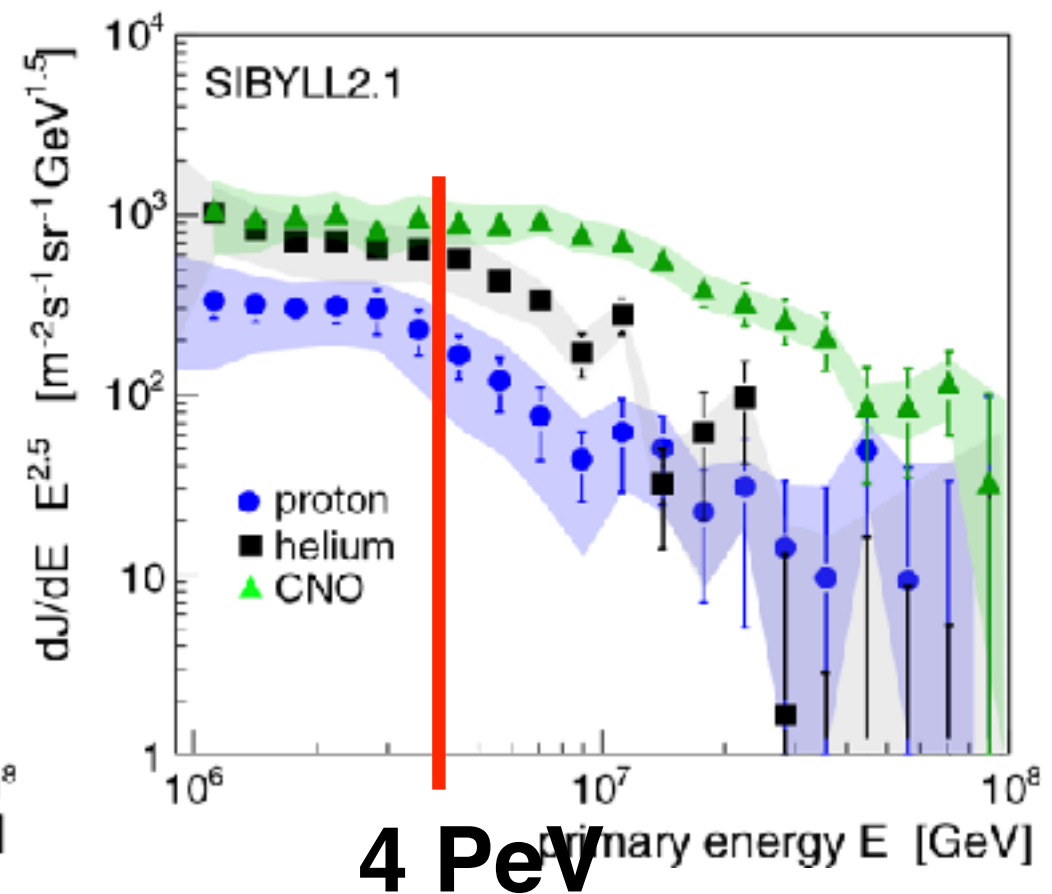
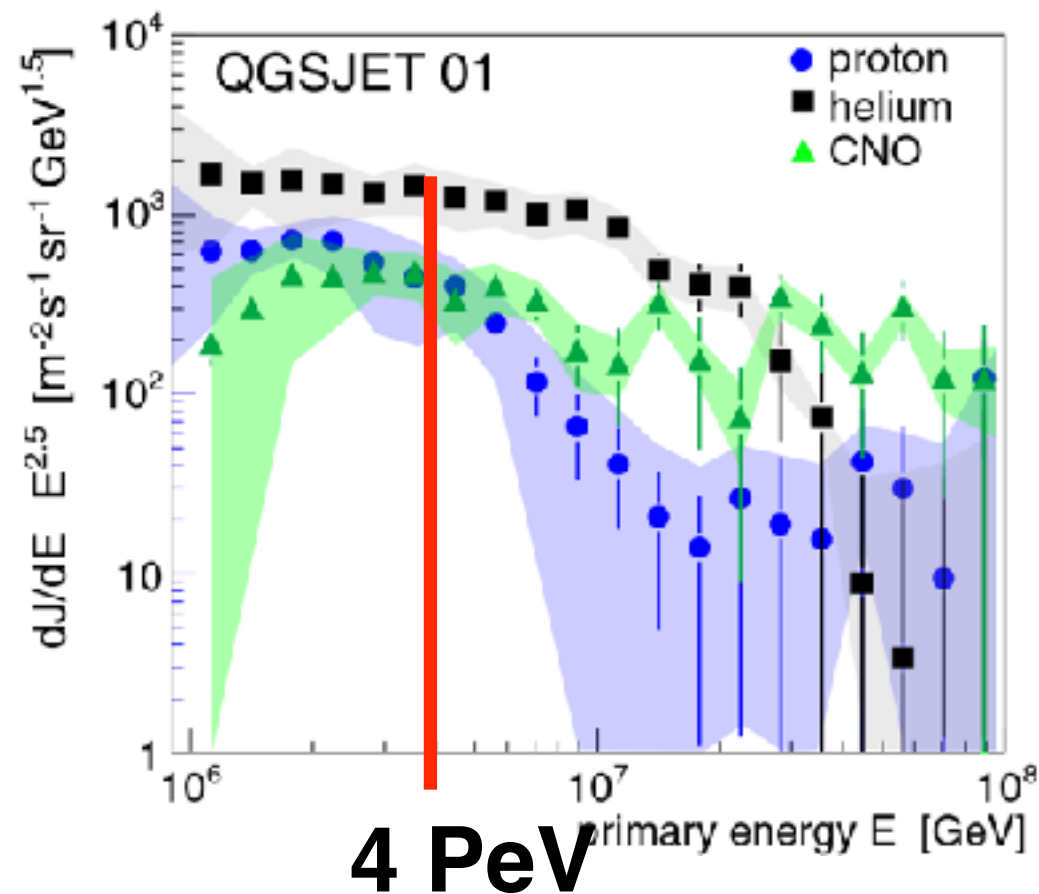
KASCADE: Energy spectra for elemental groups



Knee caused by cut-off for light elements

**Astrophysical interpretation
limited by description of
interactions in the atmosphere**

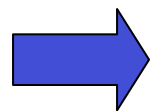
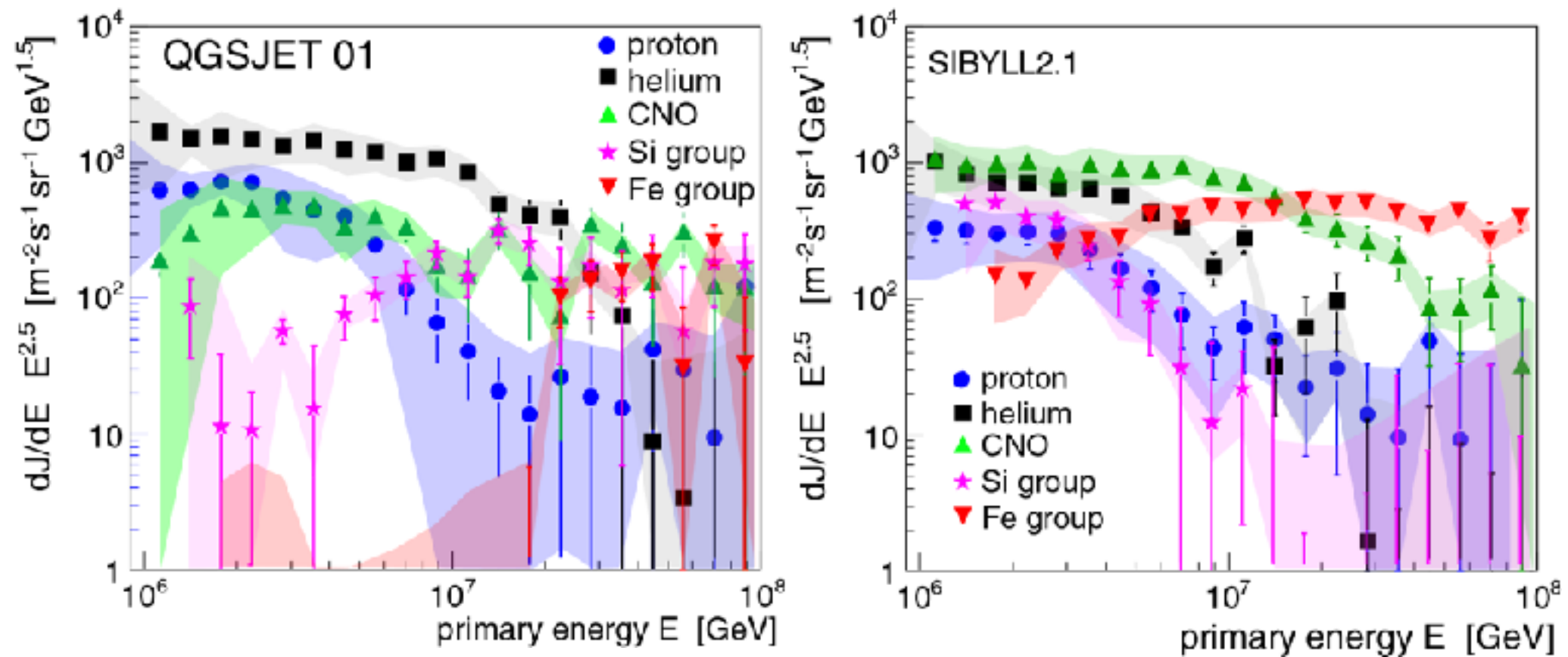
KASCADE: Energy spectra for elemental groups



Knee caused by cut-off for light elements

**Astrophysical interpretation
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KASCADE: Energy spectra for elemental groups



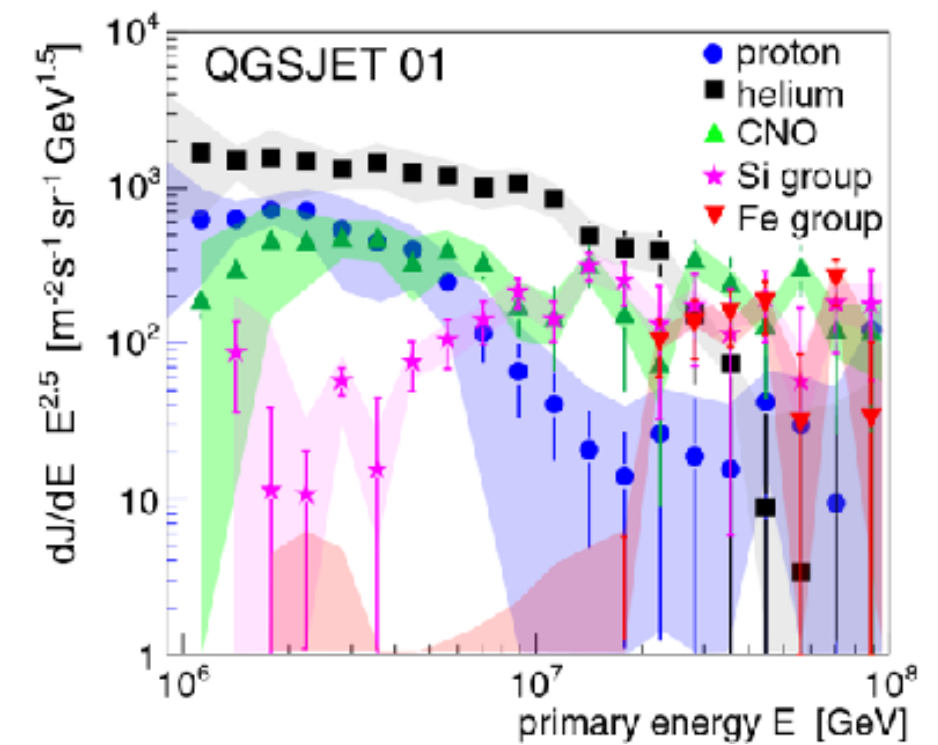
Knee caused by cut-off for light elements

**Astrophysical interpretation
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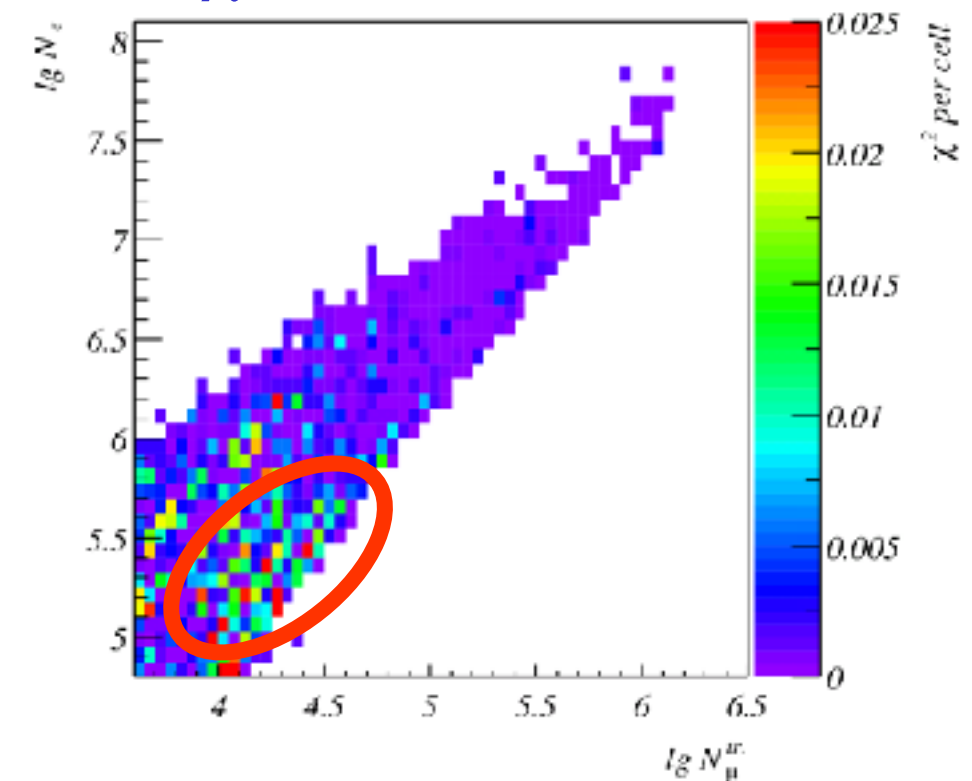
Test of hadronic interaction models

QGSJET 01

N_e - N_μ analysis



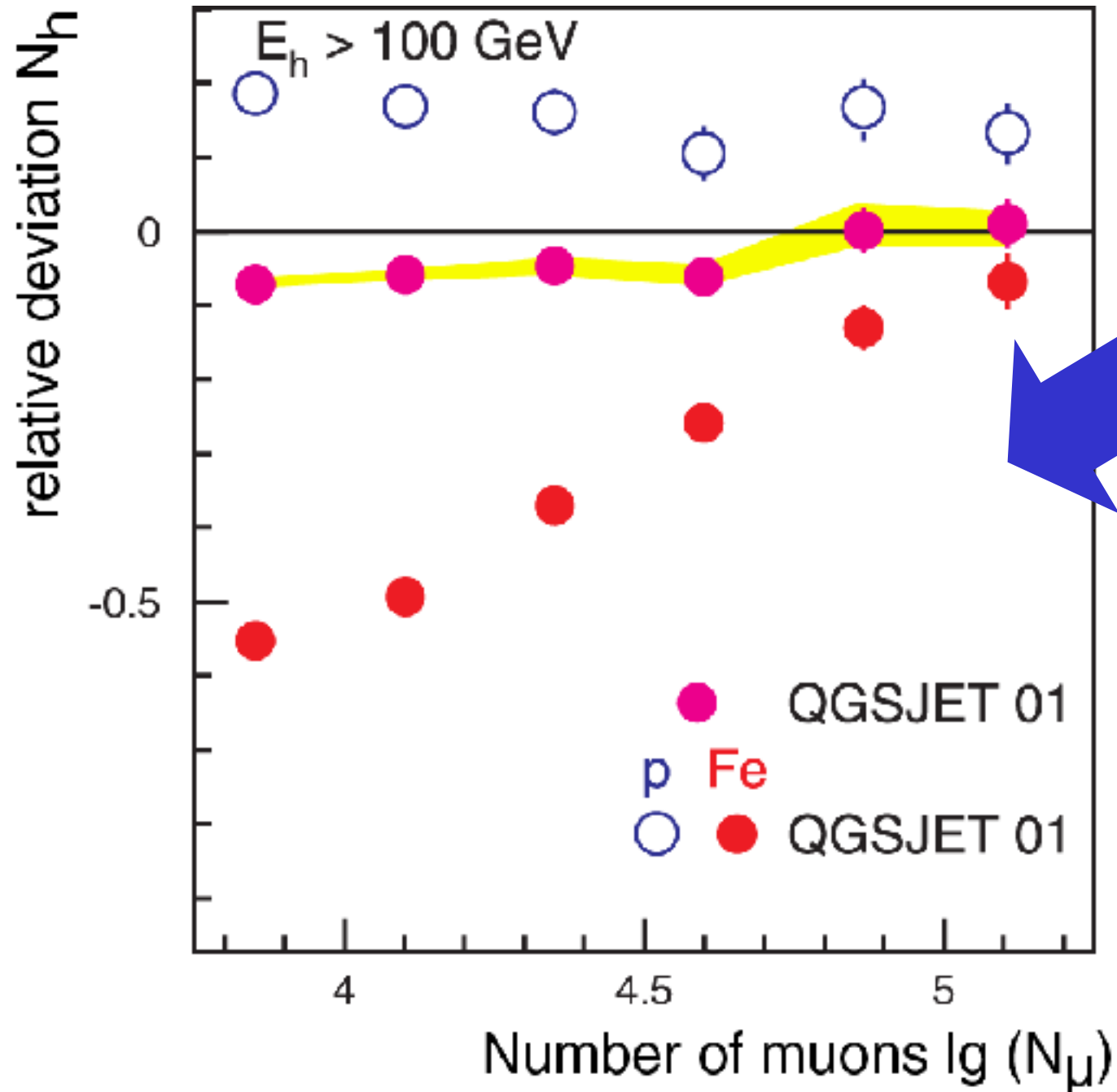
χ^2 distribution



Test of hadronic interaction models

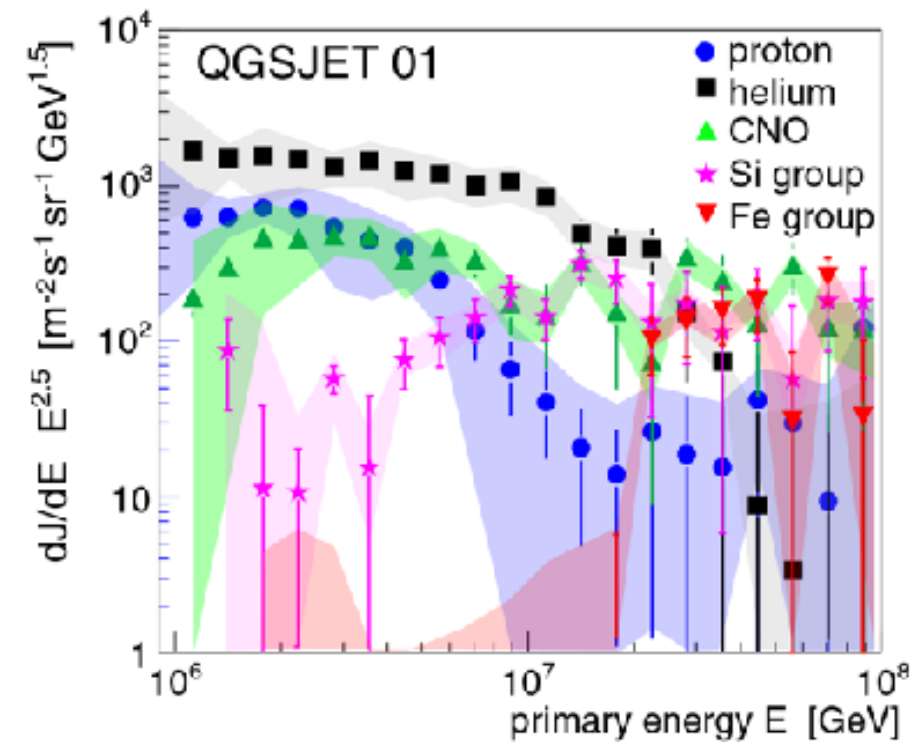
QGSJET 01

Number of hadrons vs. number of muons

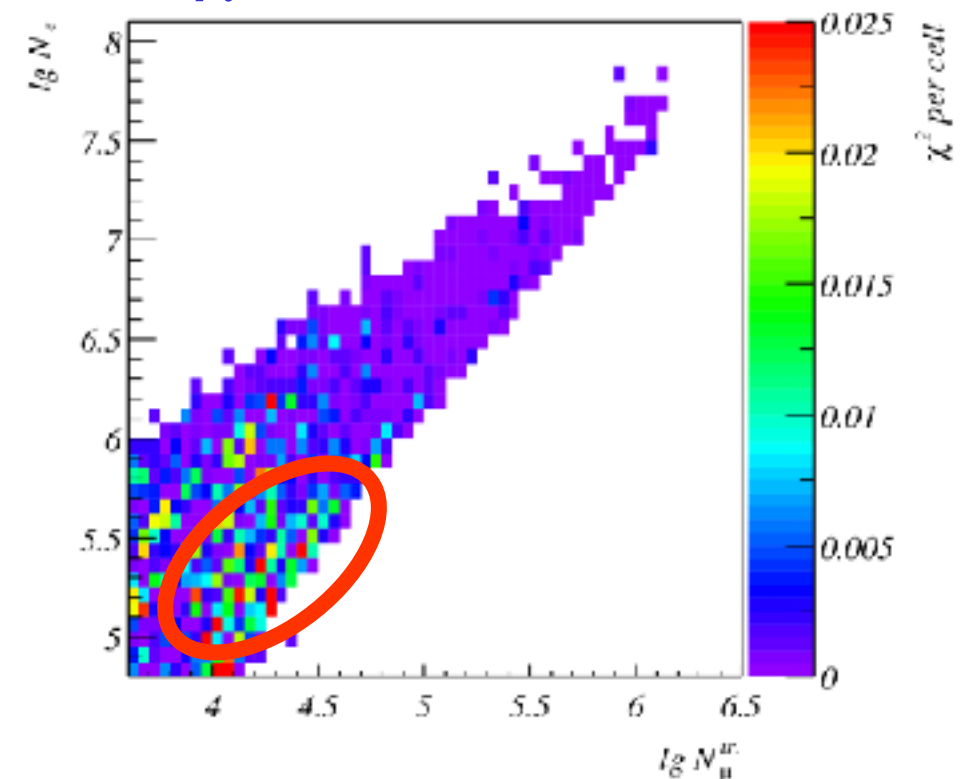


inconsistencies on 10% level

N_e - N_μ analysis



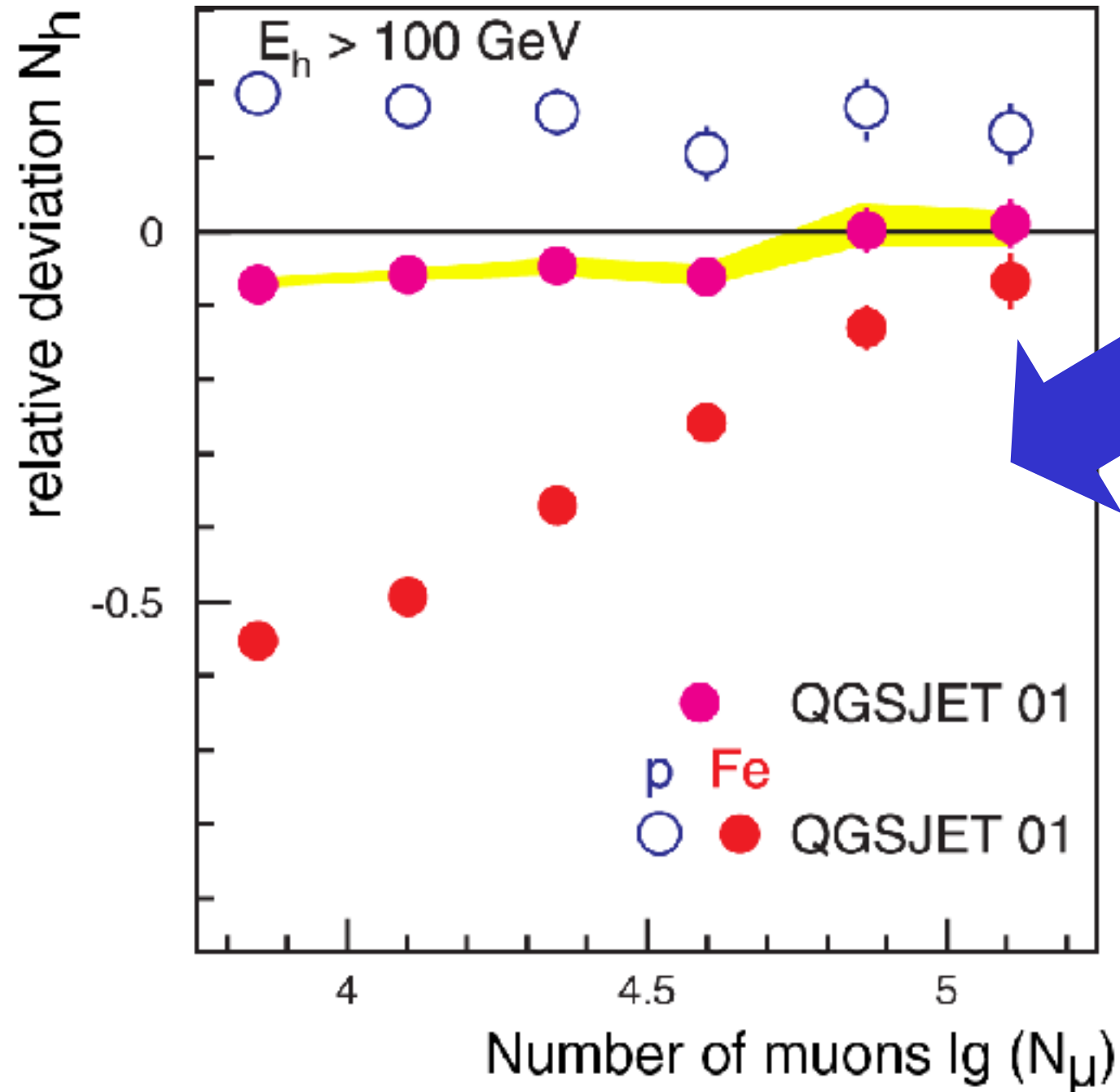
χ^2 distribution



Test of hadronic interaction models

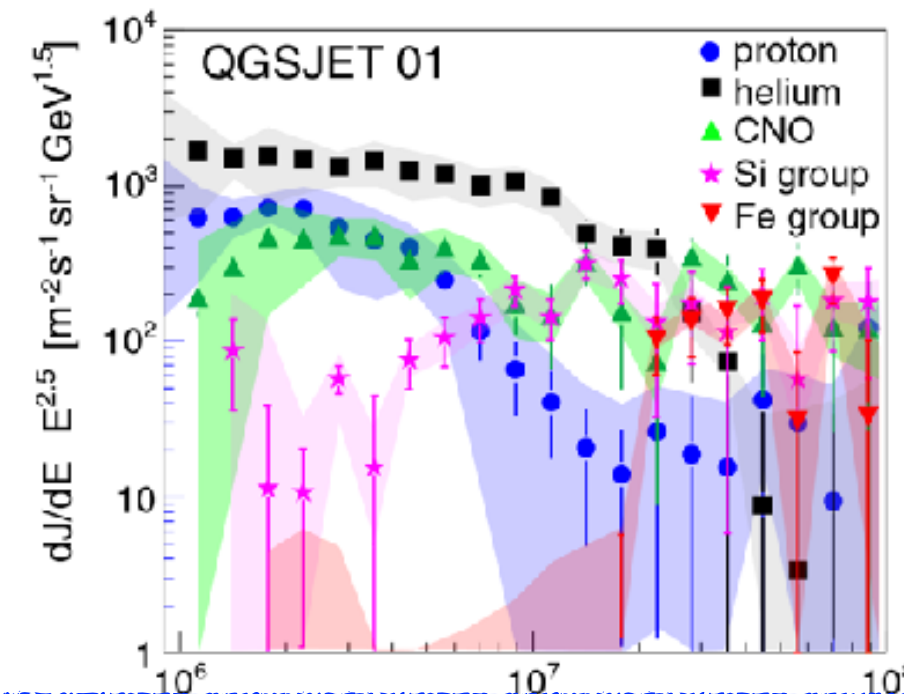
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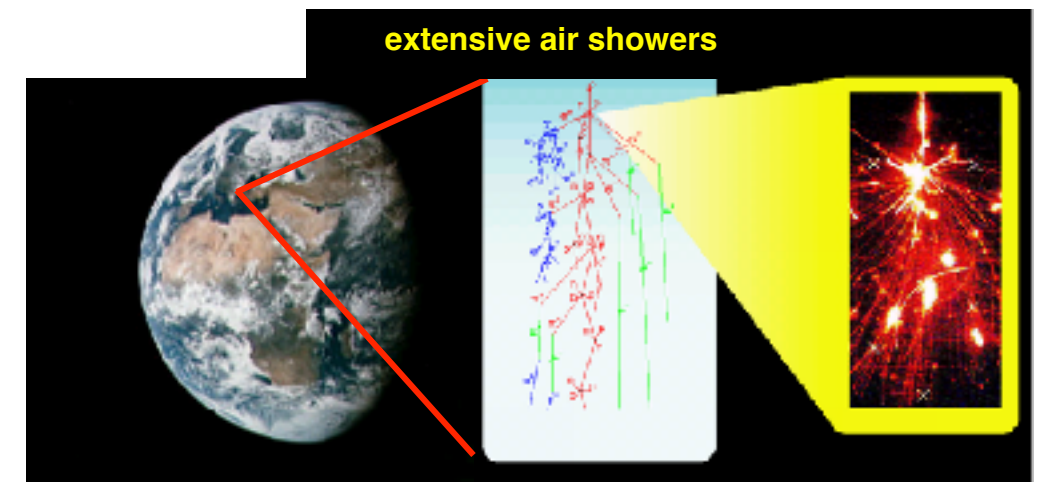
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in literature:

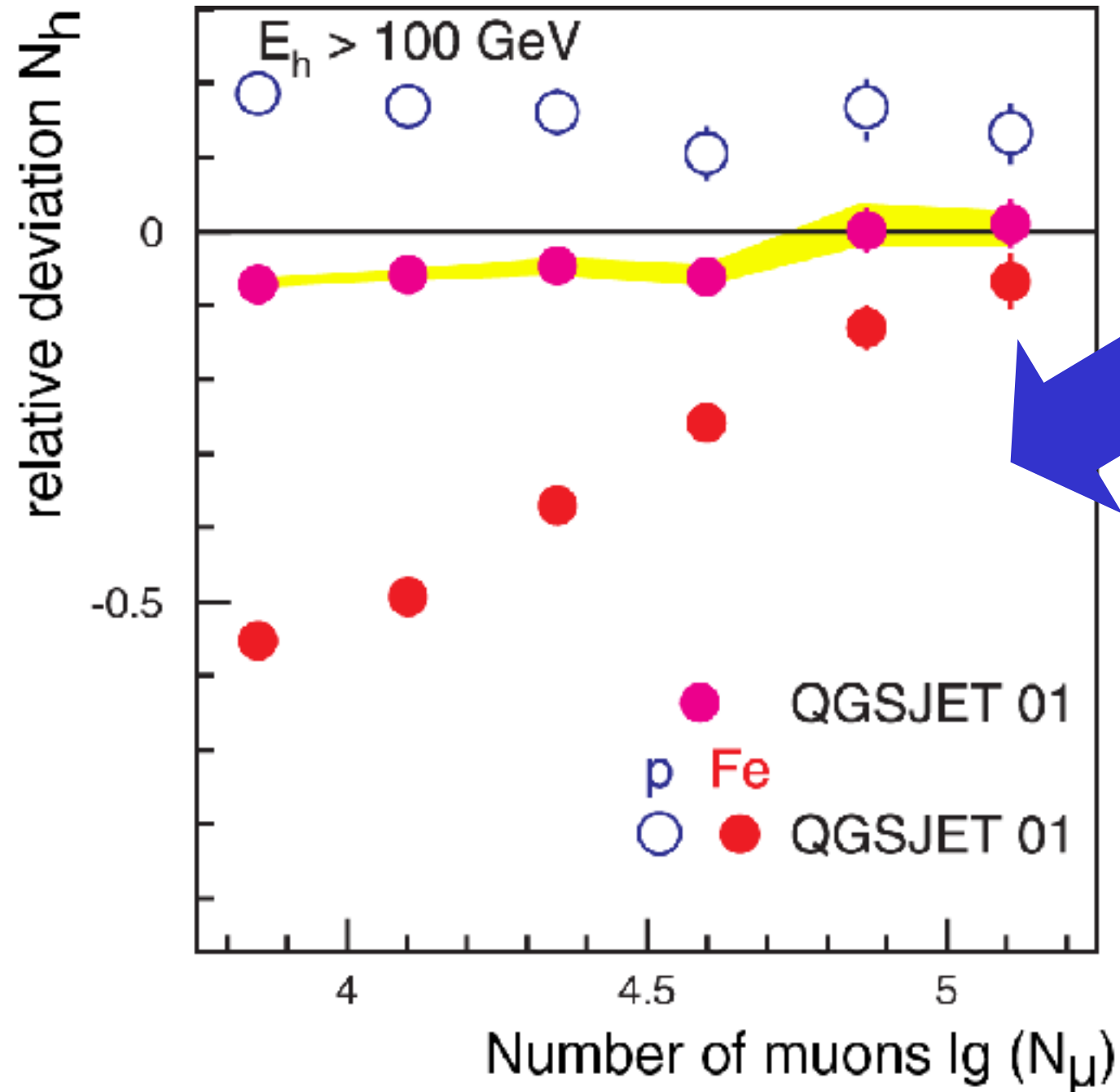
ideas that knee is caused by new interactions in atmosphere
—> energy is carried away by „invisible channels“



Test of hadronic interaction models

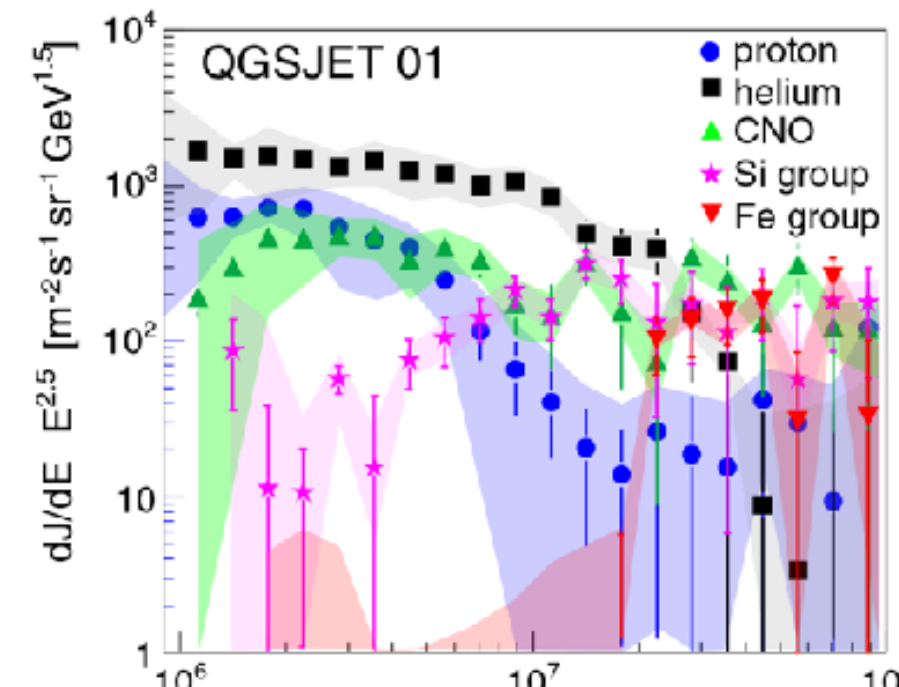
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Number of hadrons vs. number of muons



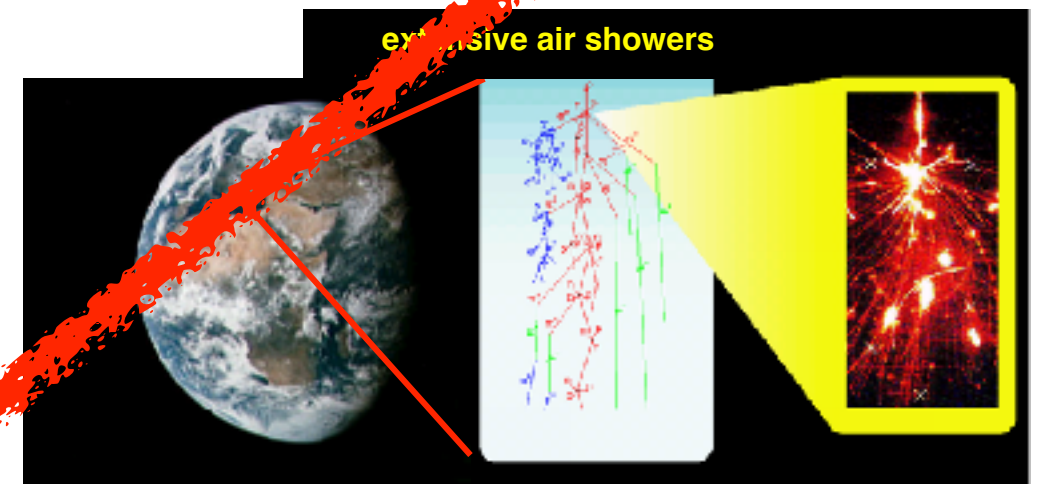
inconsistencies on 10% level

N_e - N_μ analysis



in literature:

ideas that knee is caused by new interactions in atmosphere
—> energy is carried away by „invisible channels“



Electron, muon and hadron size spectra of EAS in the "knee" region

R. Glasstetter^a and J.R. Hörandel^a for the KASCADE Collaboration*

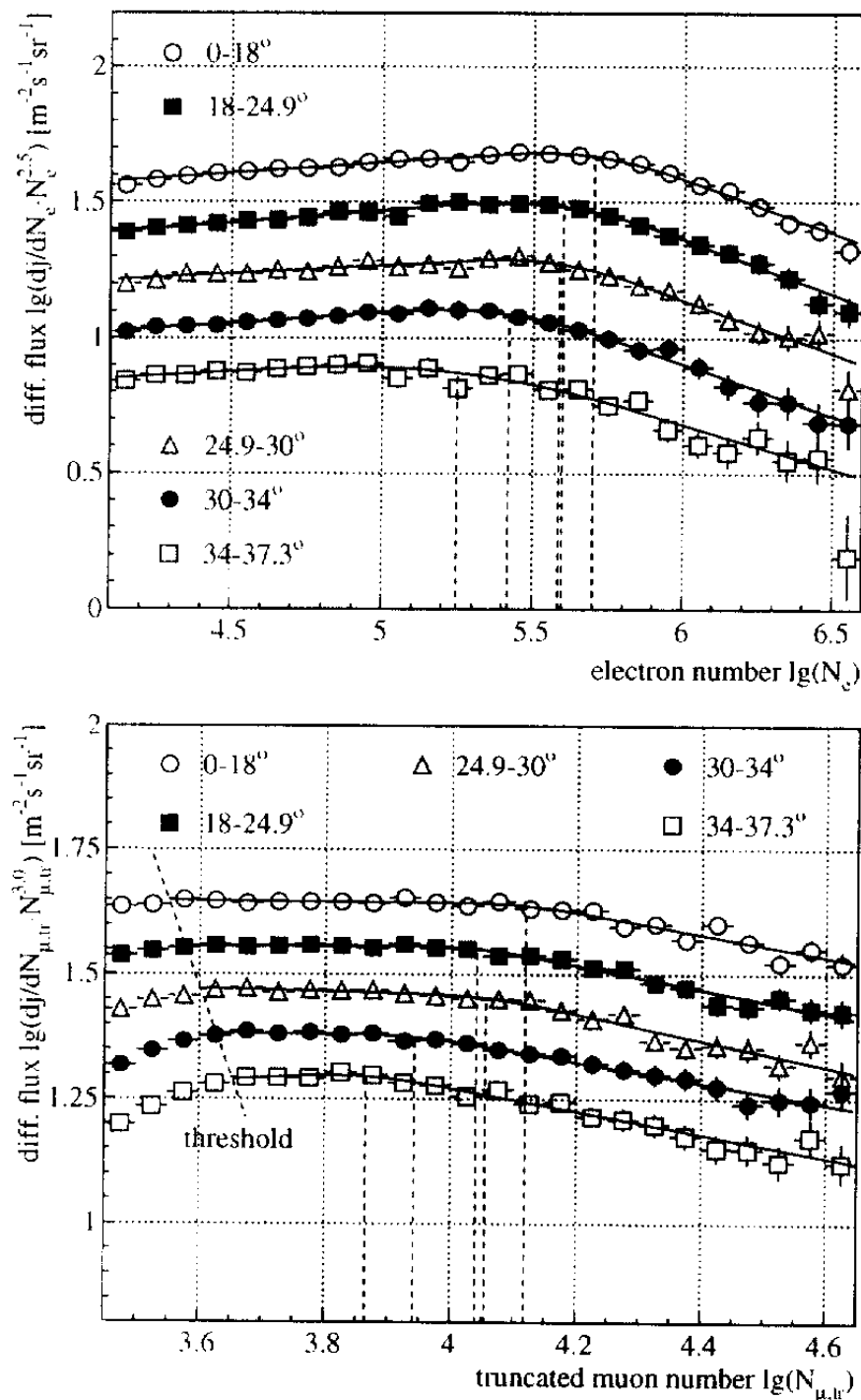


Figure 1. Electromagnetic (top) and muonic (bottom) shower size spectra for different zenith angle bins.

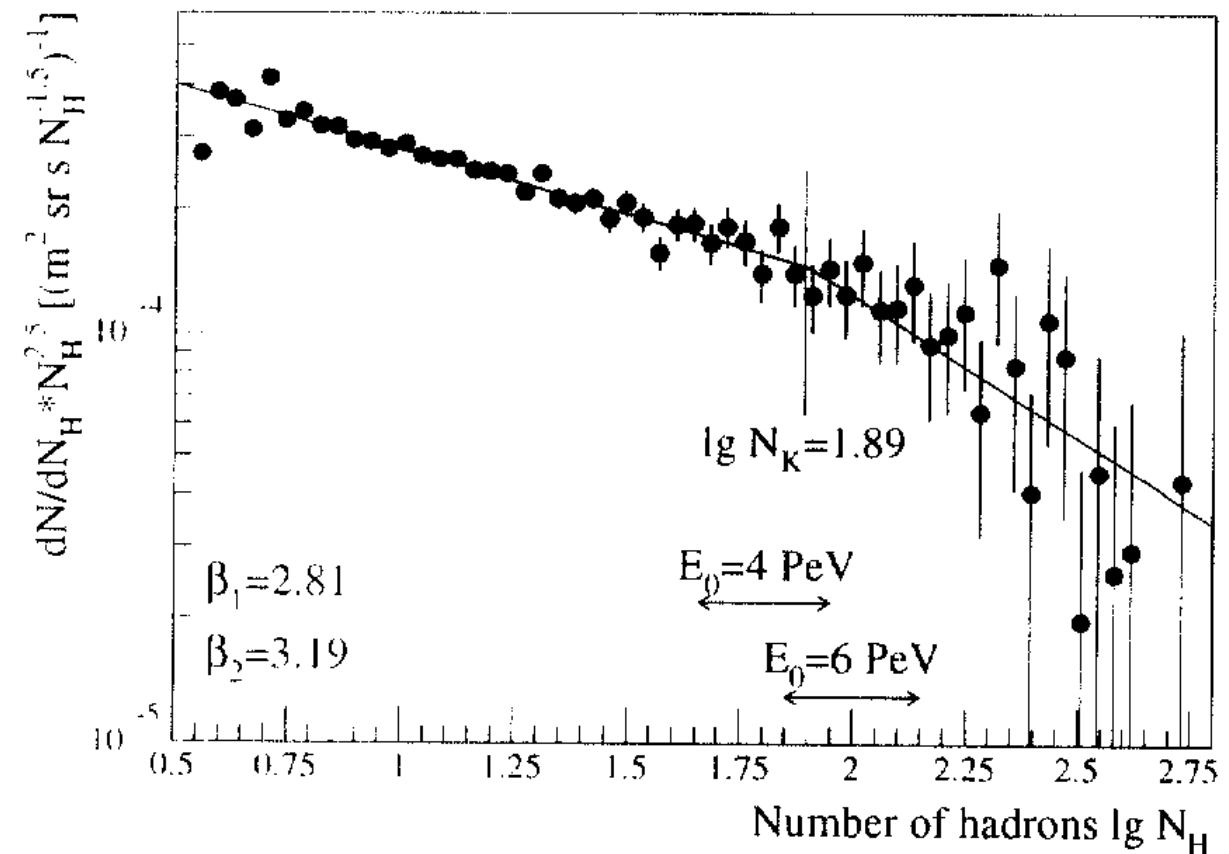


Figure 3. Hadronic shower size spectrum.

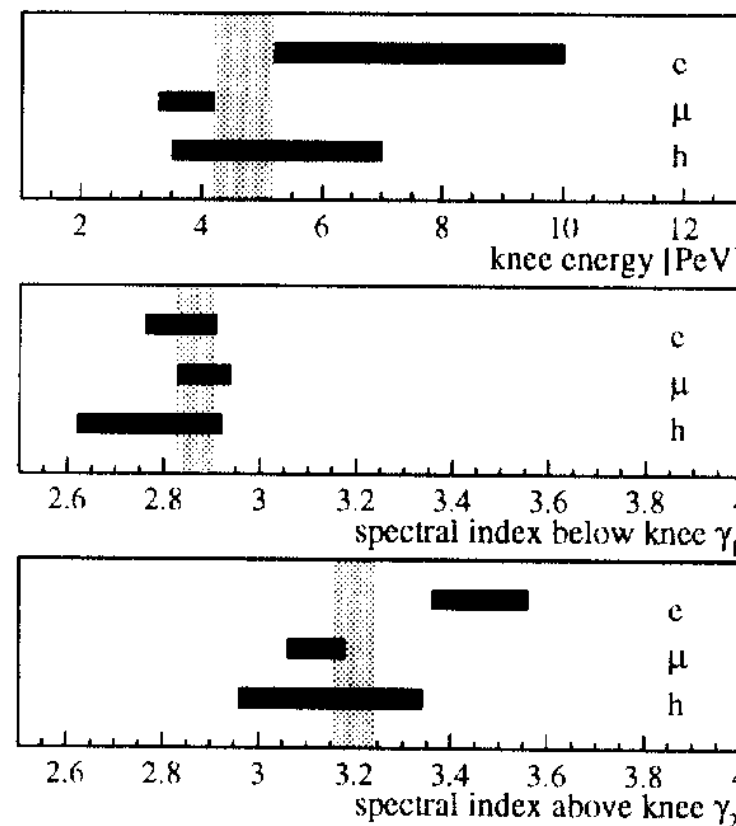
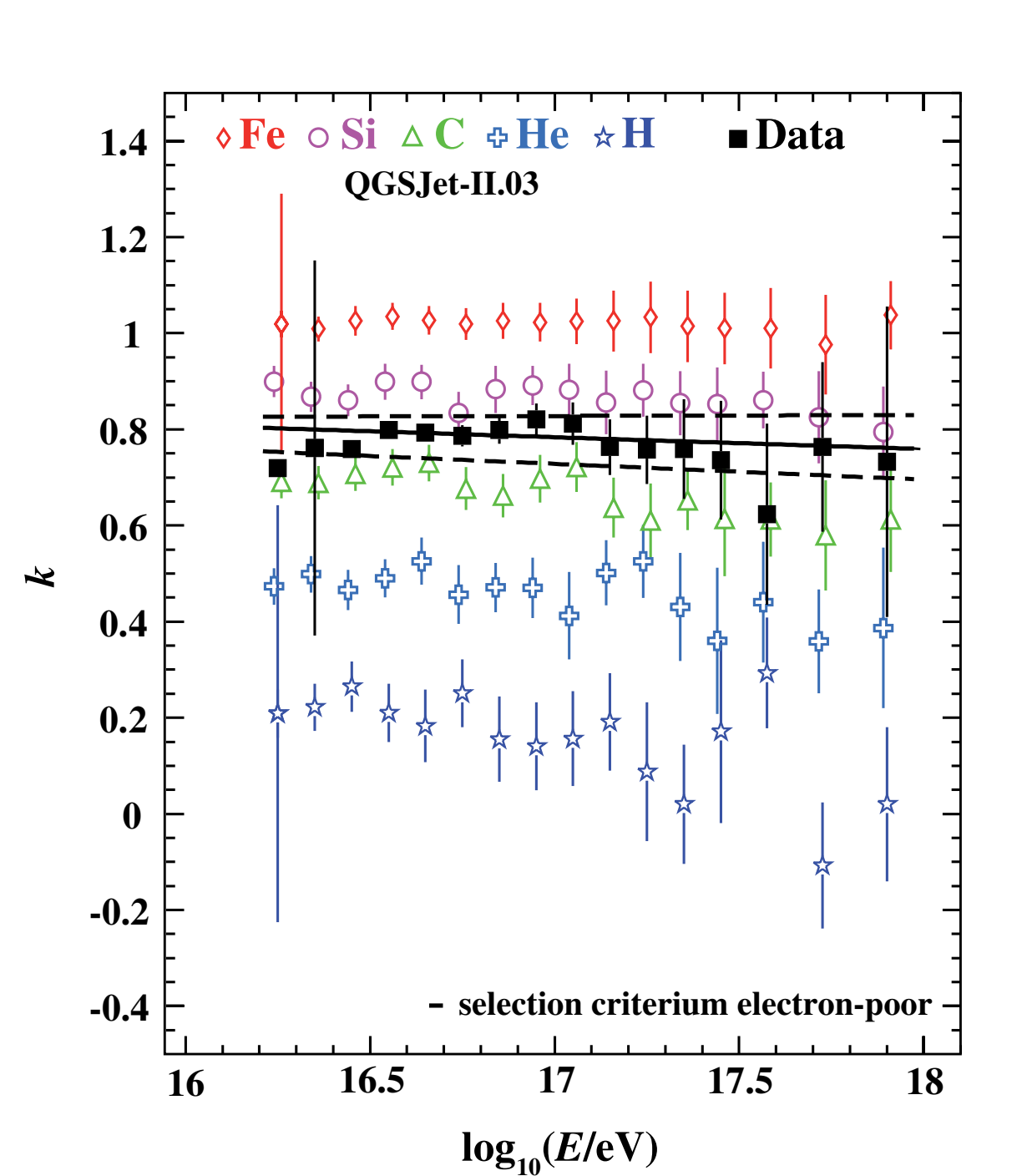


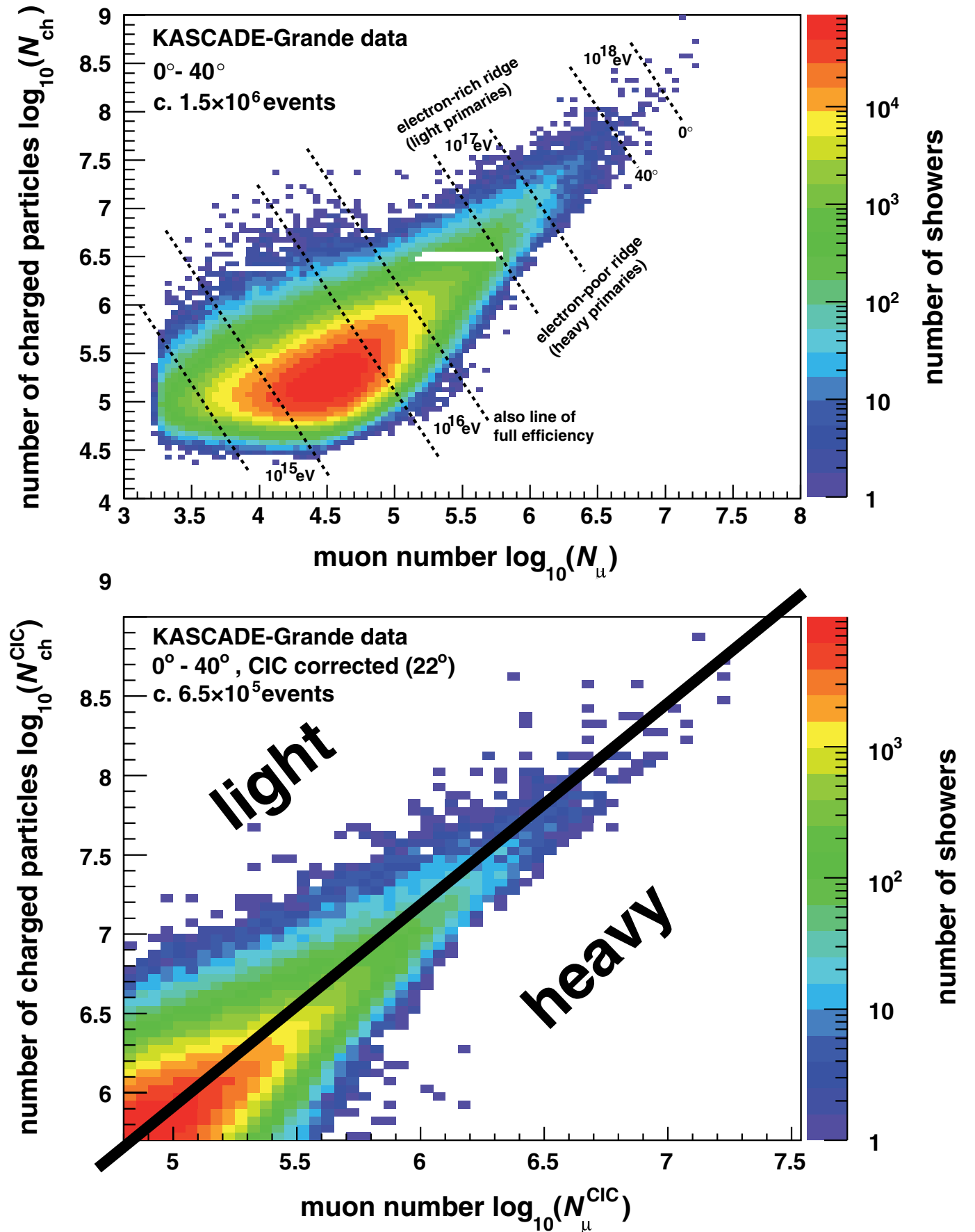
Figure 4. Knee position and spectral indices.

*knee observed in
all components,
electromagnetic,
muonic, and
hadronic!*

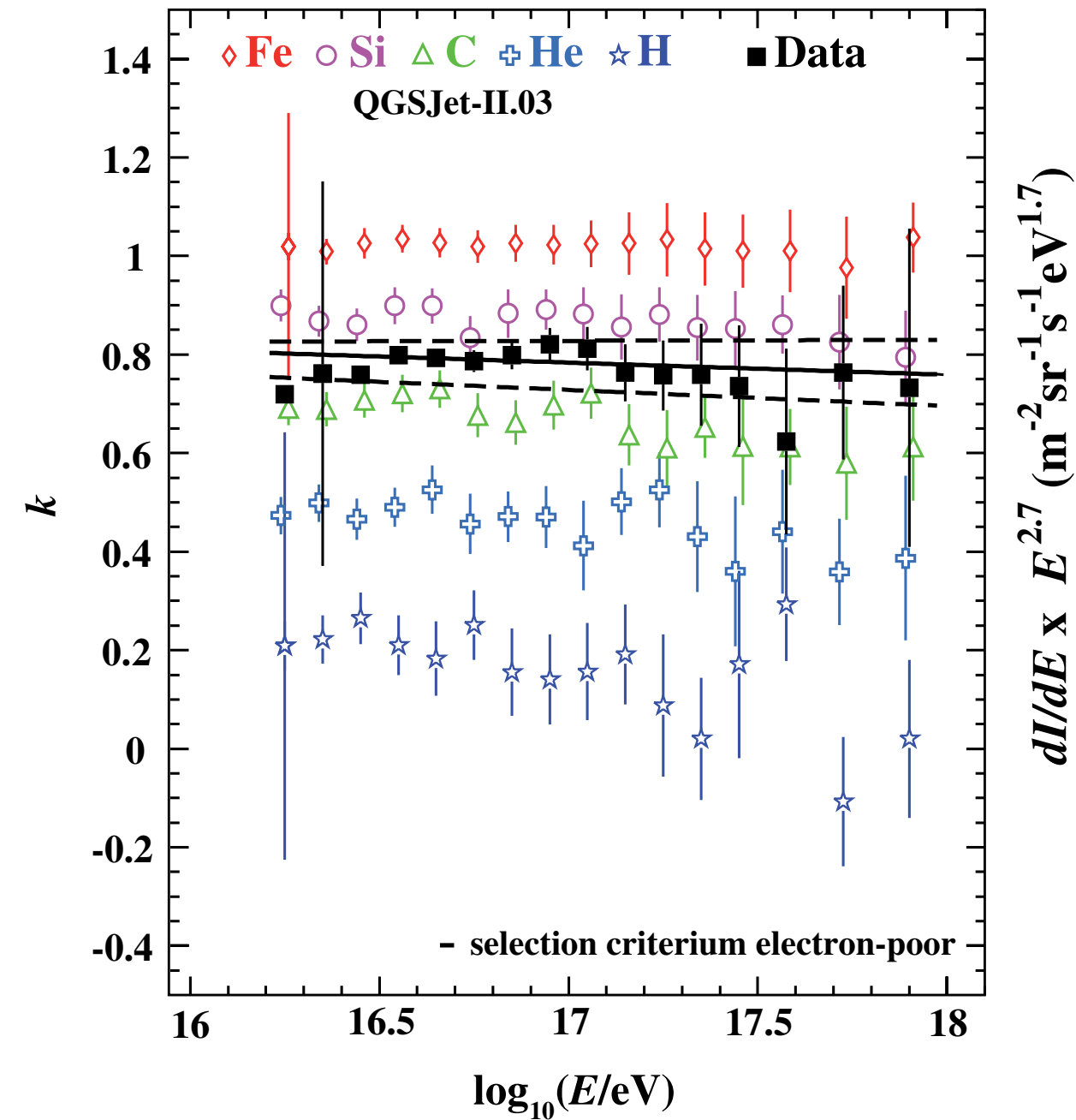
KASCADE-Grande



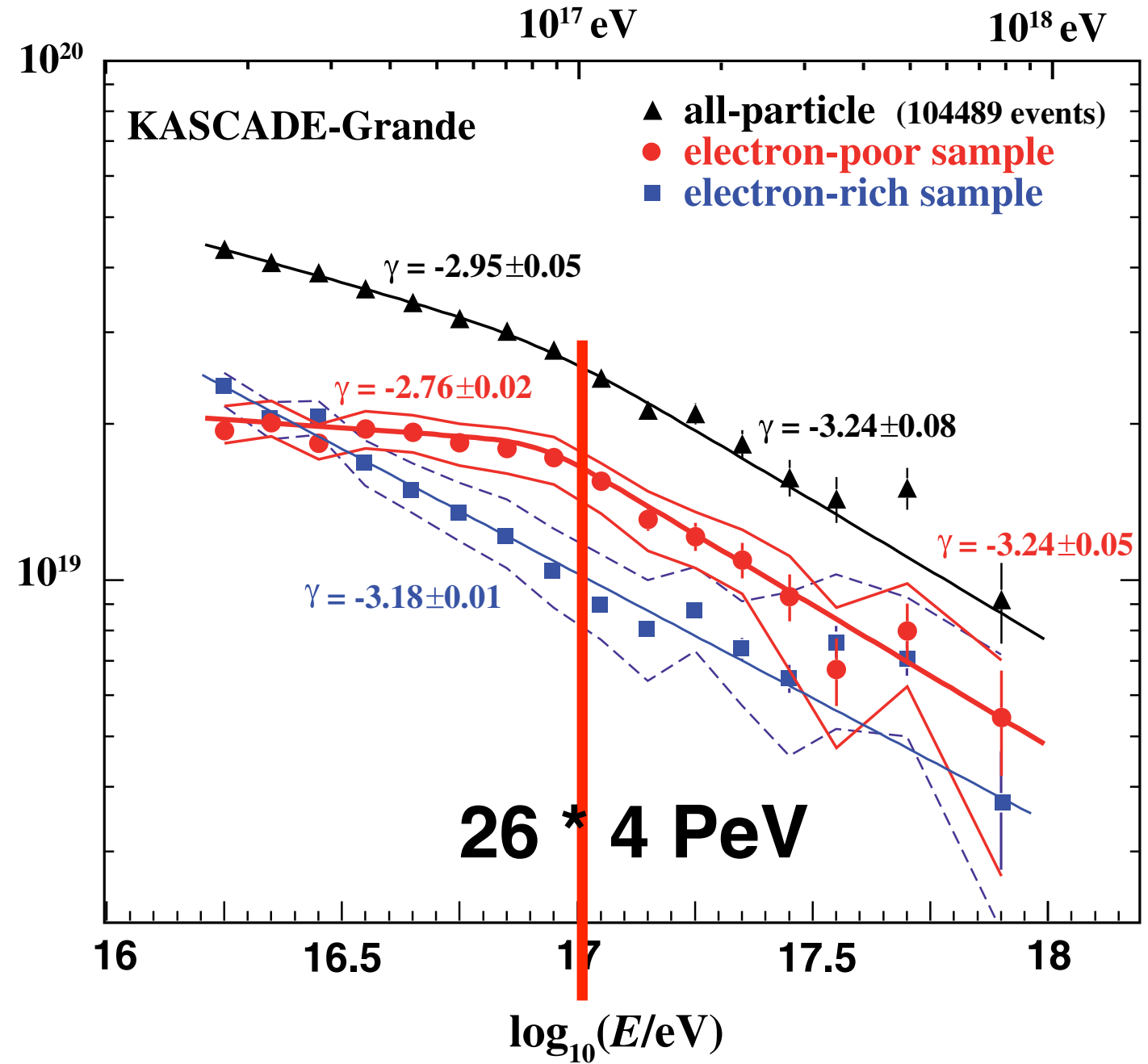
$$k = \frac{\log_{10}(N_{\text{ch}}/N_{\mu}) - \log_{10}(N_{\text{ch}}/N_{\mu})_{\text{H}}}{\log_{10}(N_{\text{ch}}/N_{\mu})_{\text{Fe}} - \log_{10}(N_{\text{ch}}/N_{\mu})_{\text{H}}},$$



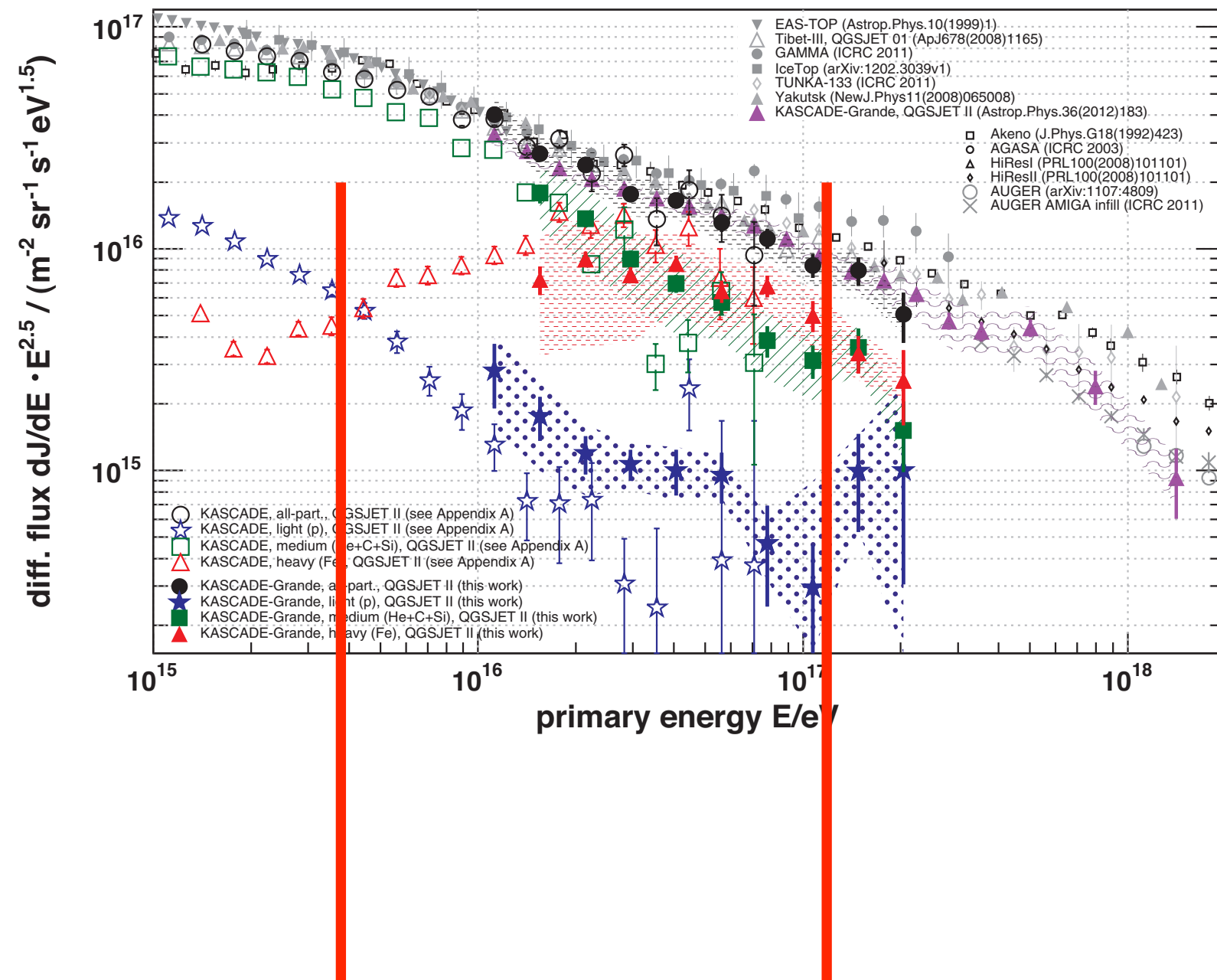
KASCADE-Grande



$$k = \frac{\log_{10}(N_{\text{ch}}/N_{\mu}) - \log_{10}(N_{\text{ch}}/N_{\mu})_{\text{H}}}{\log_{10}(N_{\text{ch}}/N_{\mu})_{\text{Fe}} - \log_{10}(N_{\text{ch}}/N_{\mu})_{\text{H}}},$$



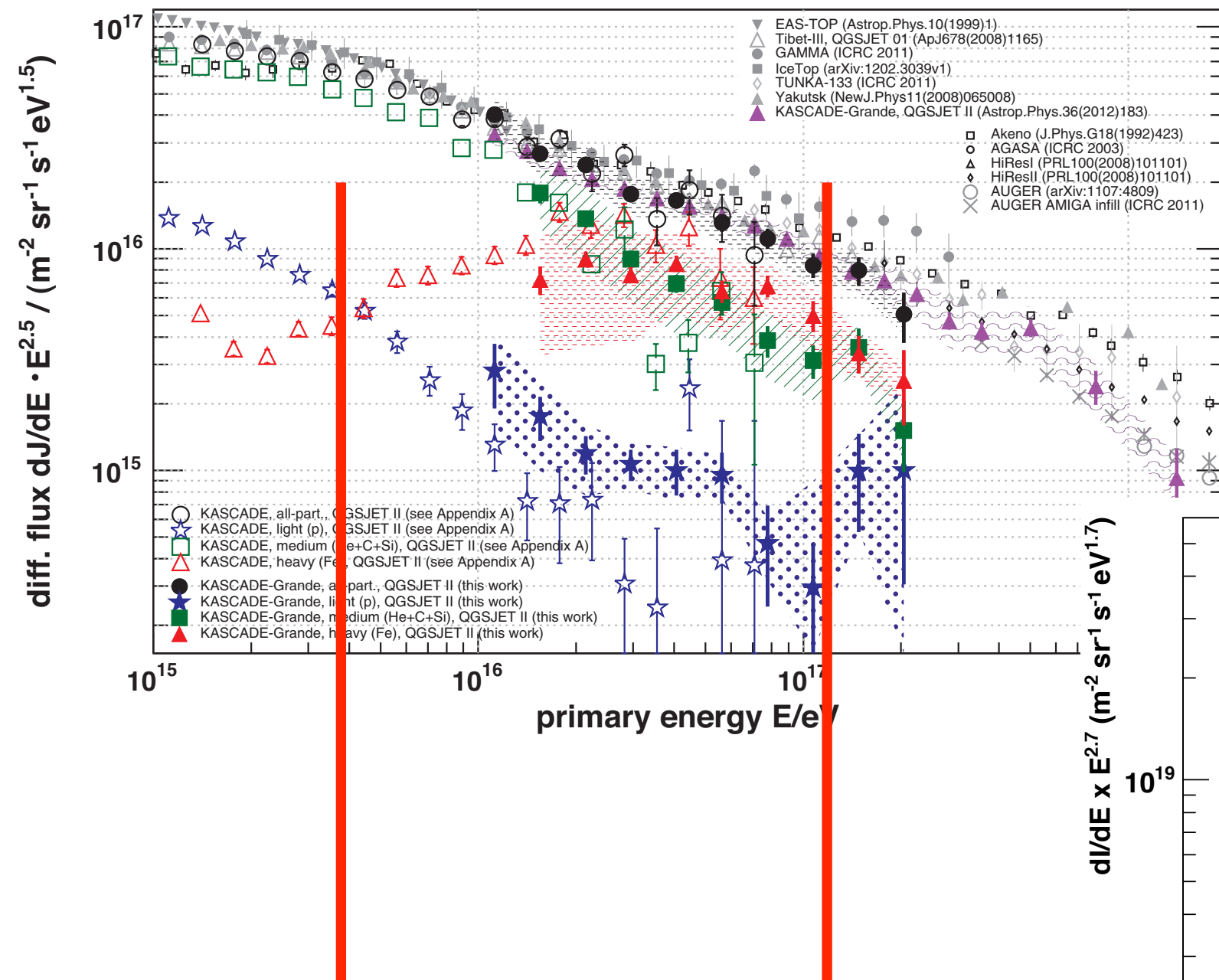
KASCADE-Grande



knee 4 PeV

26 * 4 PeV

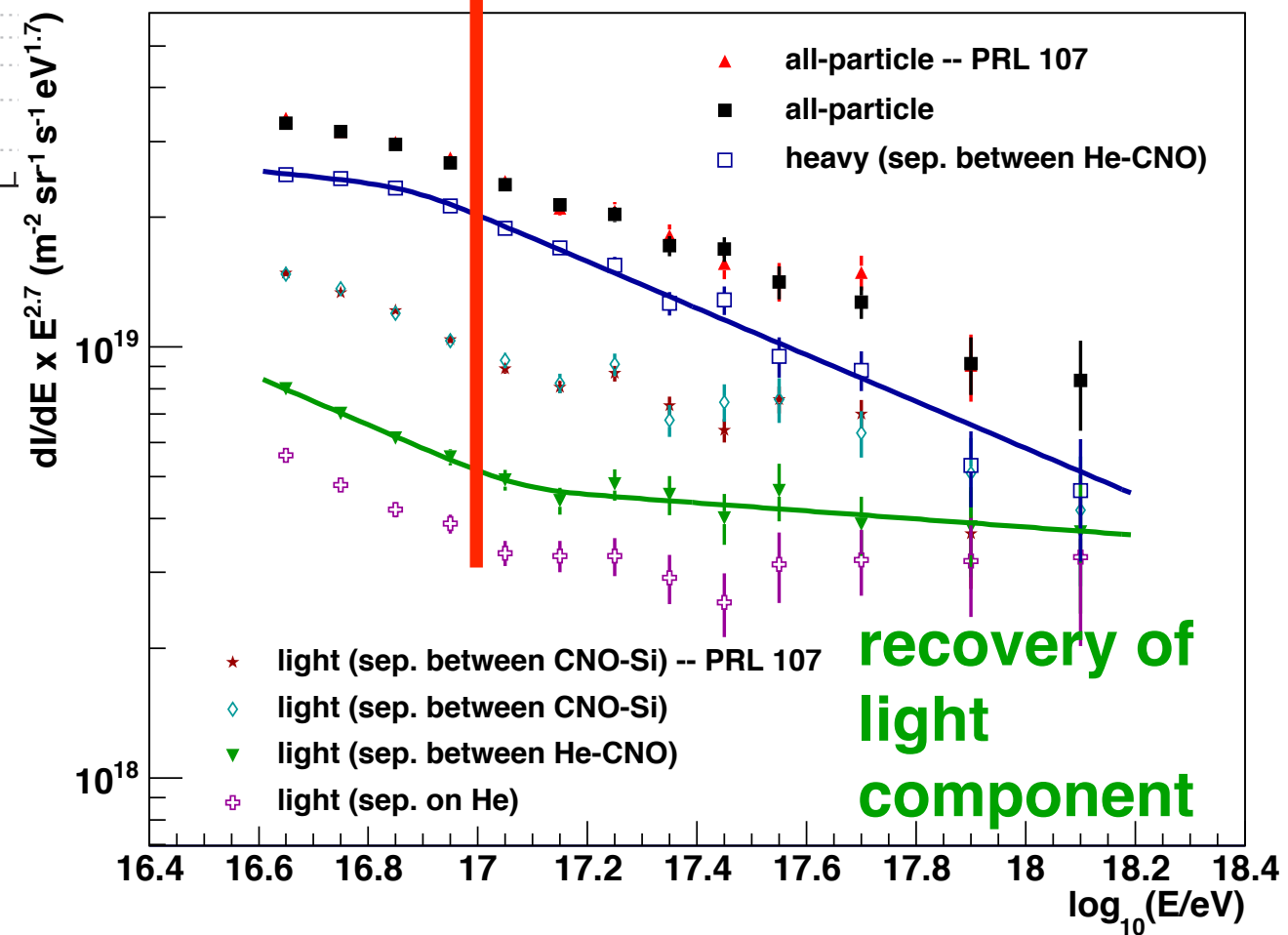
KASCADE-Grande



knee 4 PeV

26 * 4 PeV

26 * 4 PeV



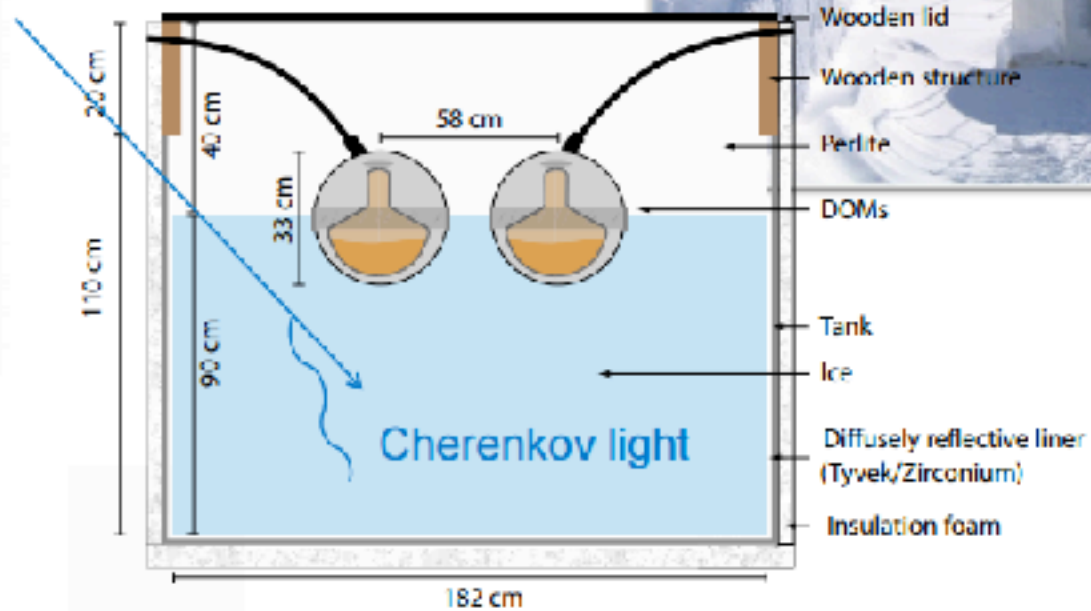
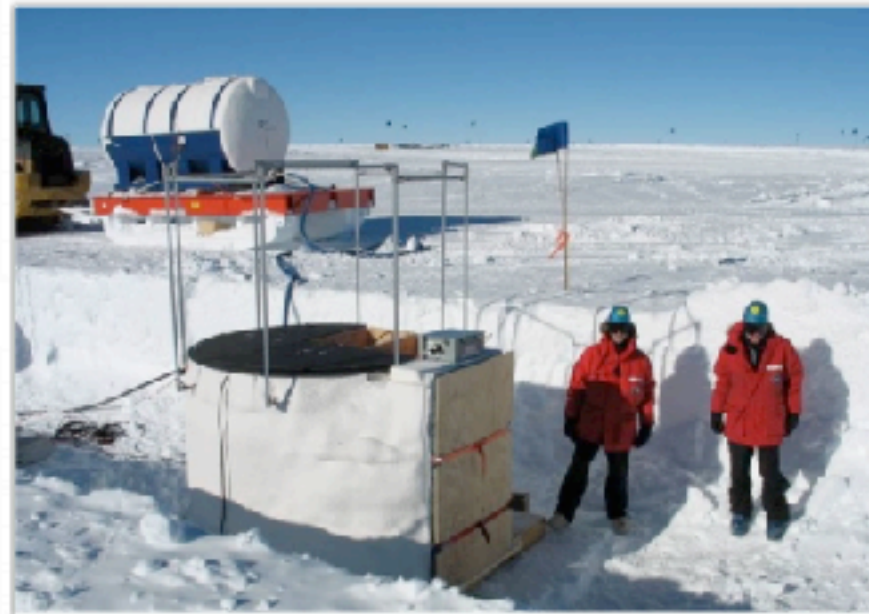
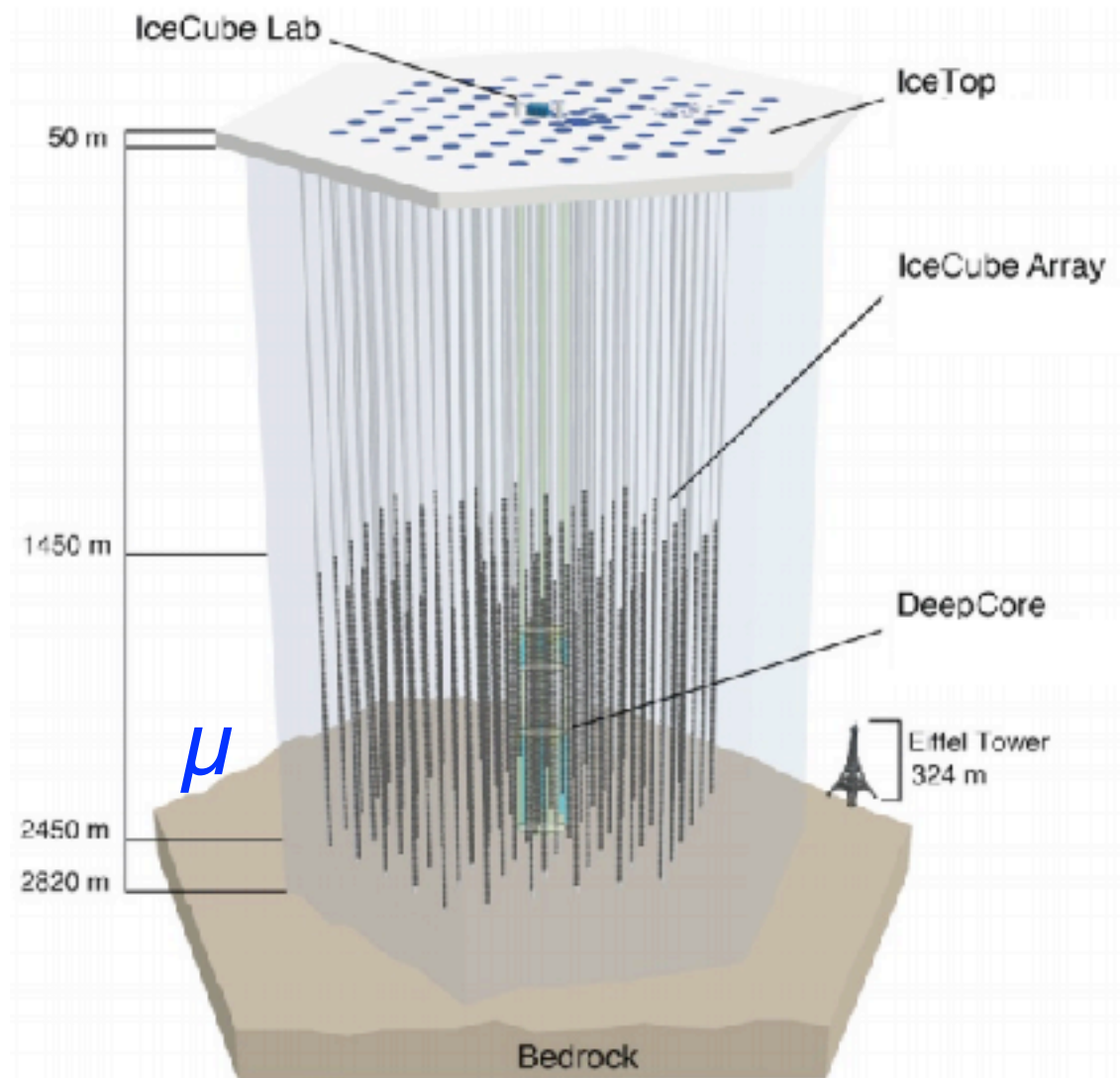
W.D. Apel et al., PRD 87 (2013) 081101

W.D. Apel et al., Astropart. Phys 47 (2013) 54

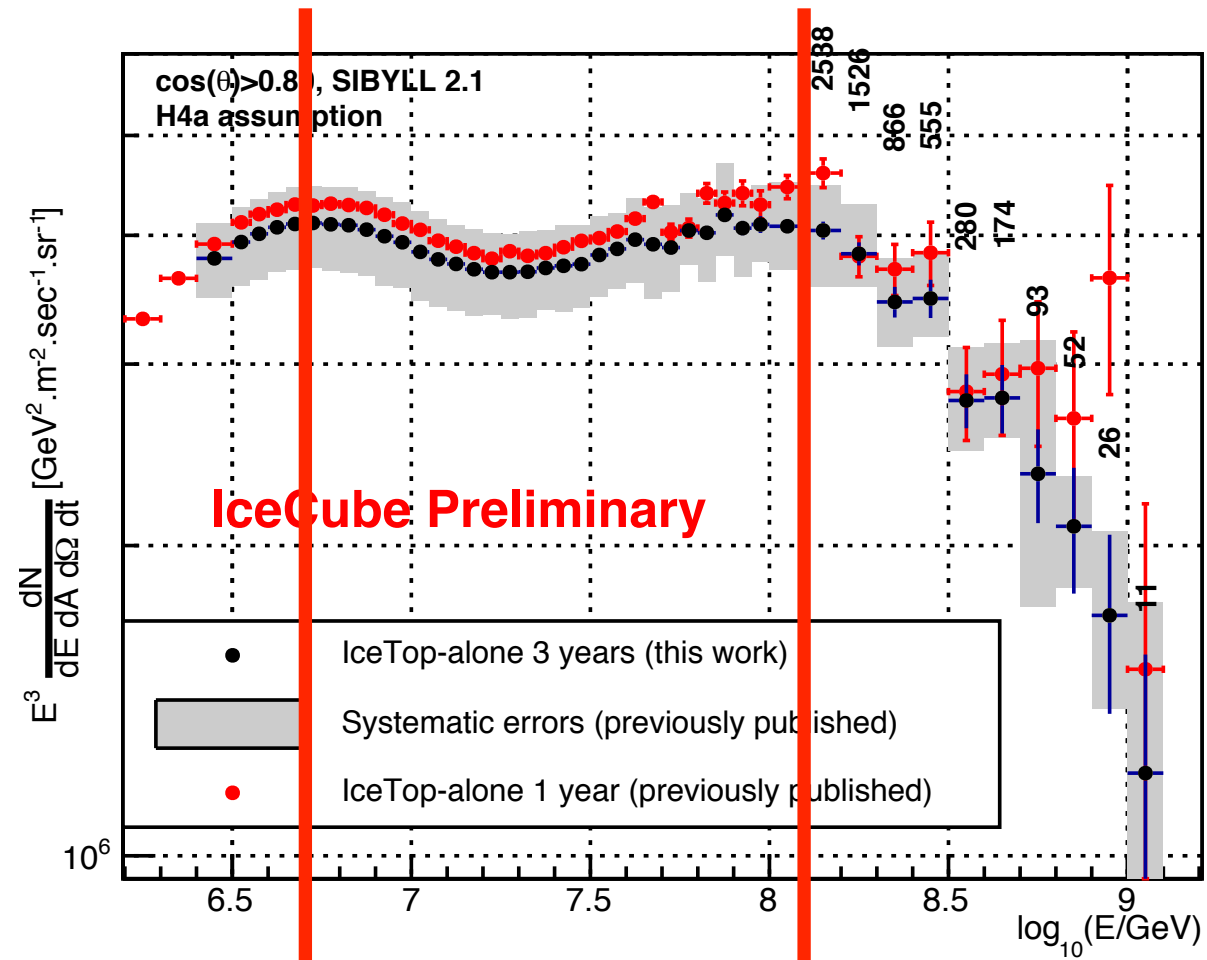
Ice Cube - Ice Top

$e/m (+\mu)$

IceTop



Ice Cube - Ice Top

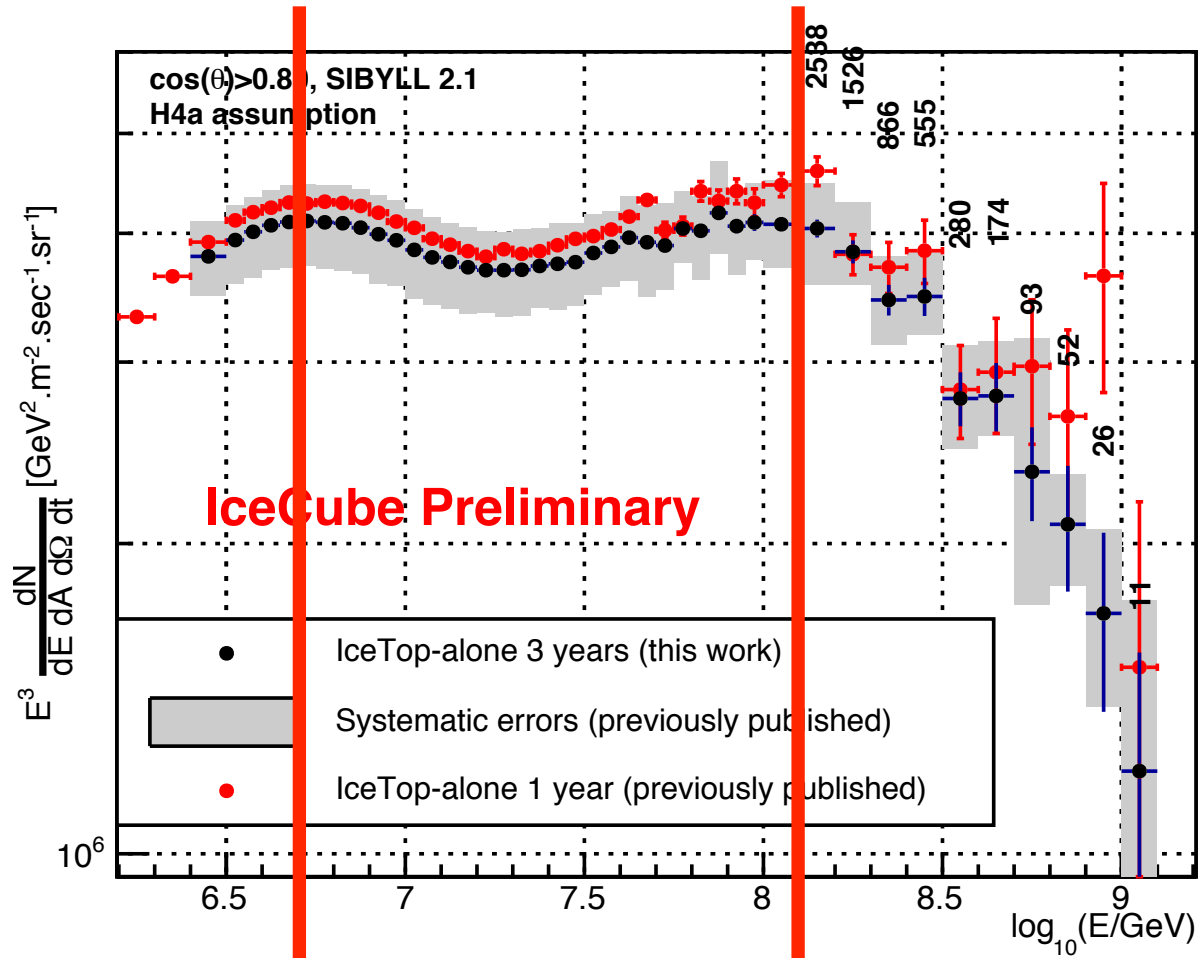


5 PeV

26*5 PeV

Ice Top only

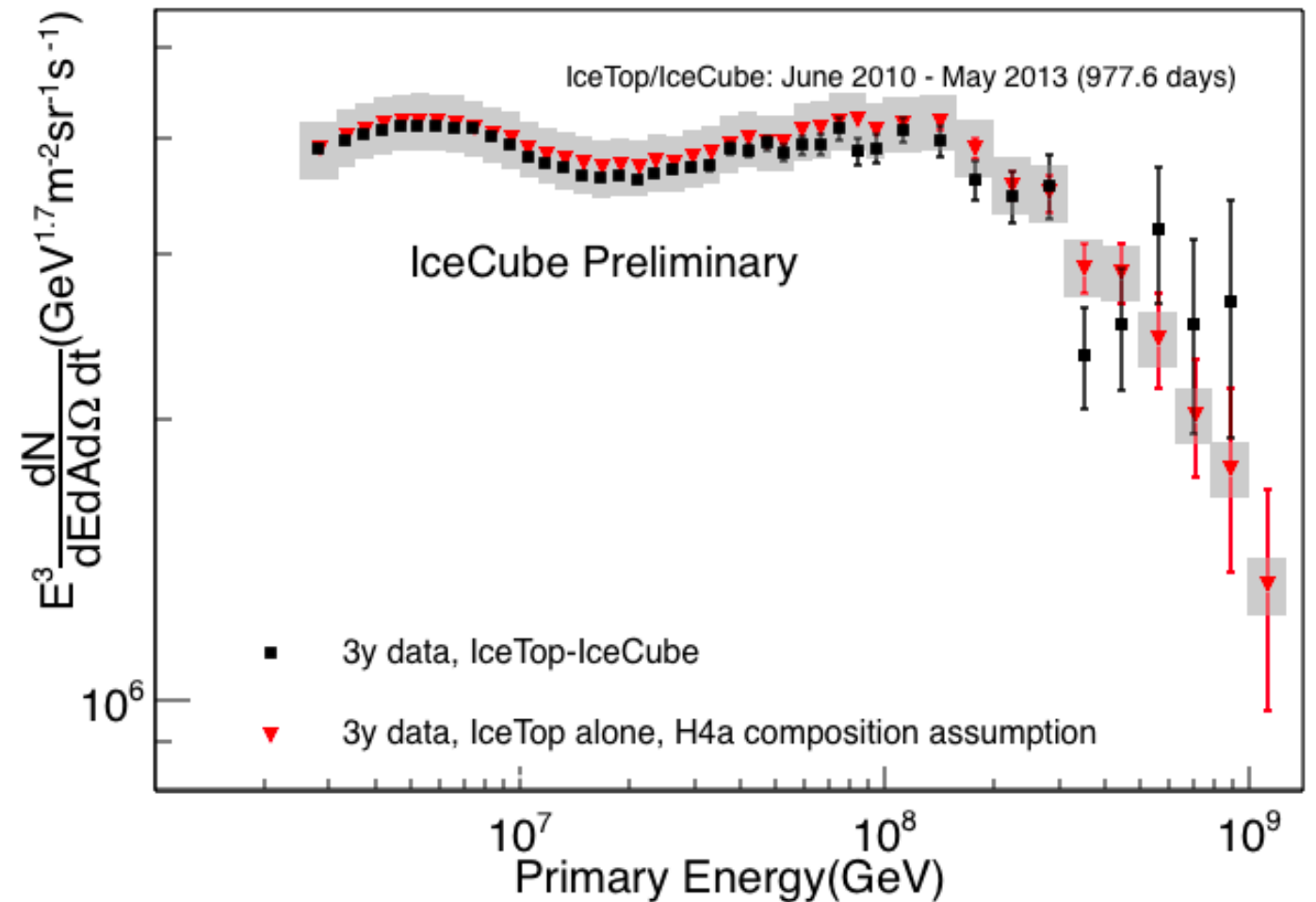
Ice Cube - Ice Top



5 PeV

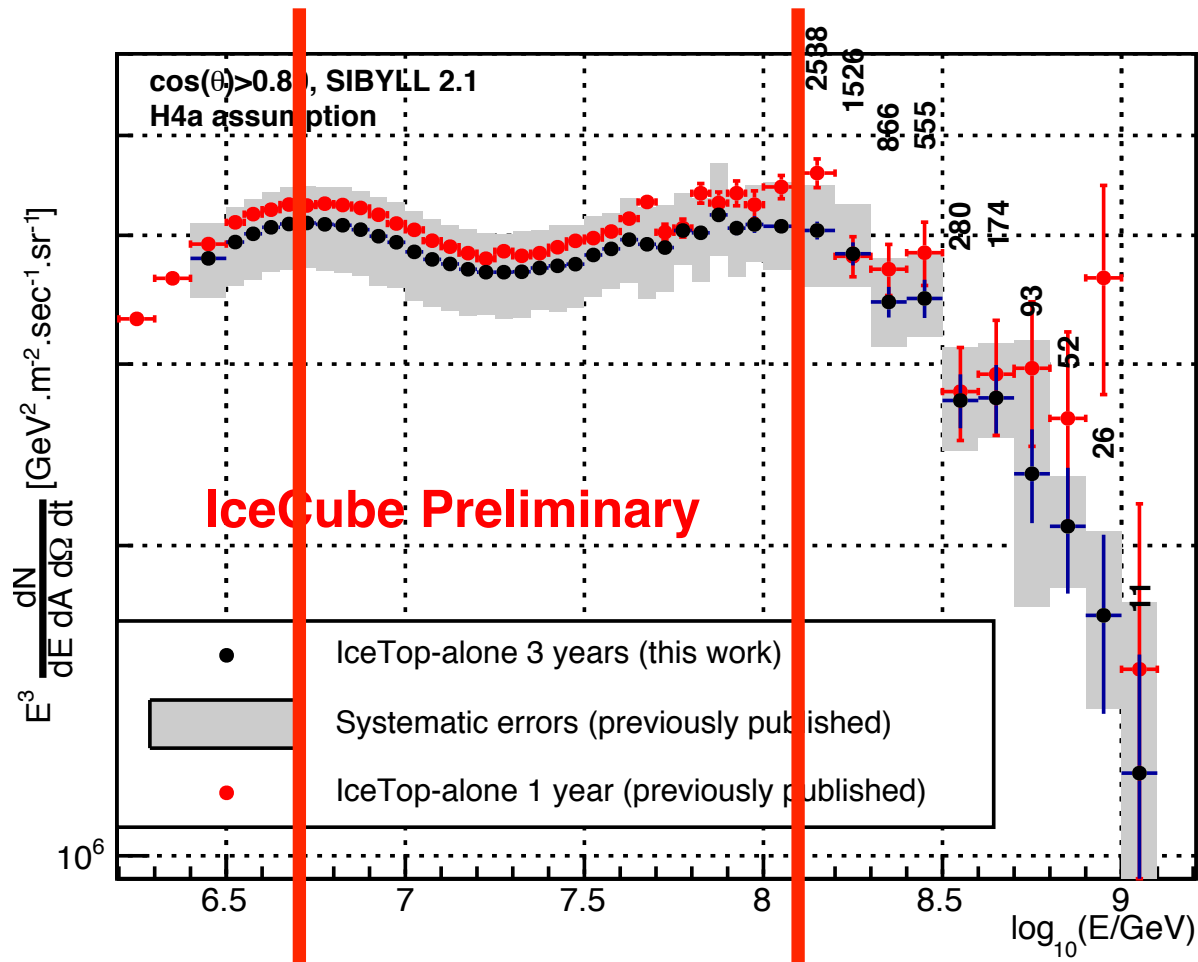
26*5 PeV

Ice Top only



combined

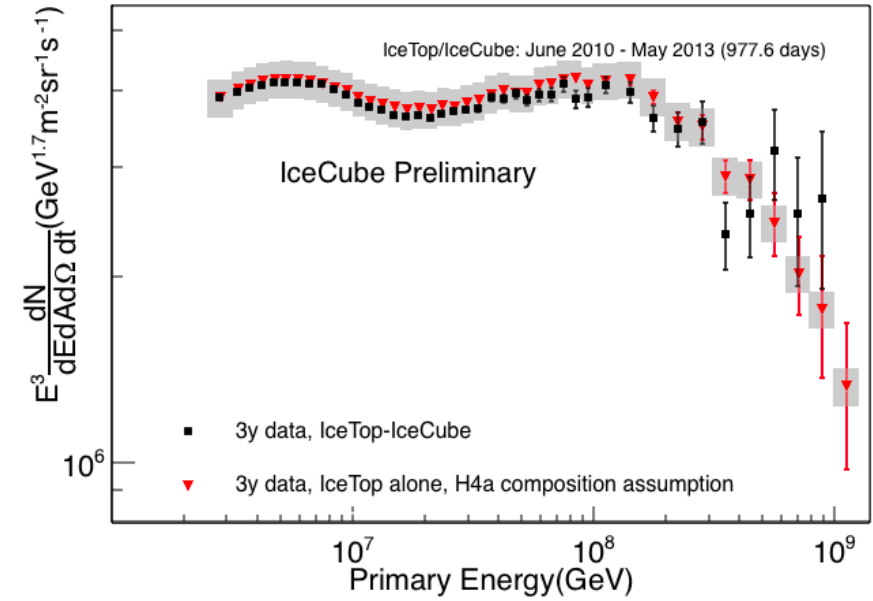
Ice Cube - Ice Top



5 PeV

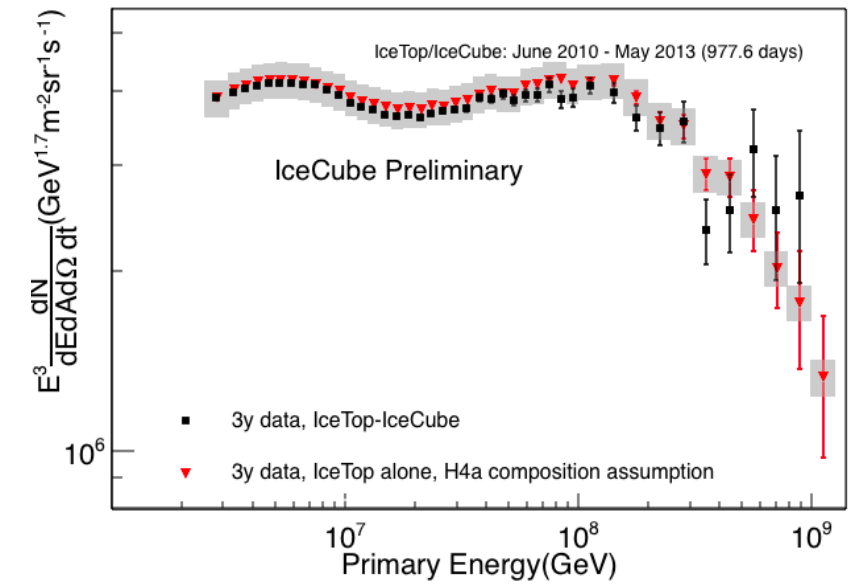
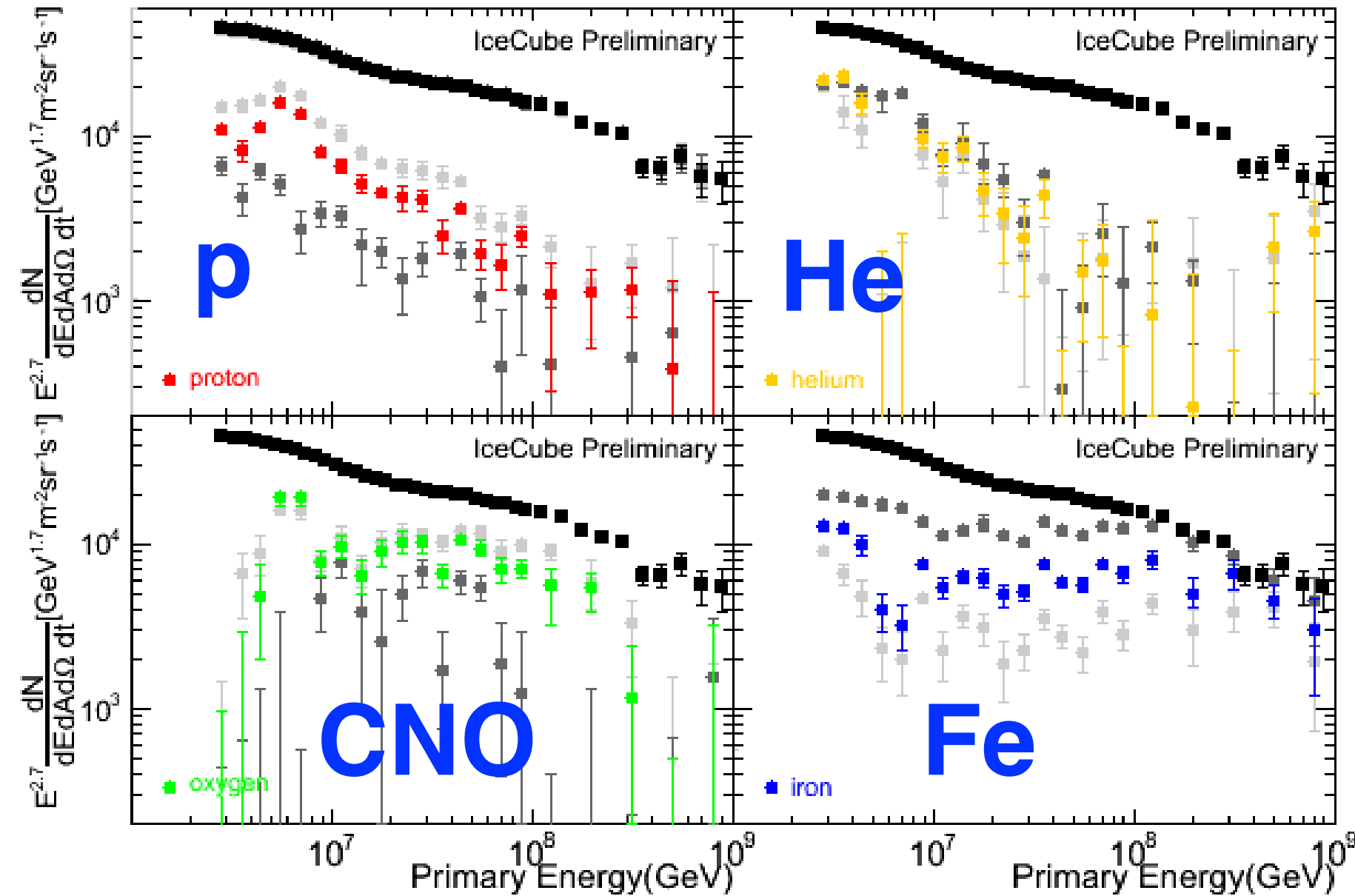
26*5 PeV

Ice Top only

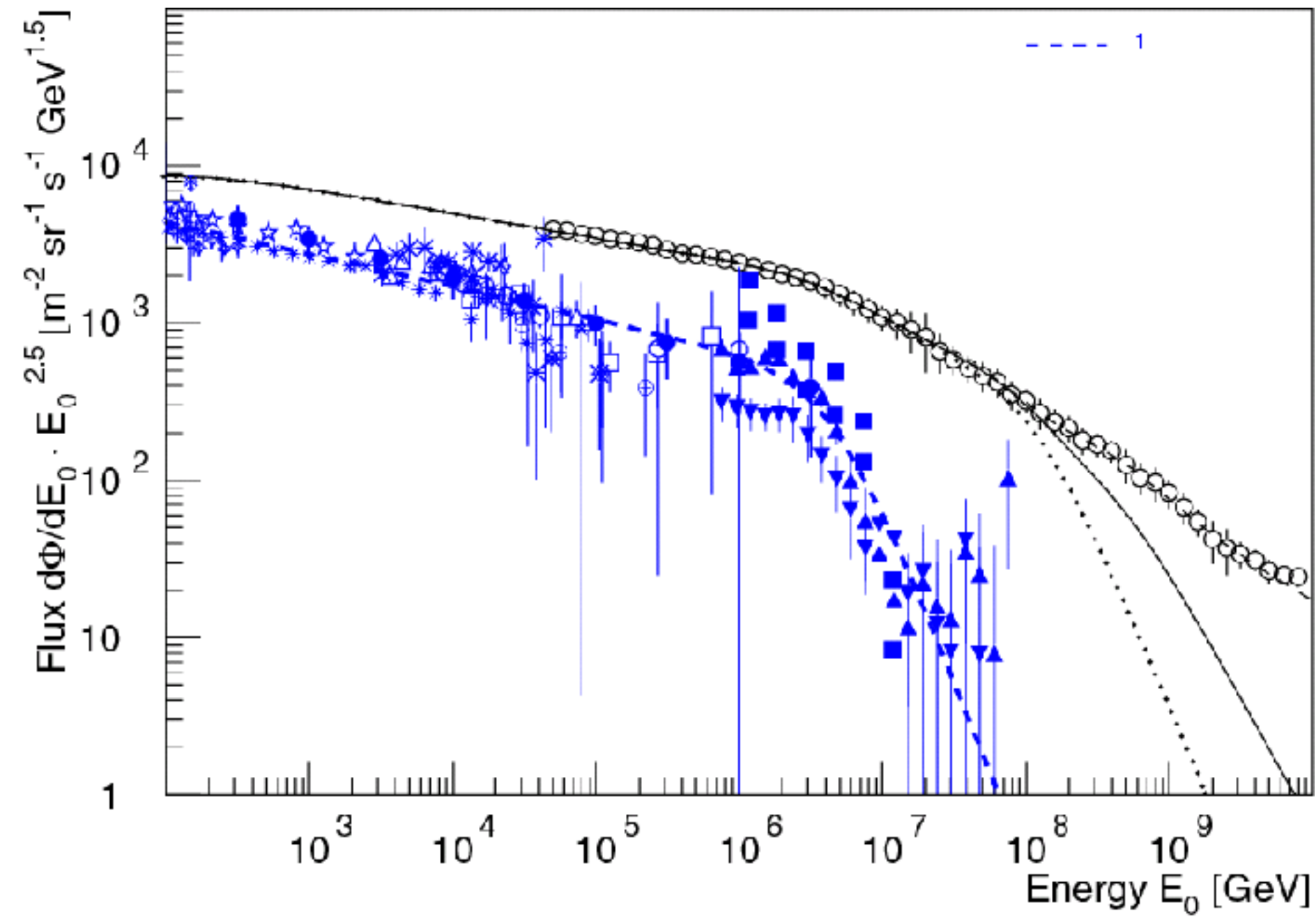


combined

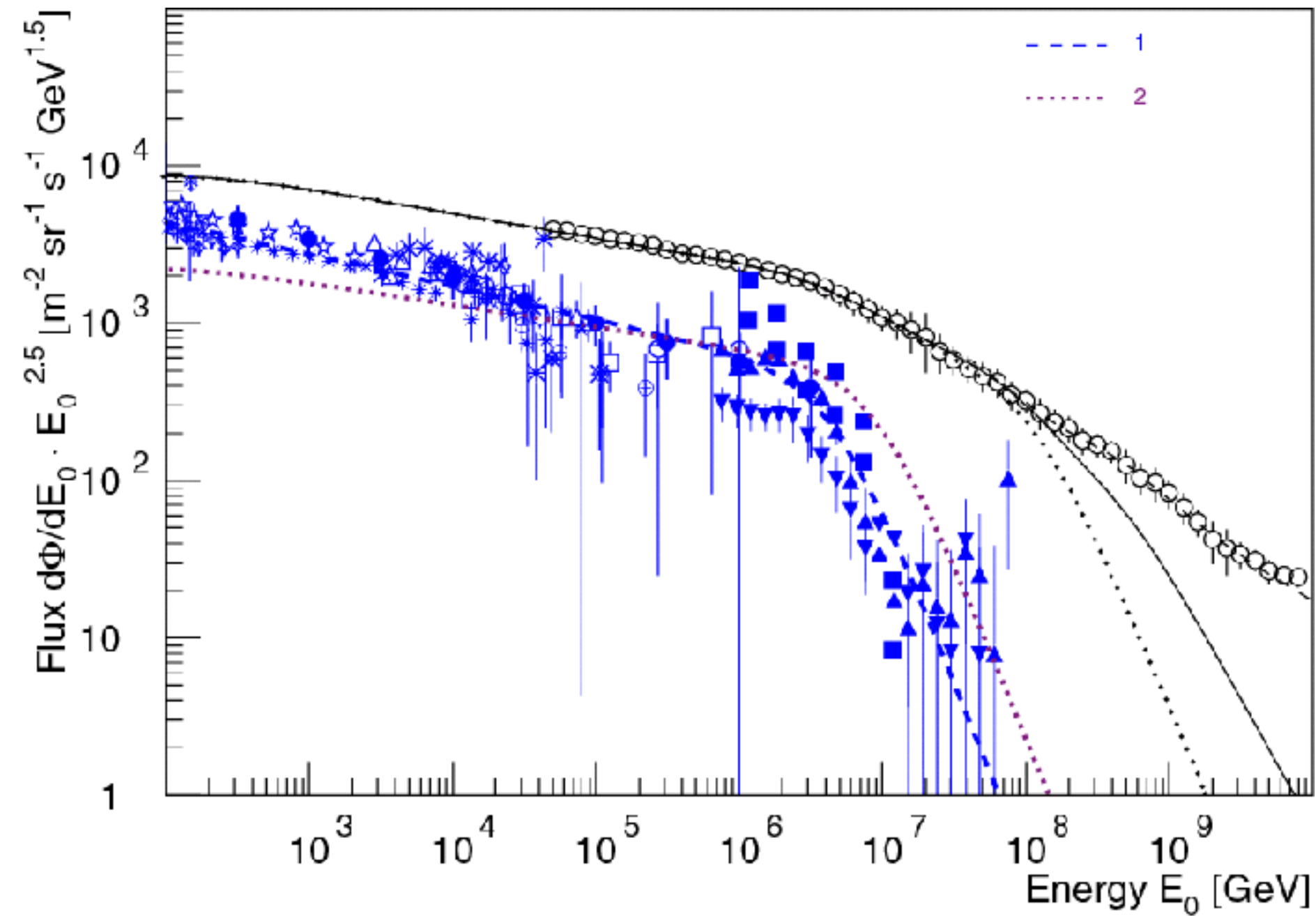
Ice Cube - Ice Top



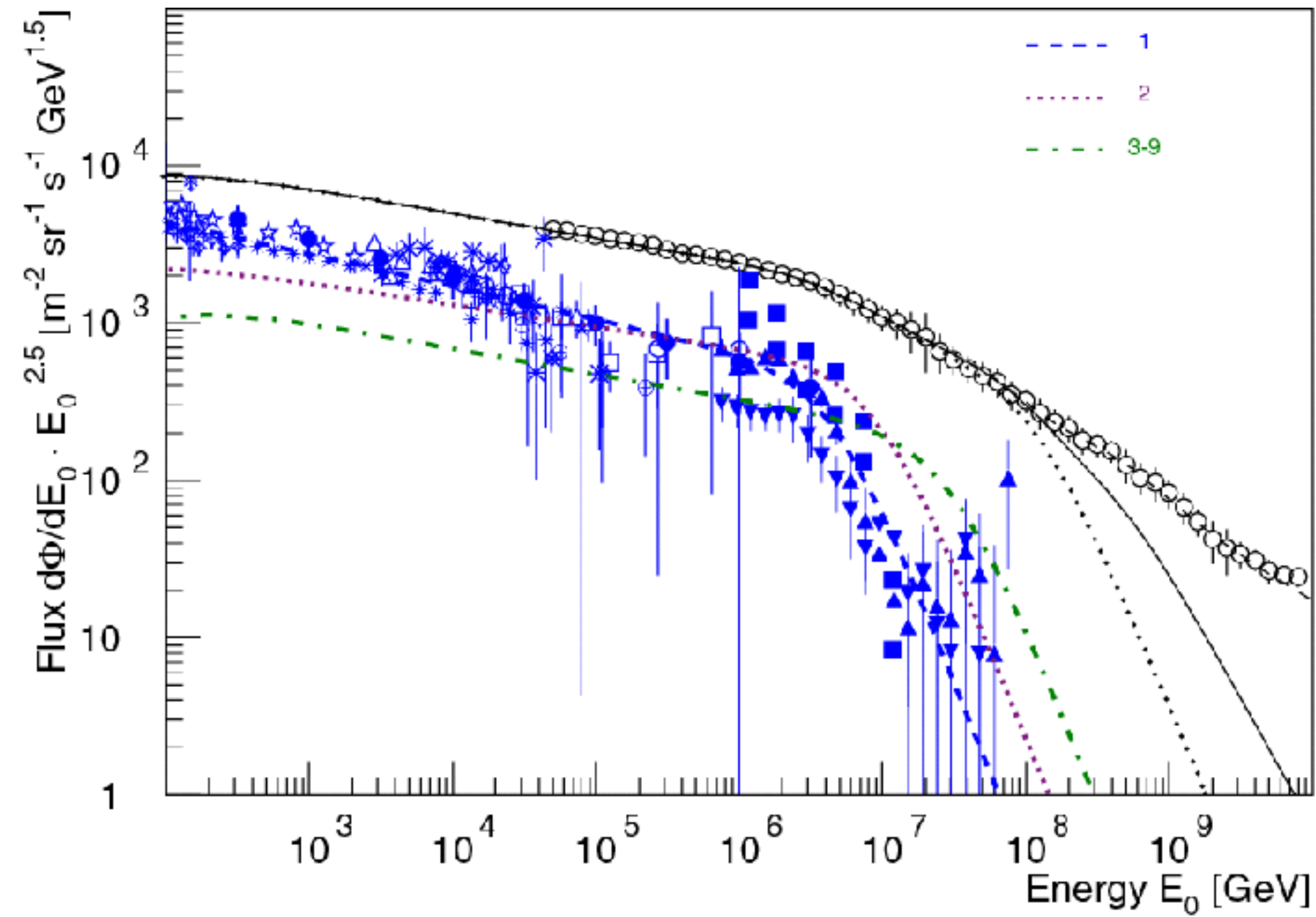
Cosmic-ray energy spectrum



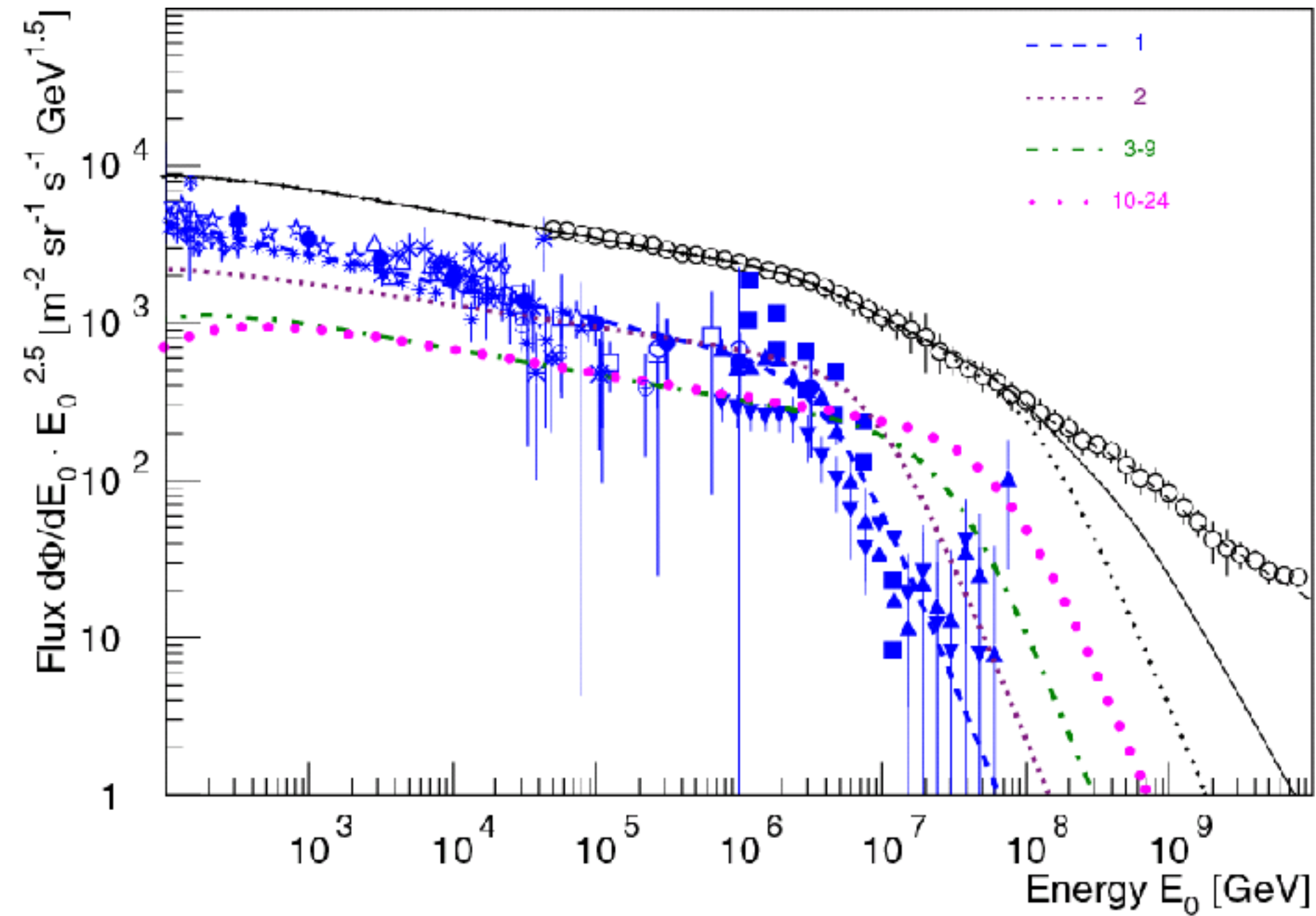
Cosmic-ray energy spectrum



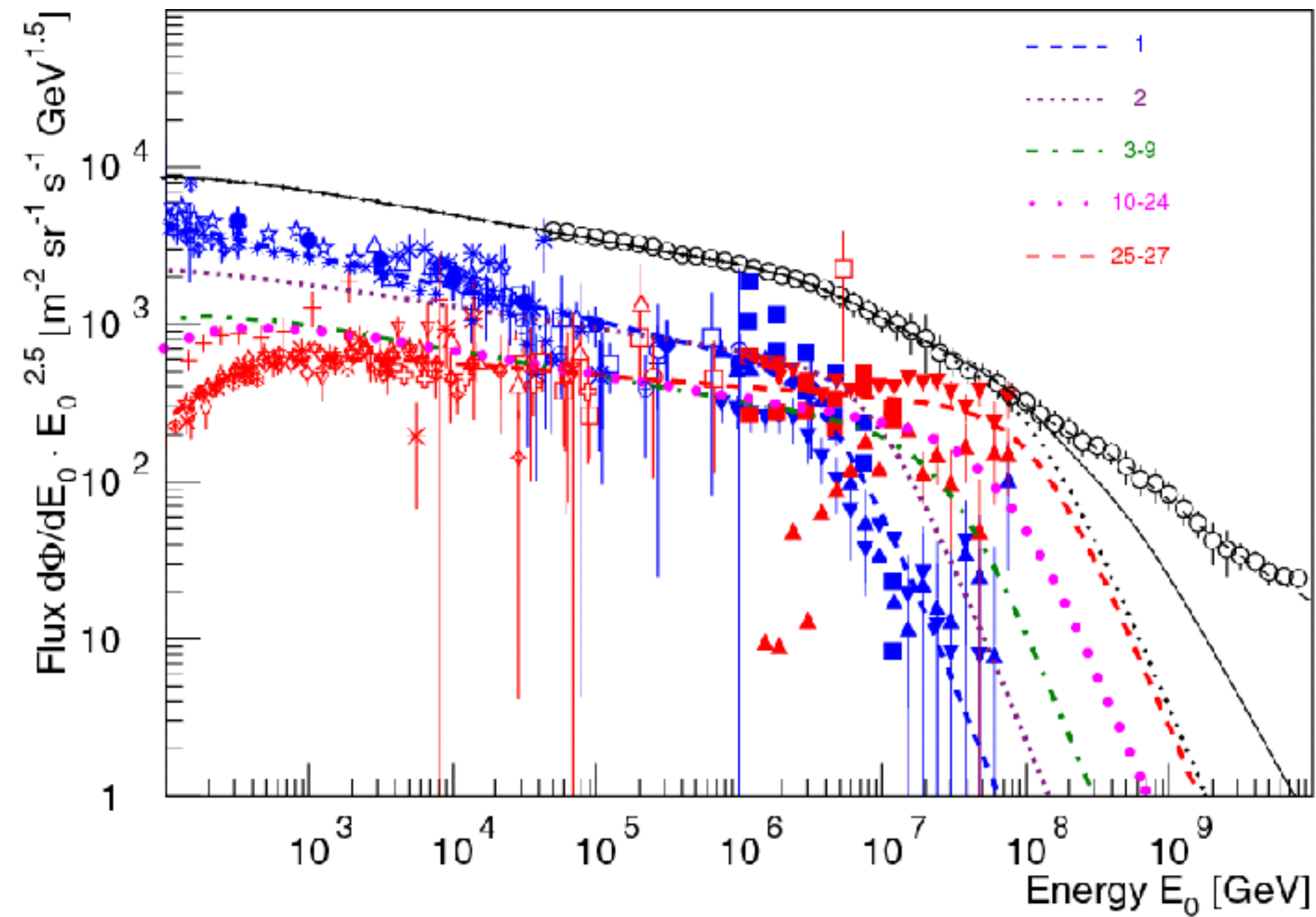
Cosmic-ray energy spectrum



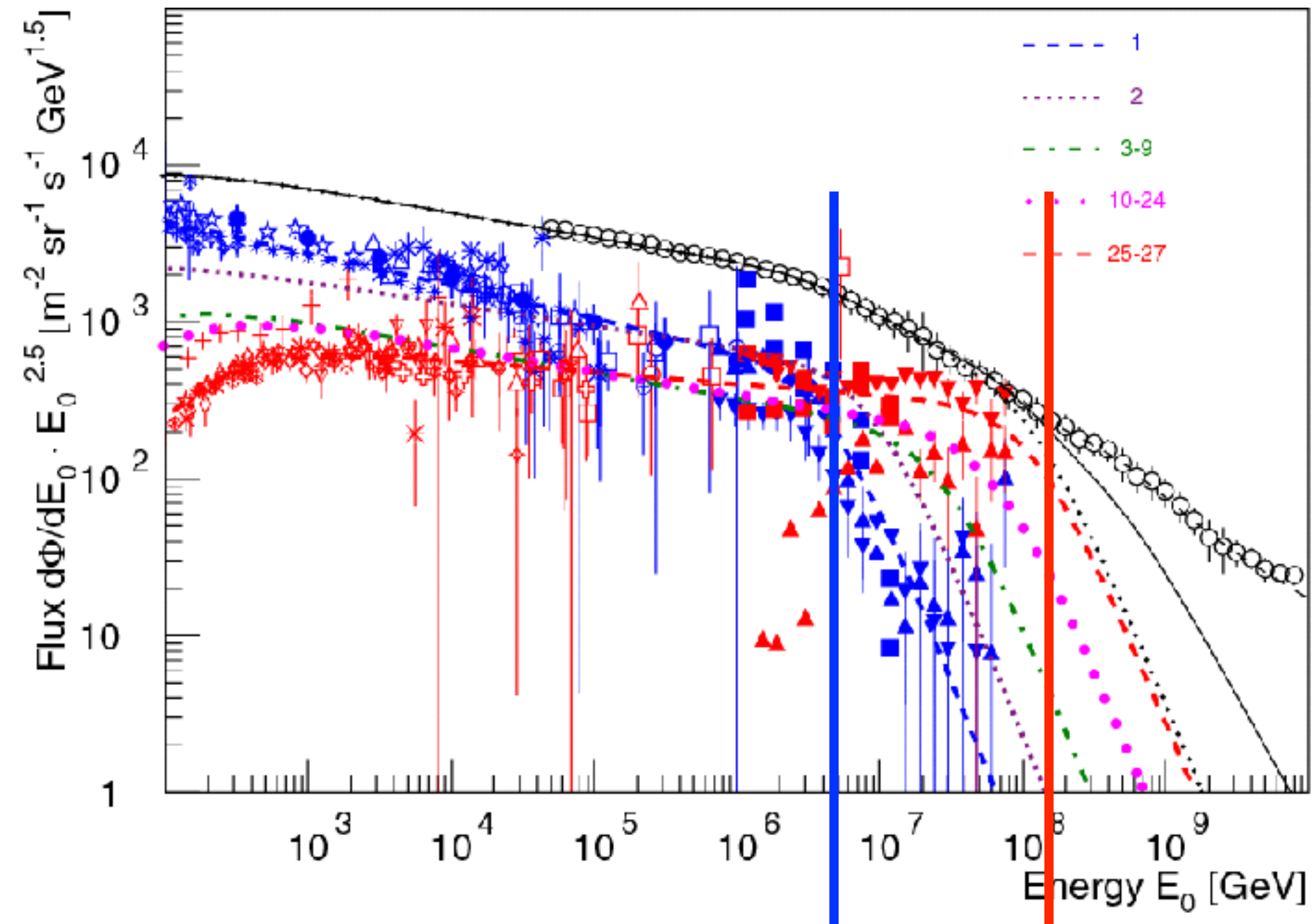
Cosmic-ray energy spectrum



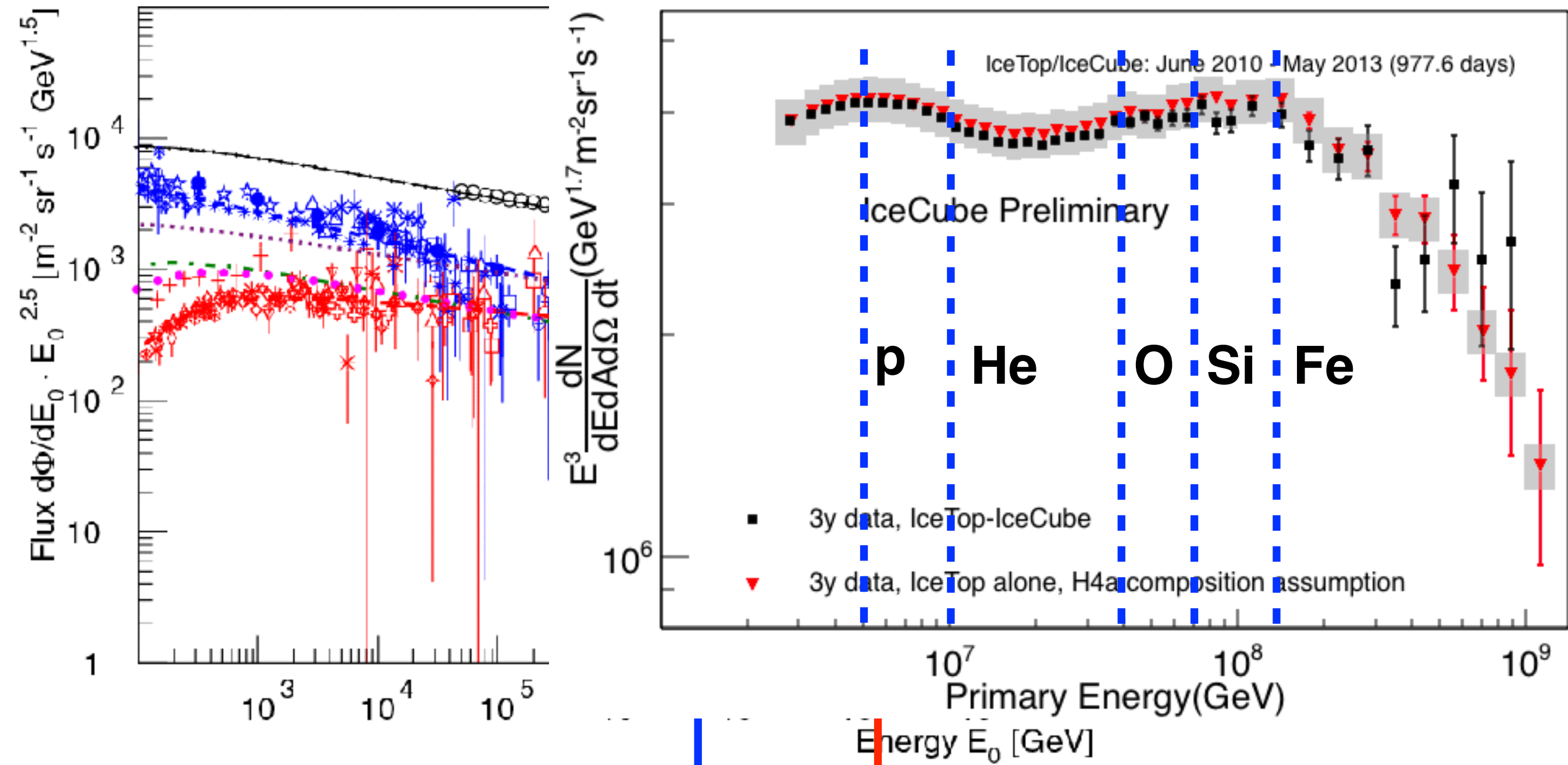
Cosmic-ray energy spectrum



Cosmic-ray energy spectrum



Cosmic-ray energy spectrum



TALE (TA low-energy extension)

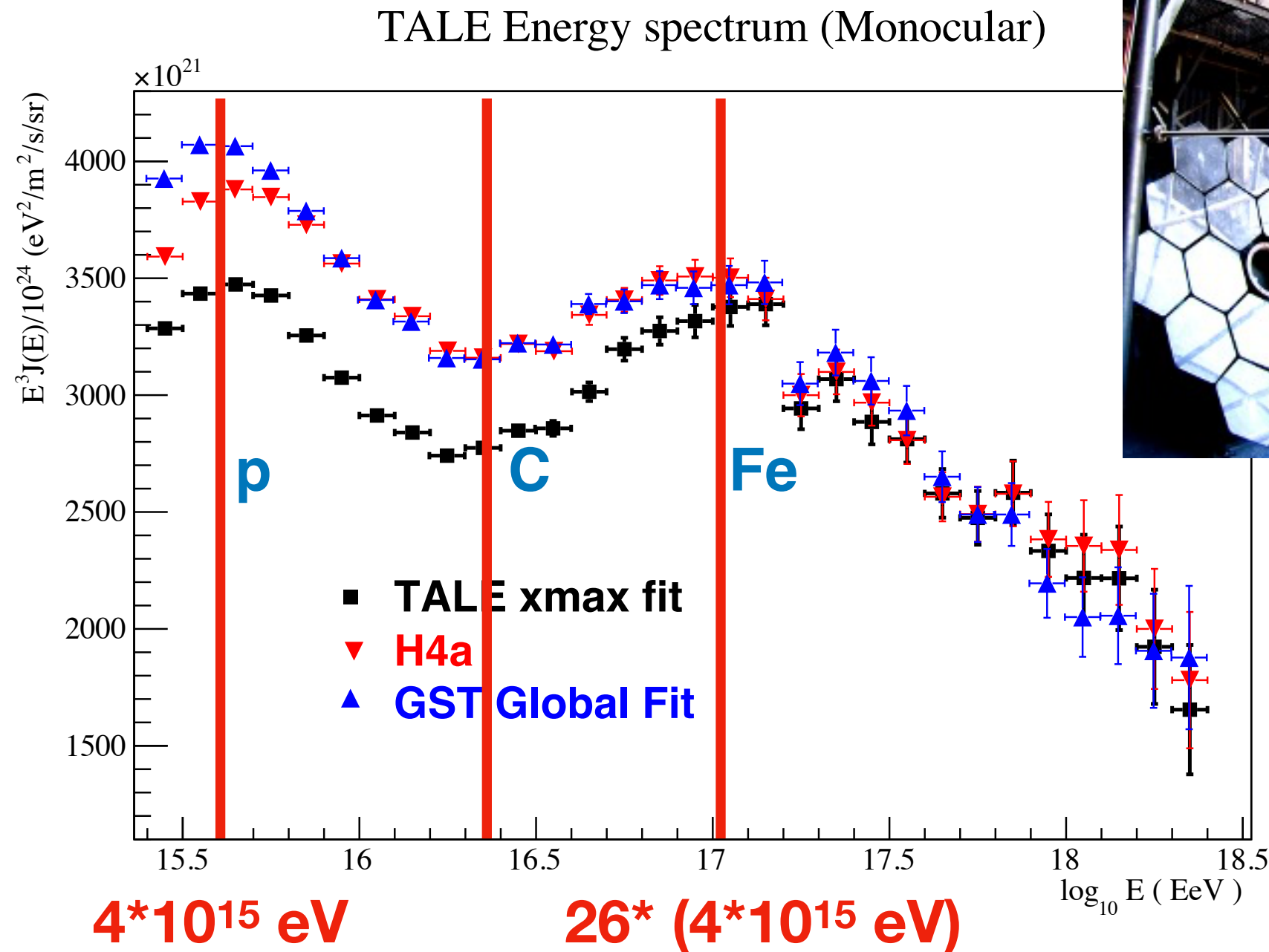
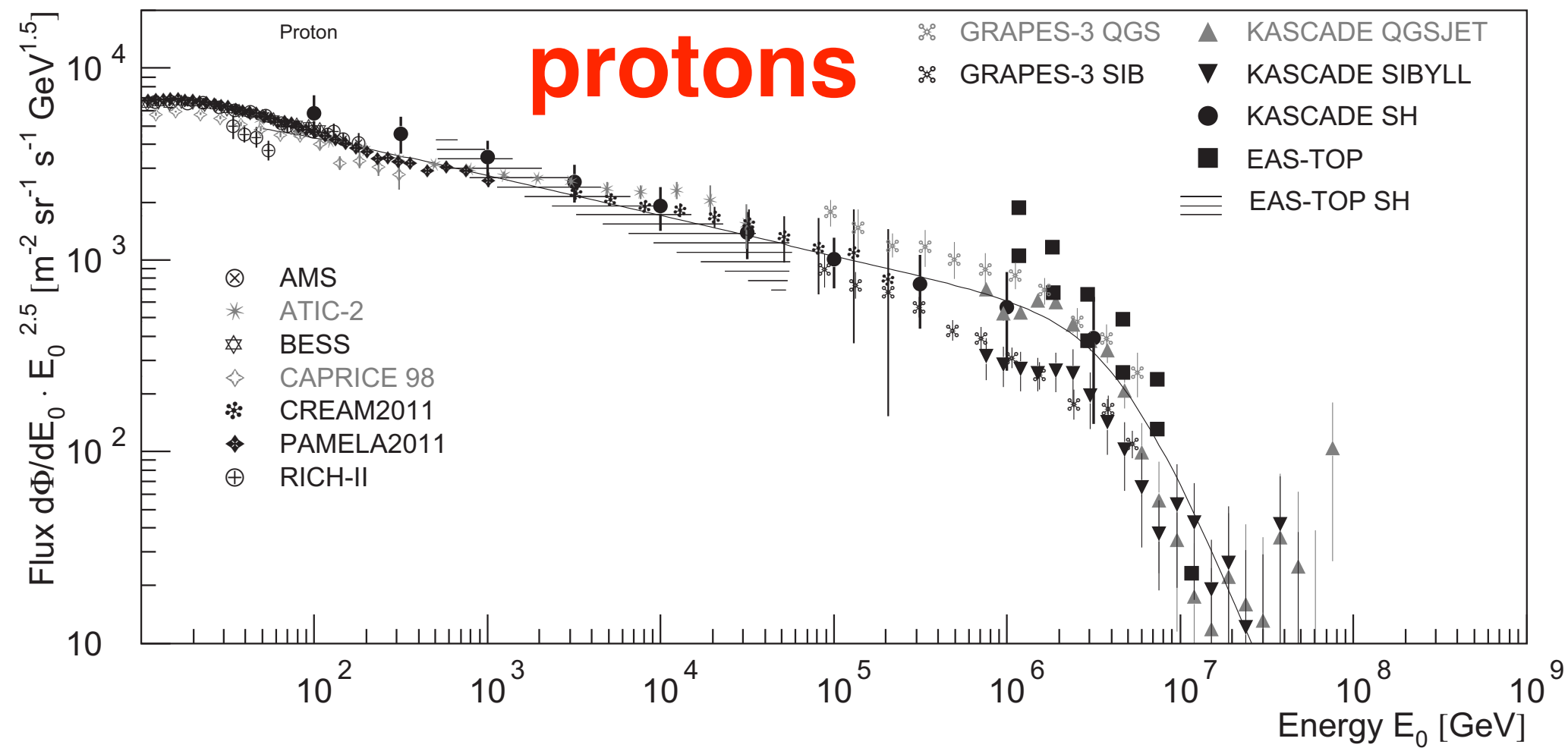
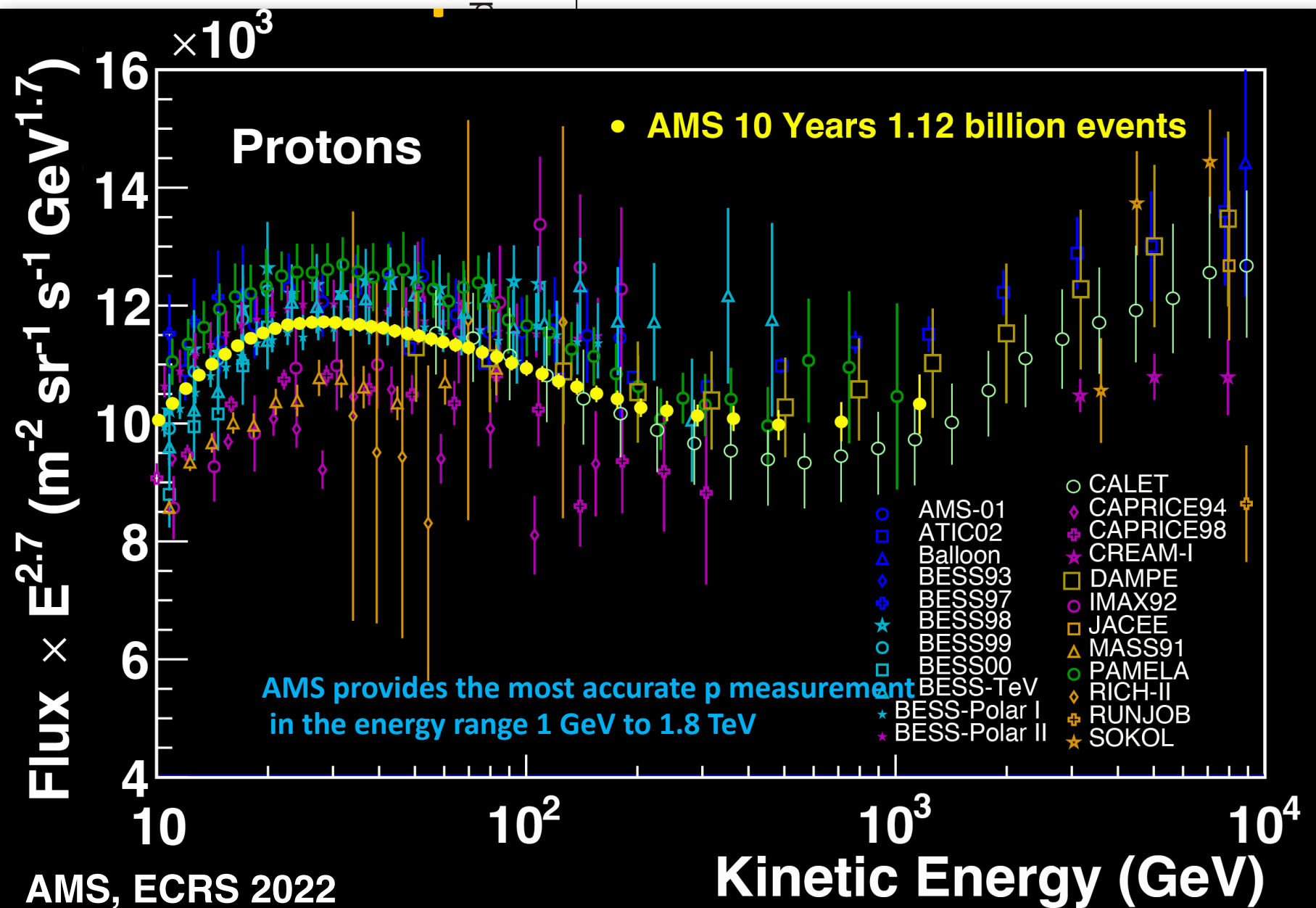
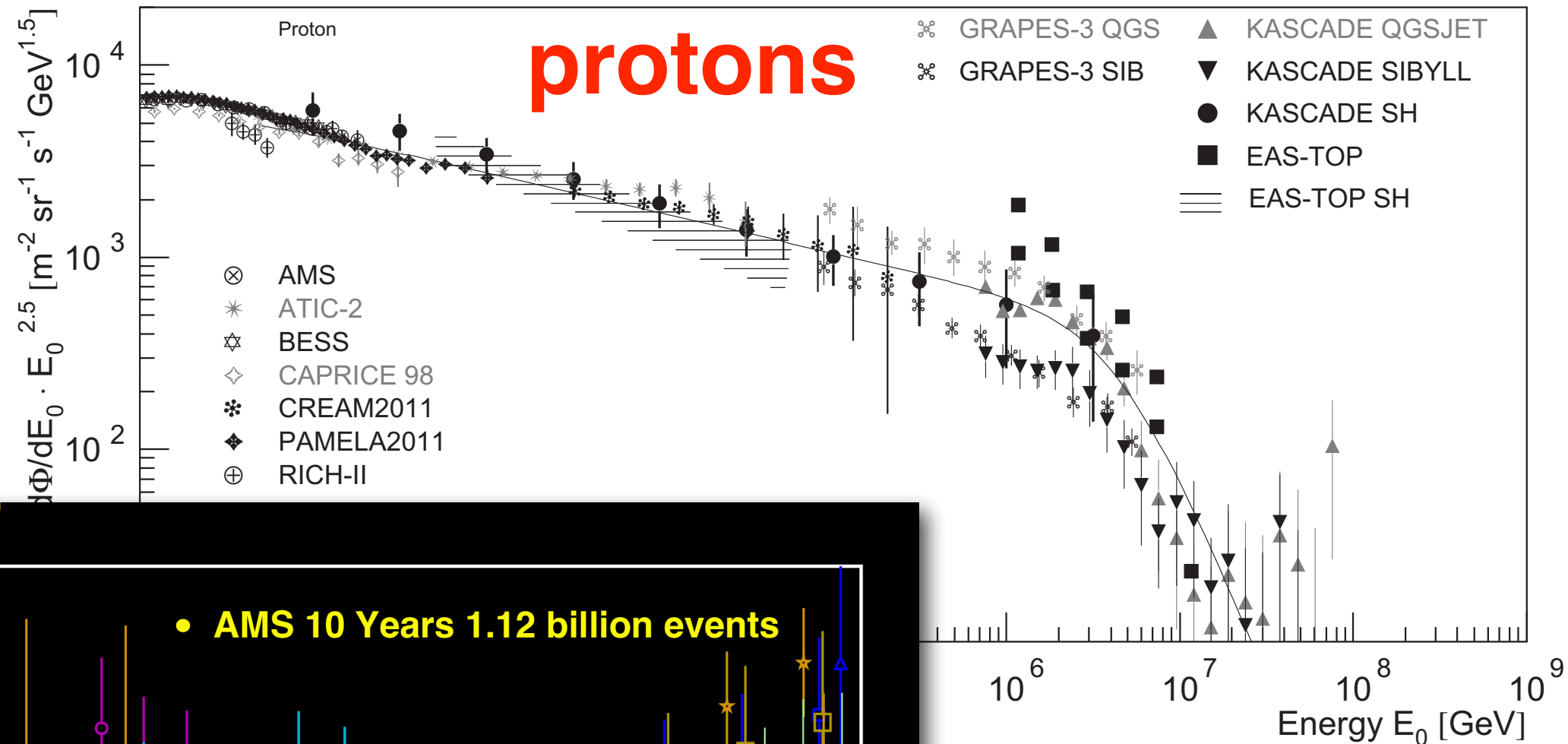
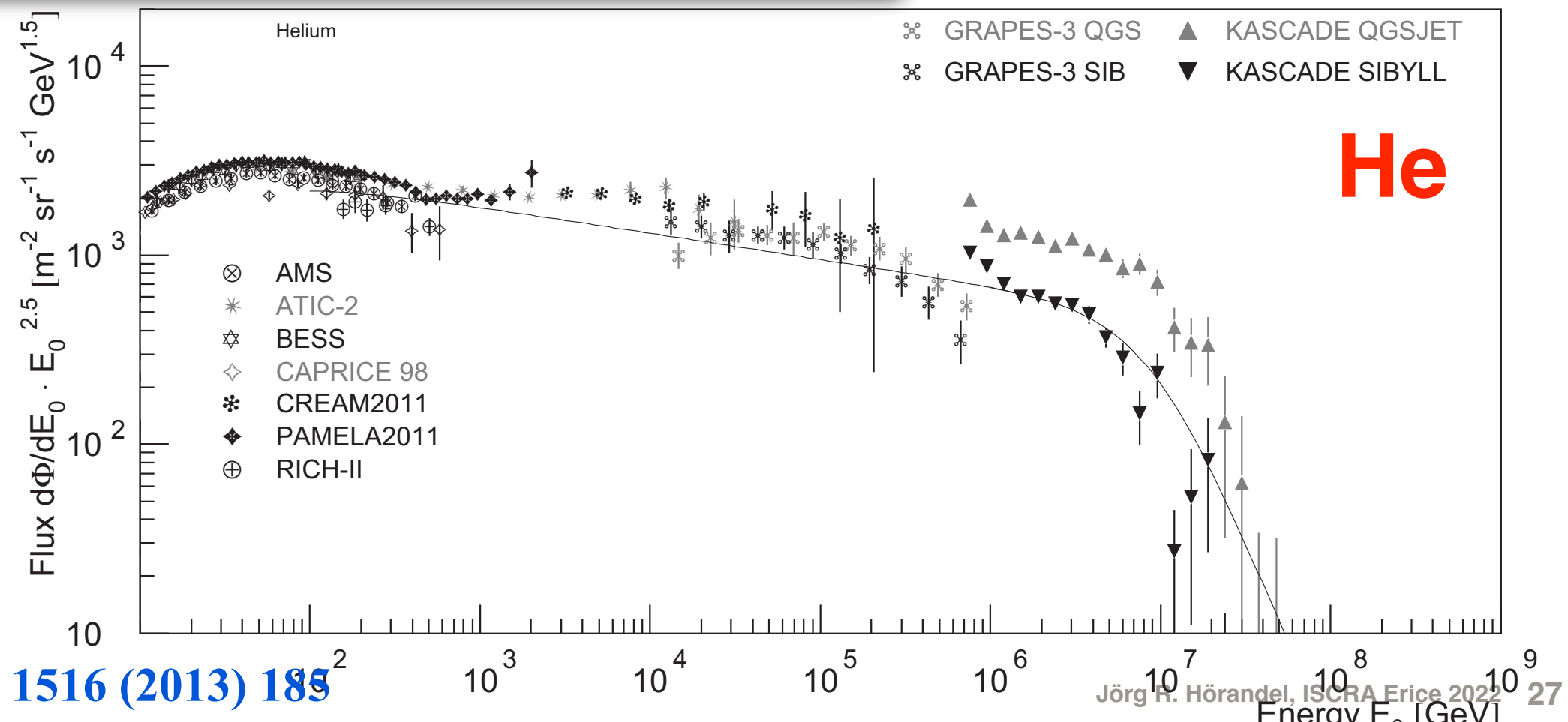
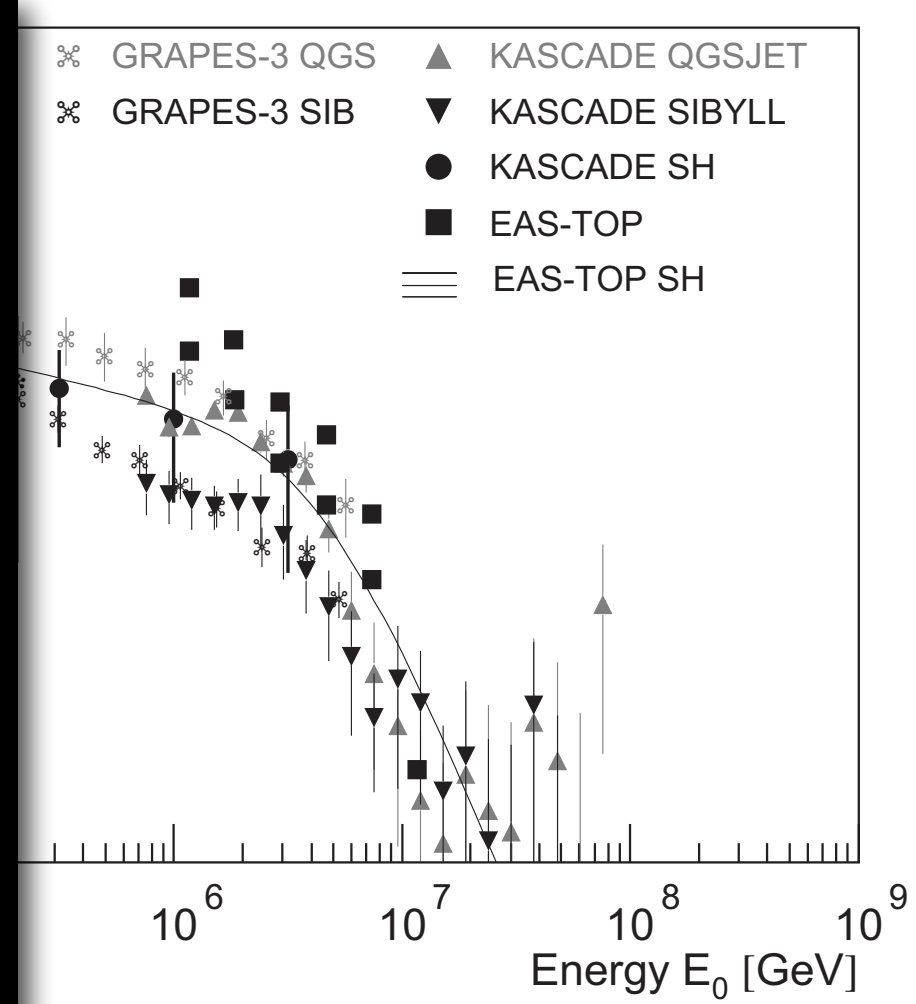
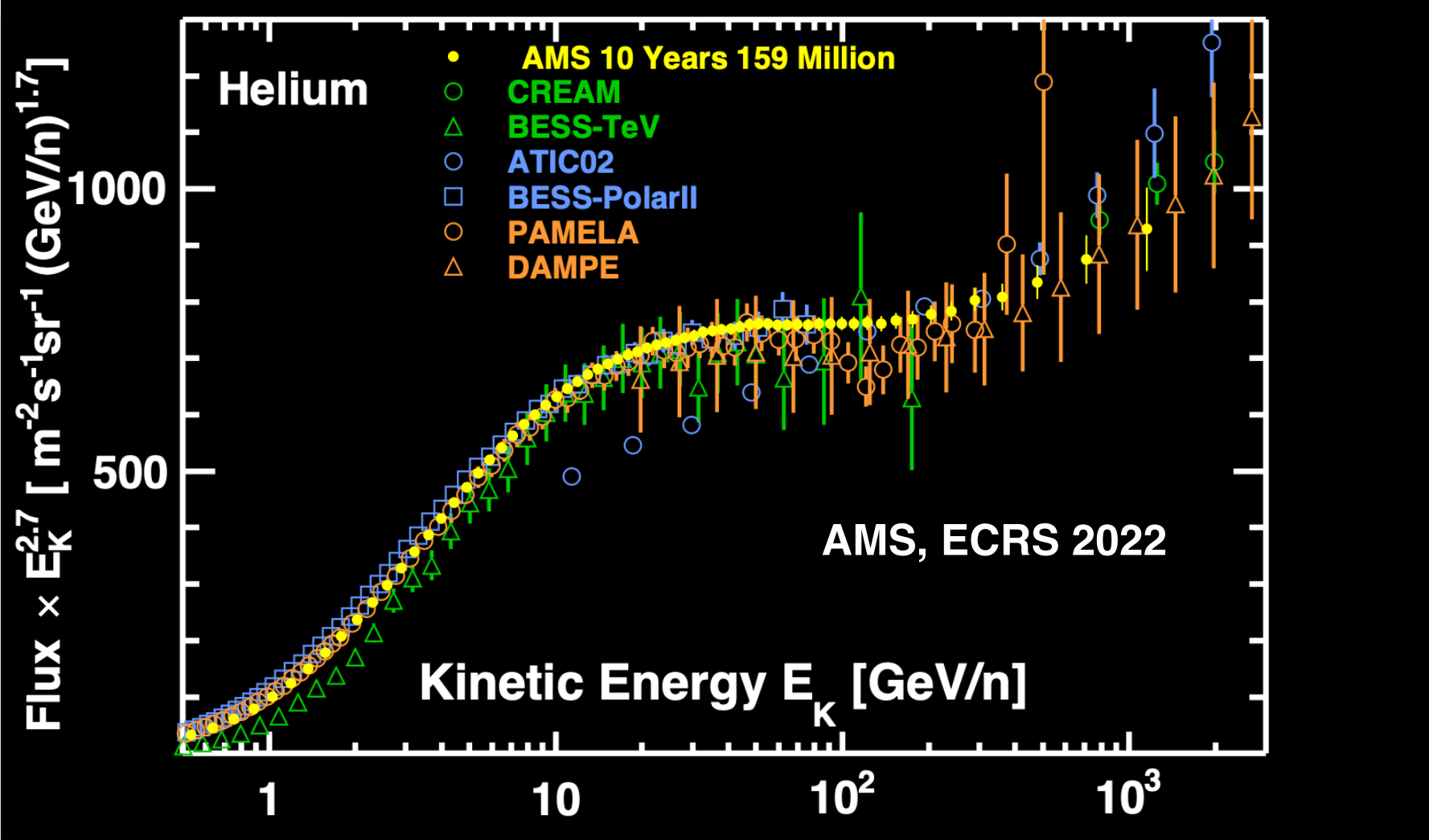
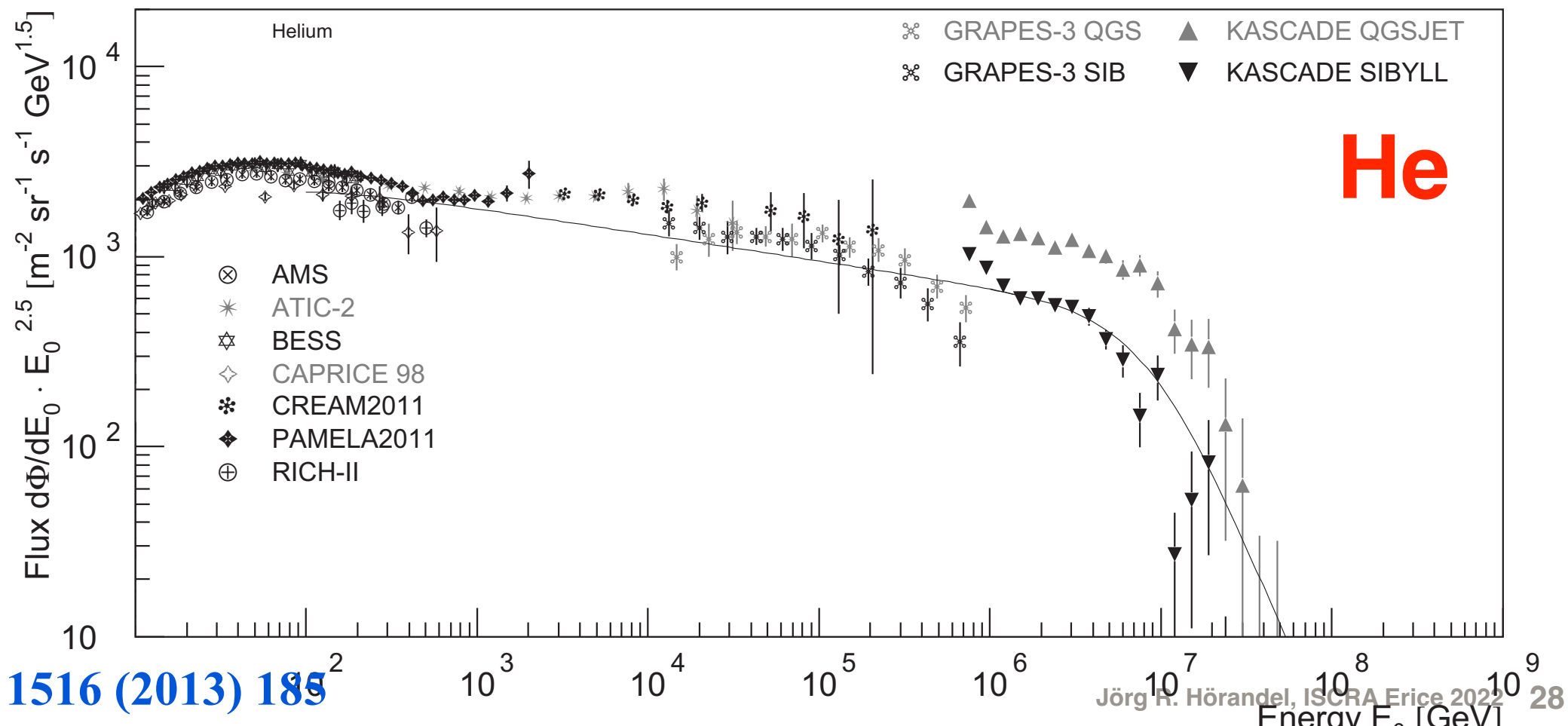
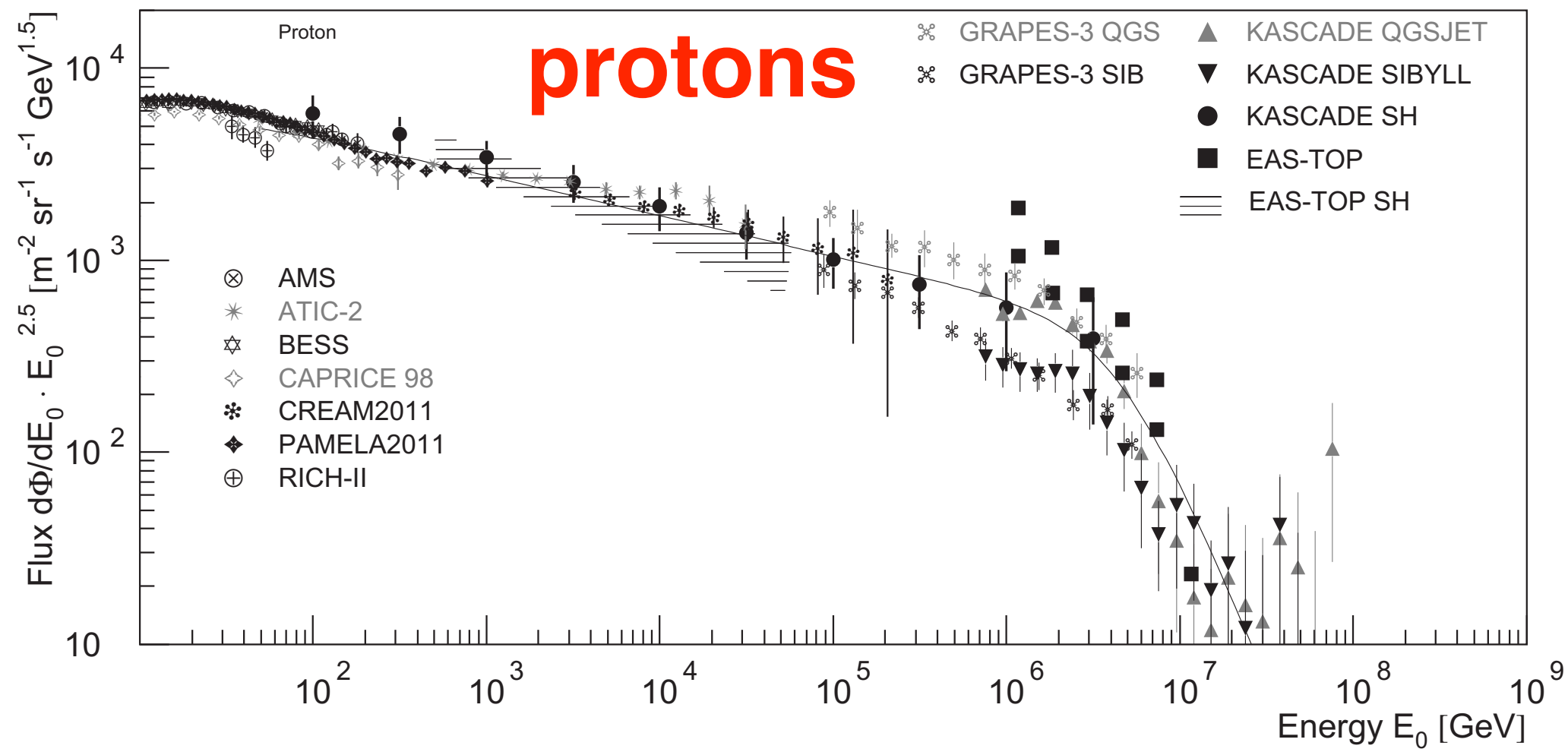


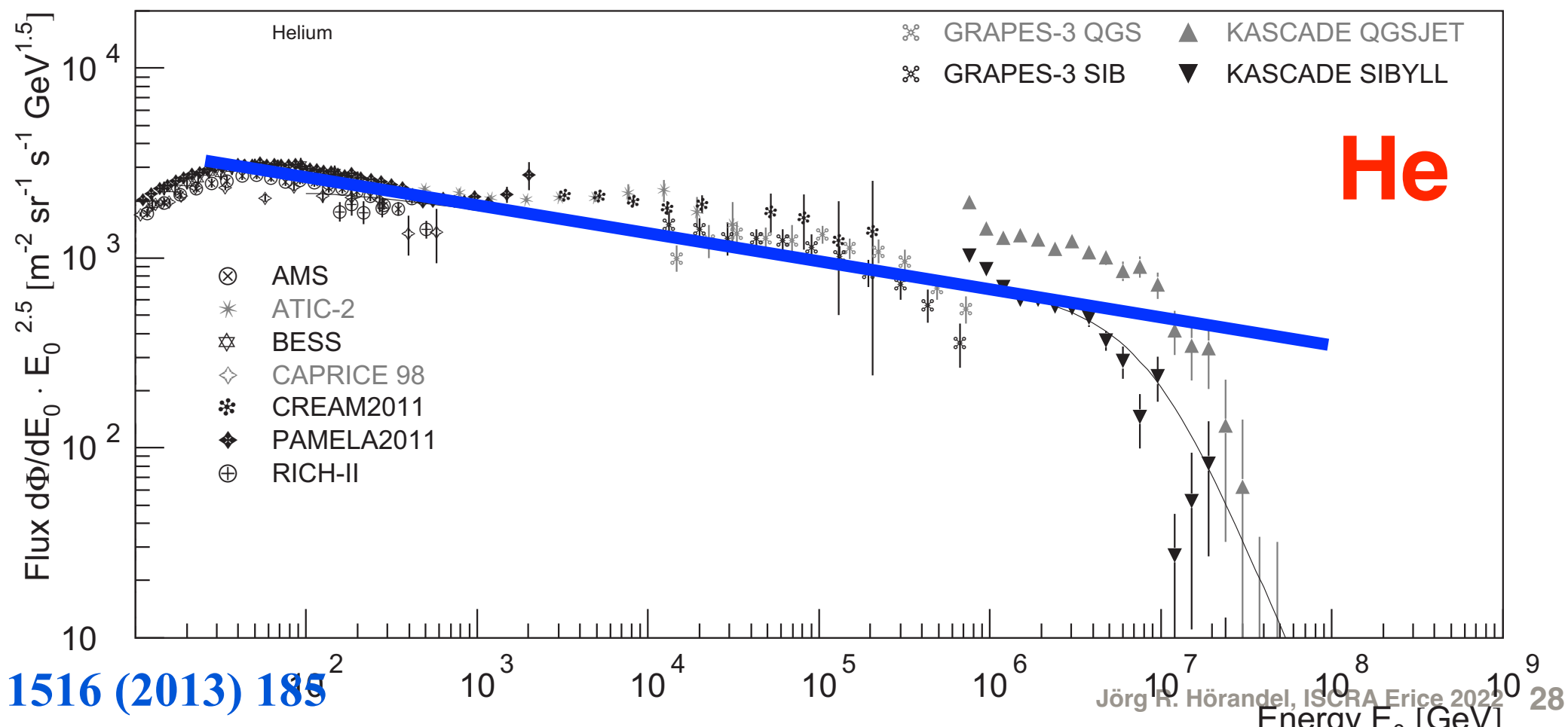
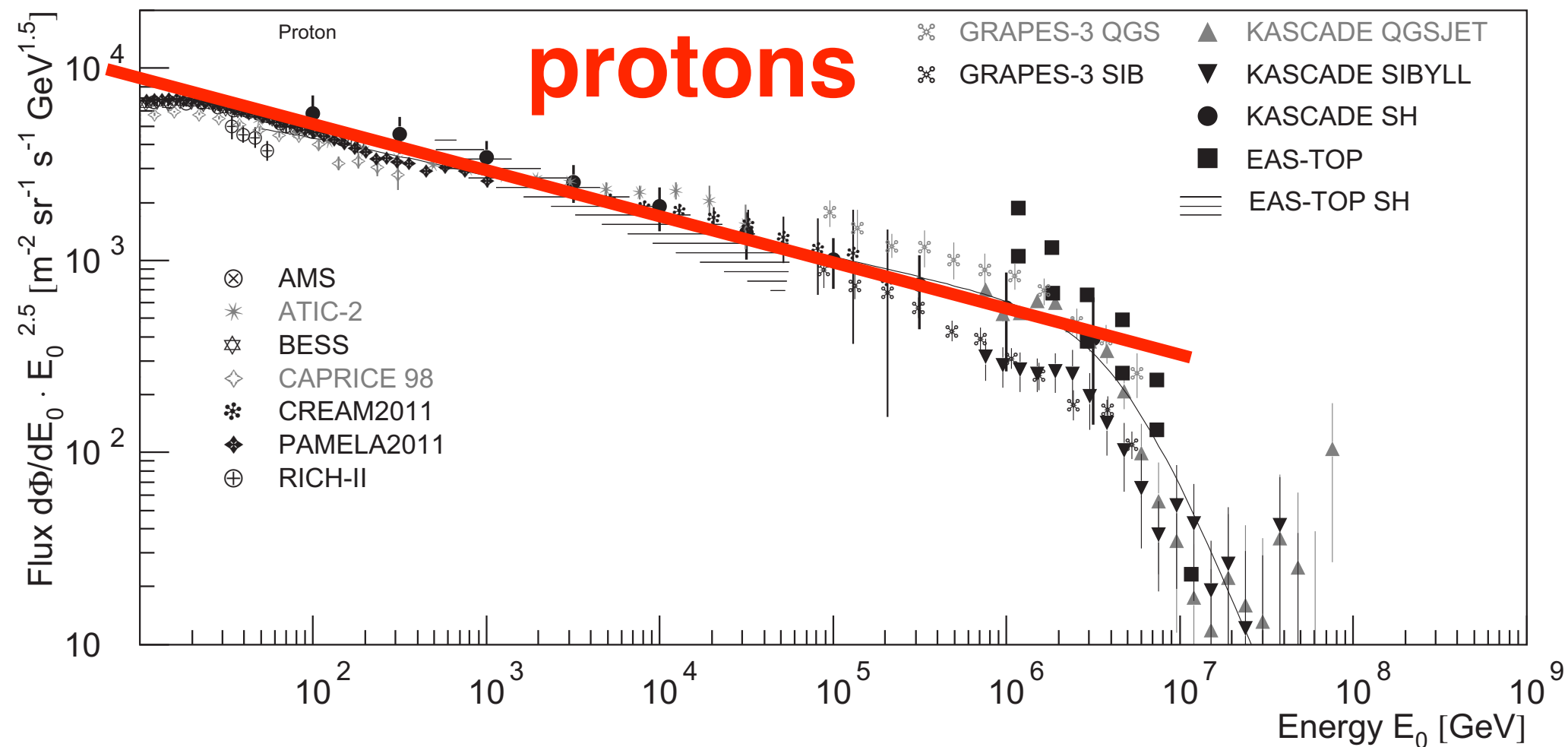
Figure 3: TALE Cosmic rays energy spectrum measured with TALE. The result is based on a QGSJet II-3 hadronic model assumption. A mixed primary composition given by the H4a, and “global fit” models, as well as a TALE derived mix was used in the calculations.

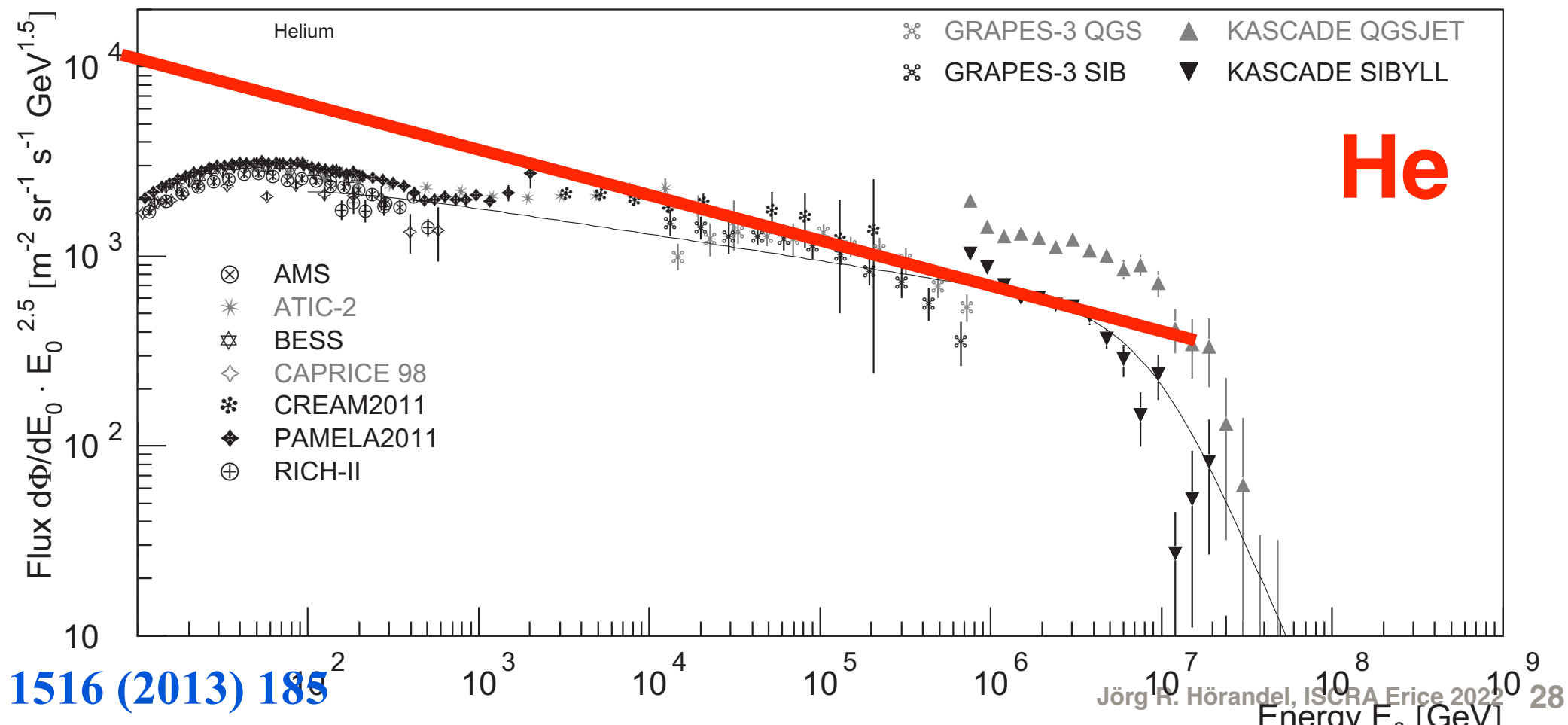
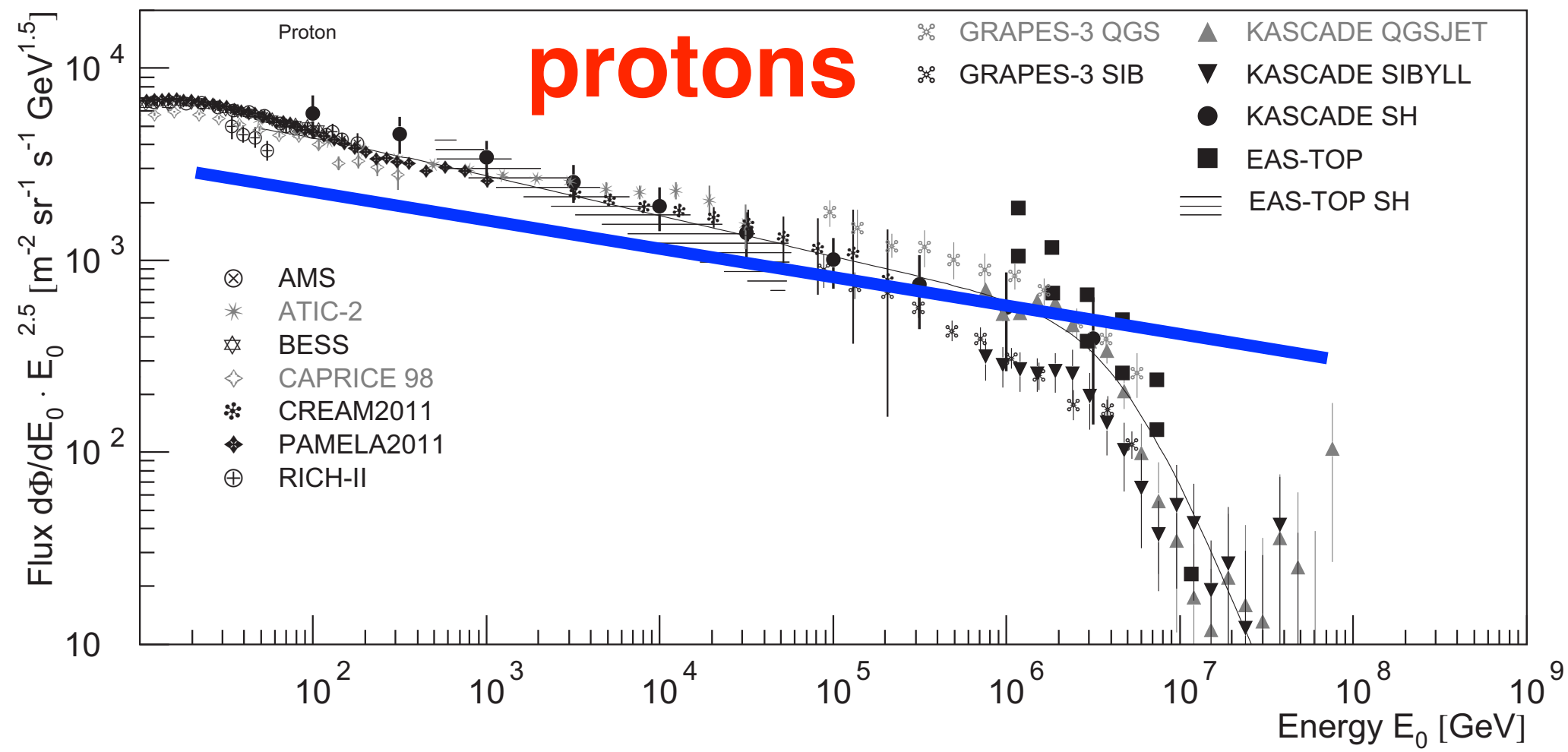


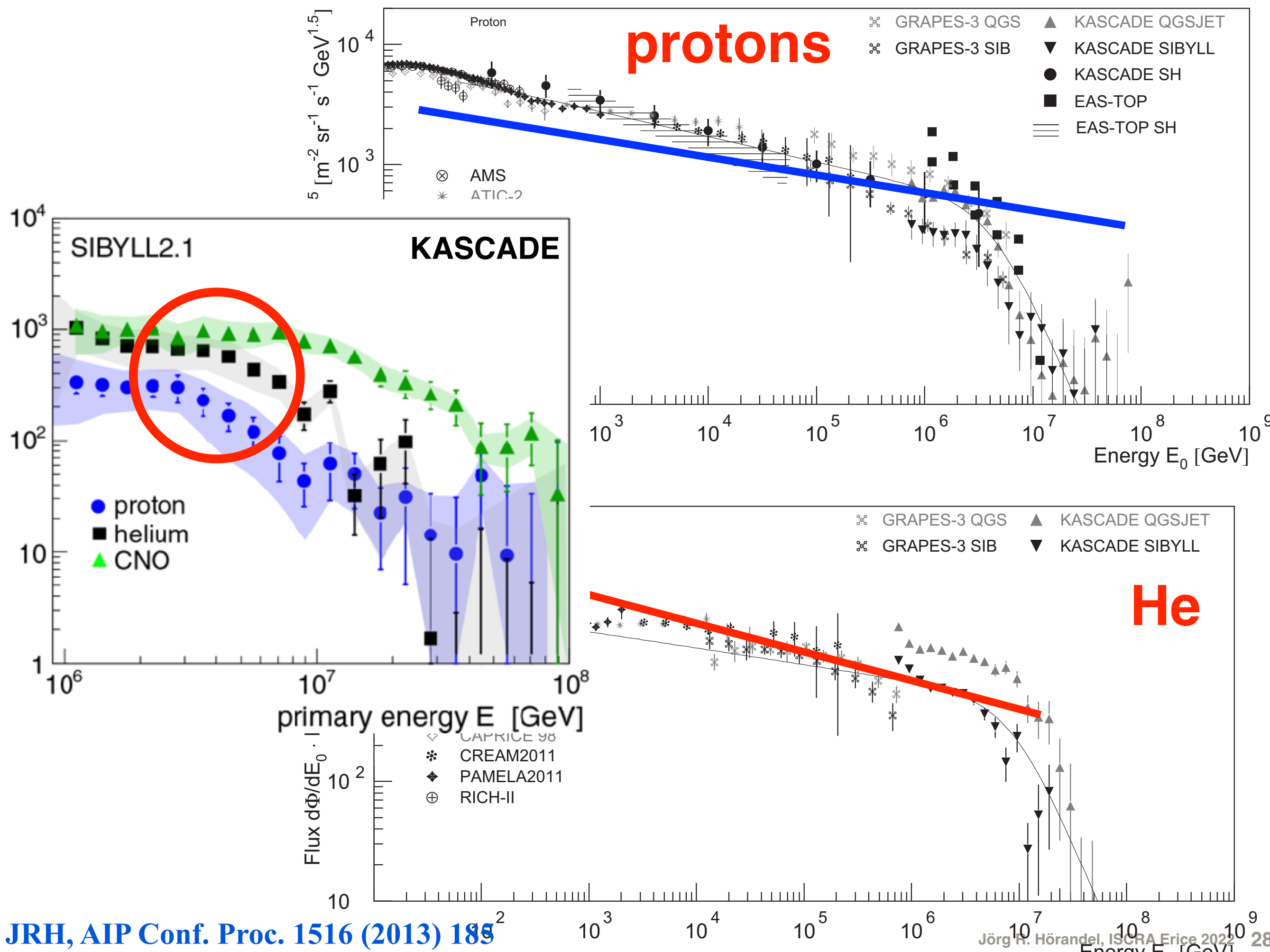


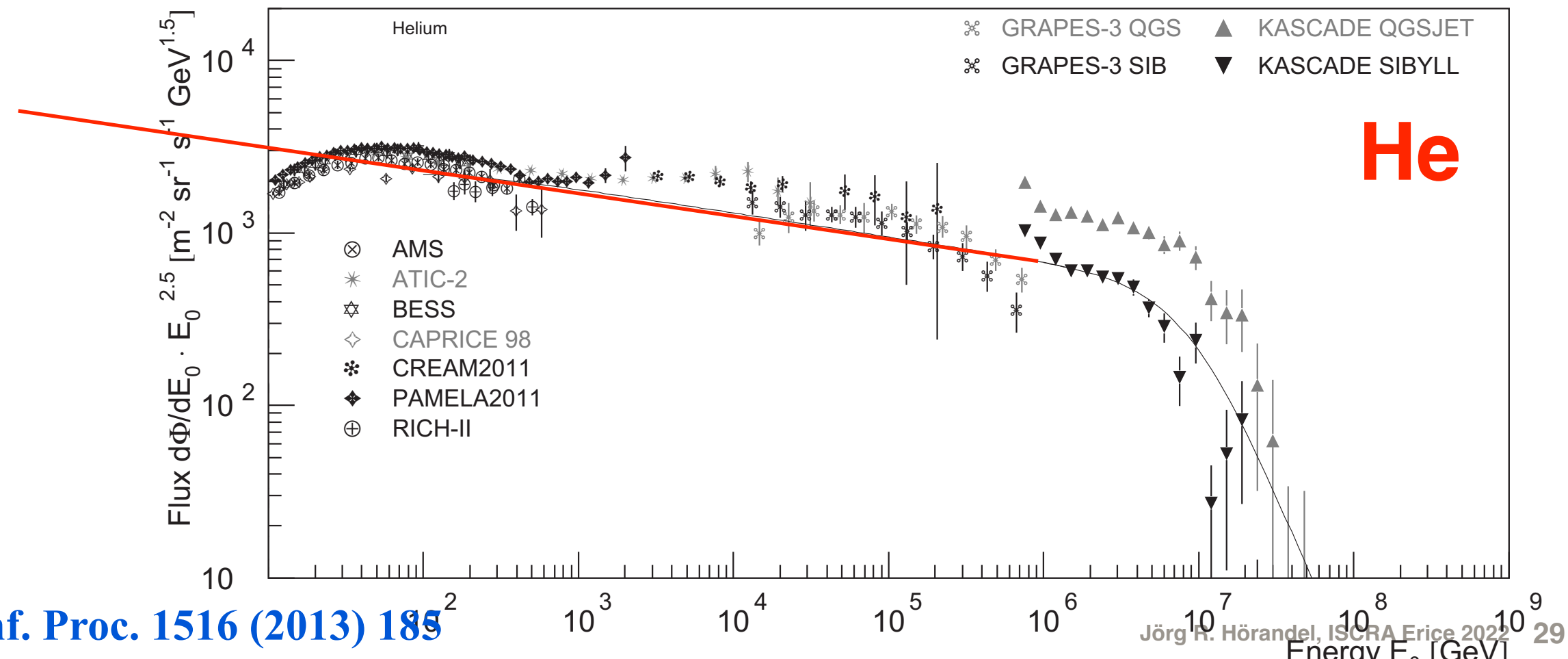
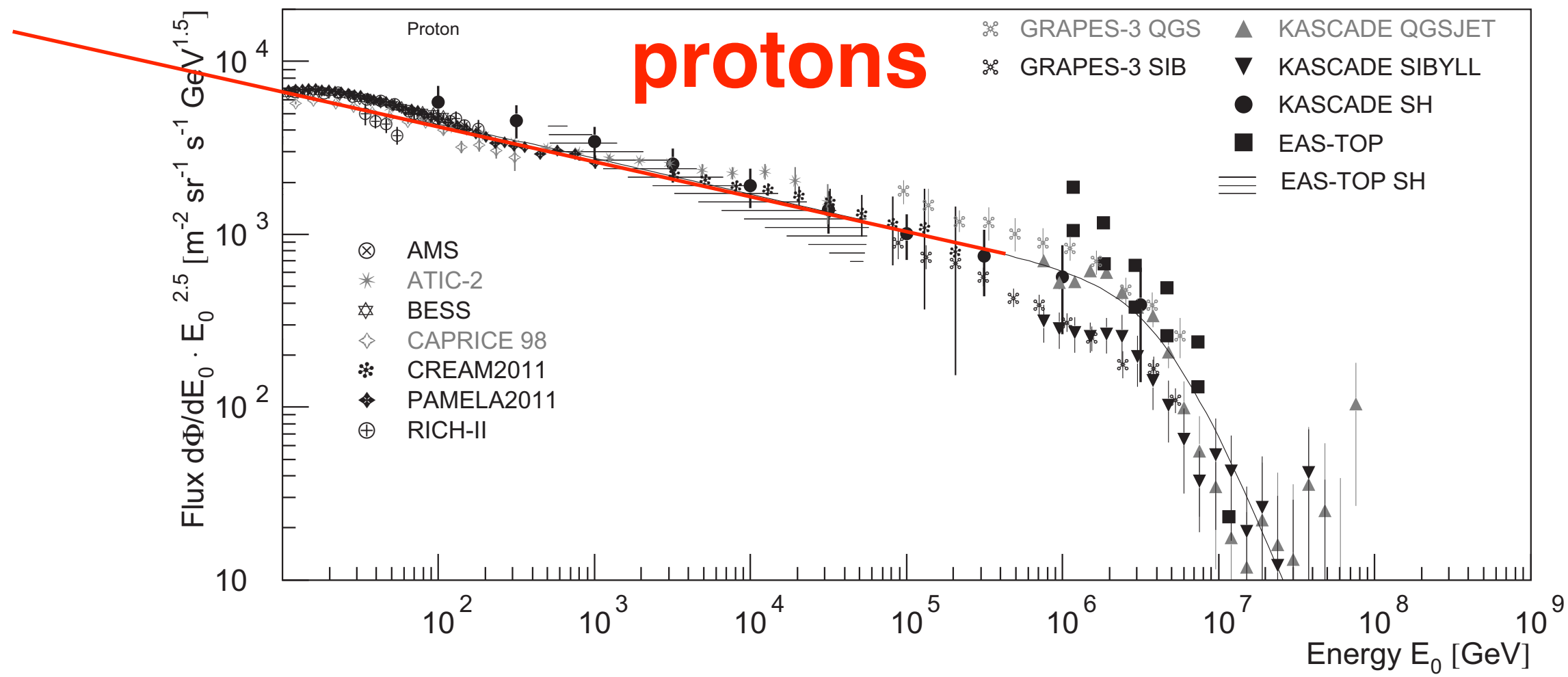


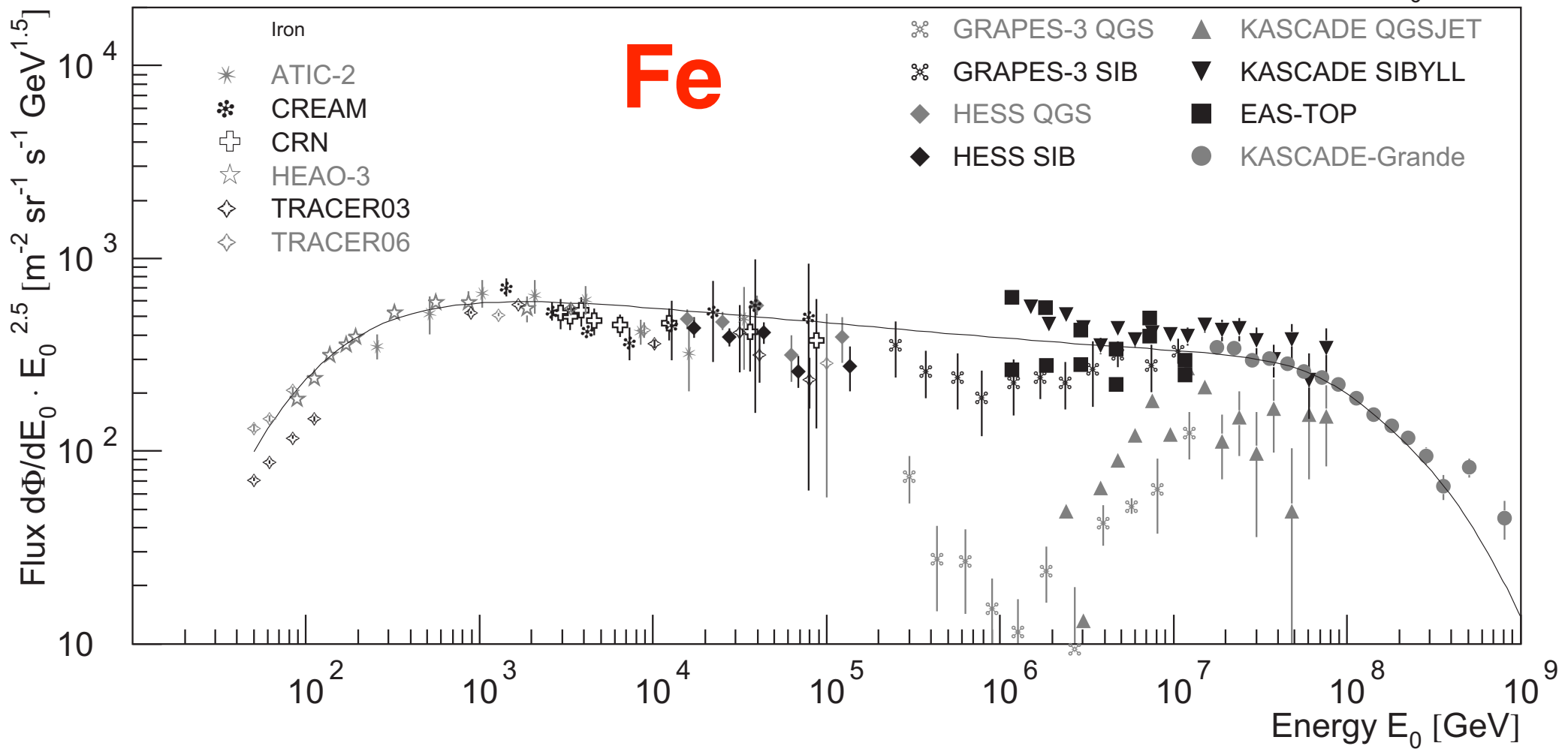
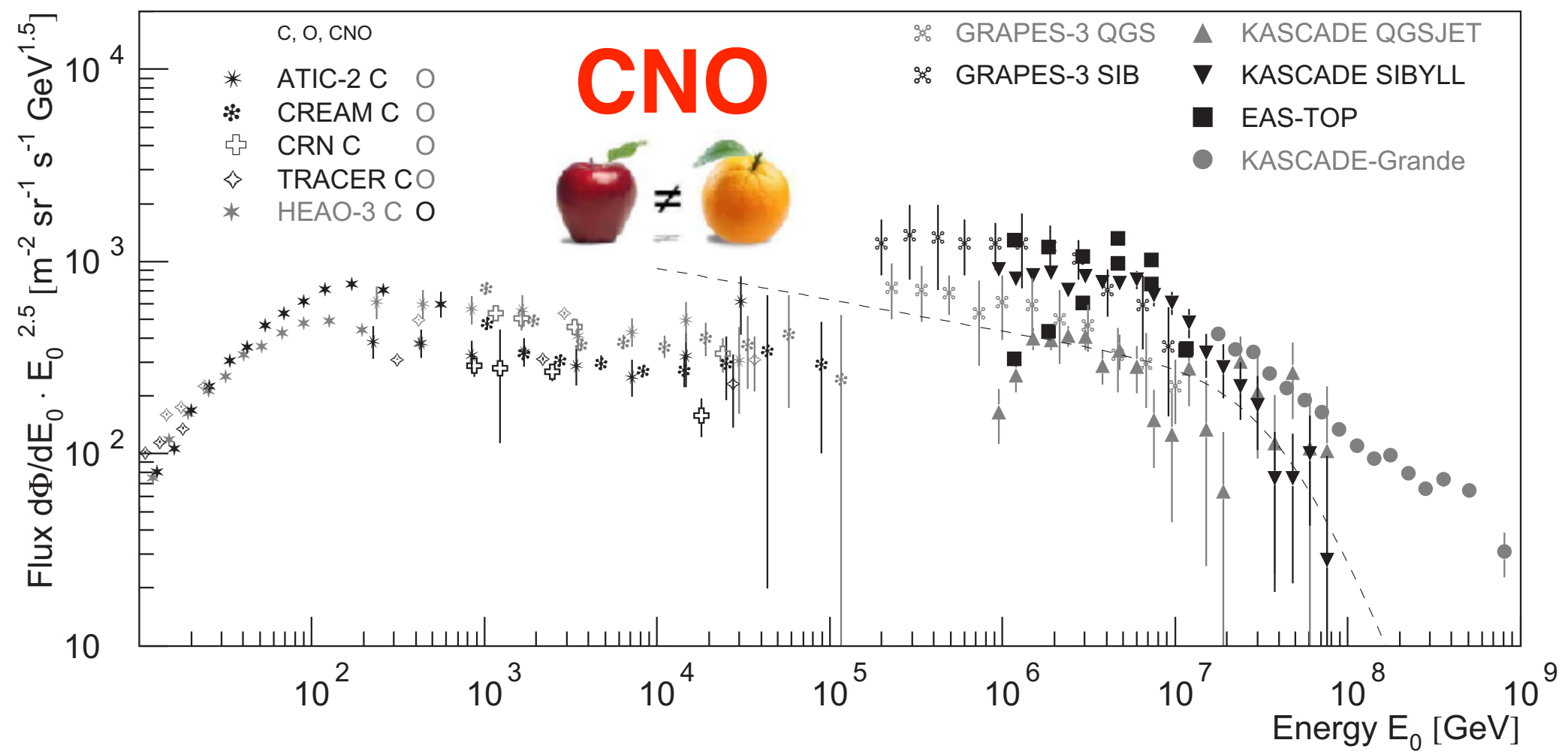


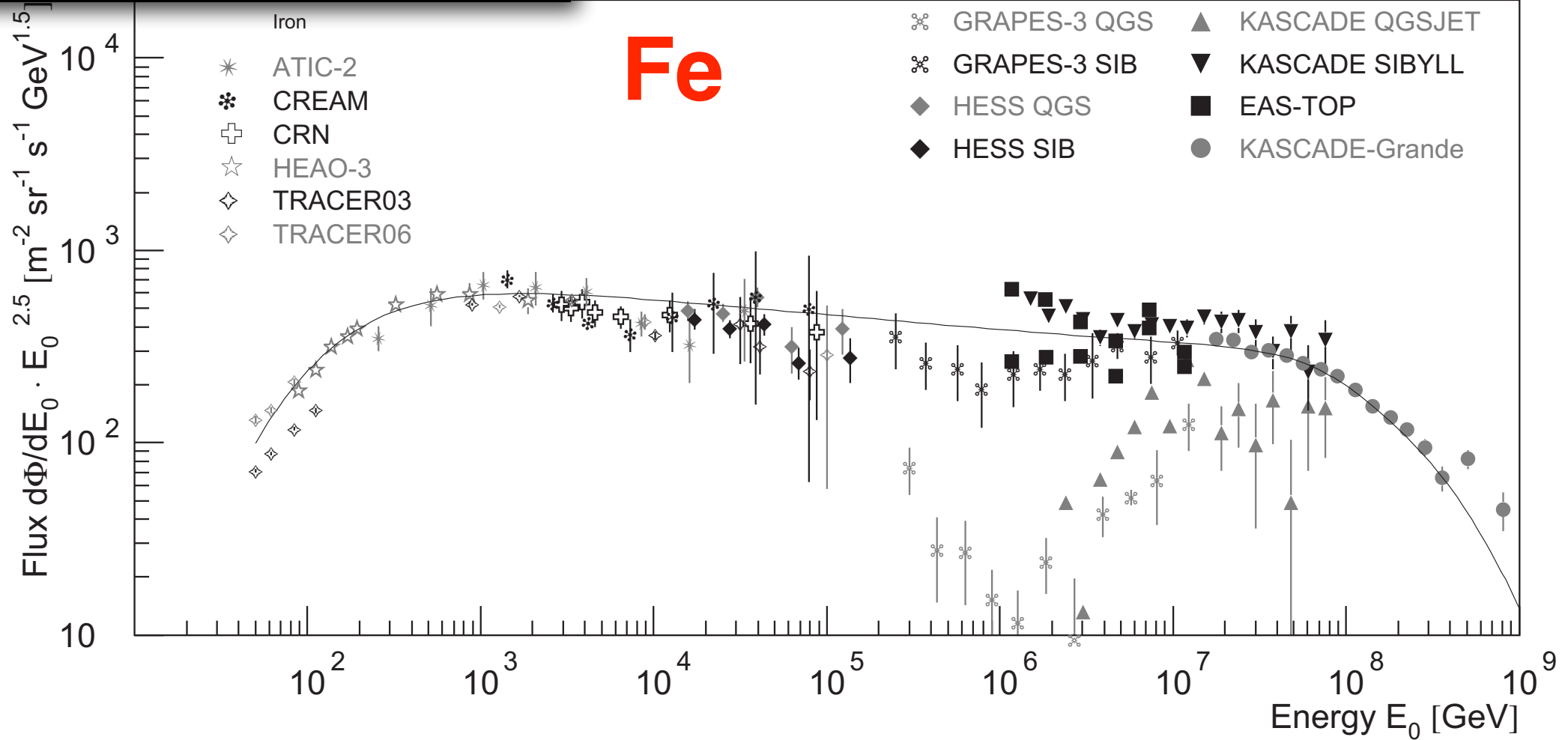
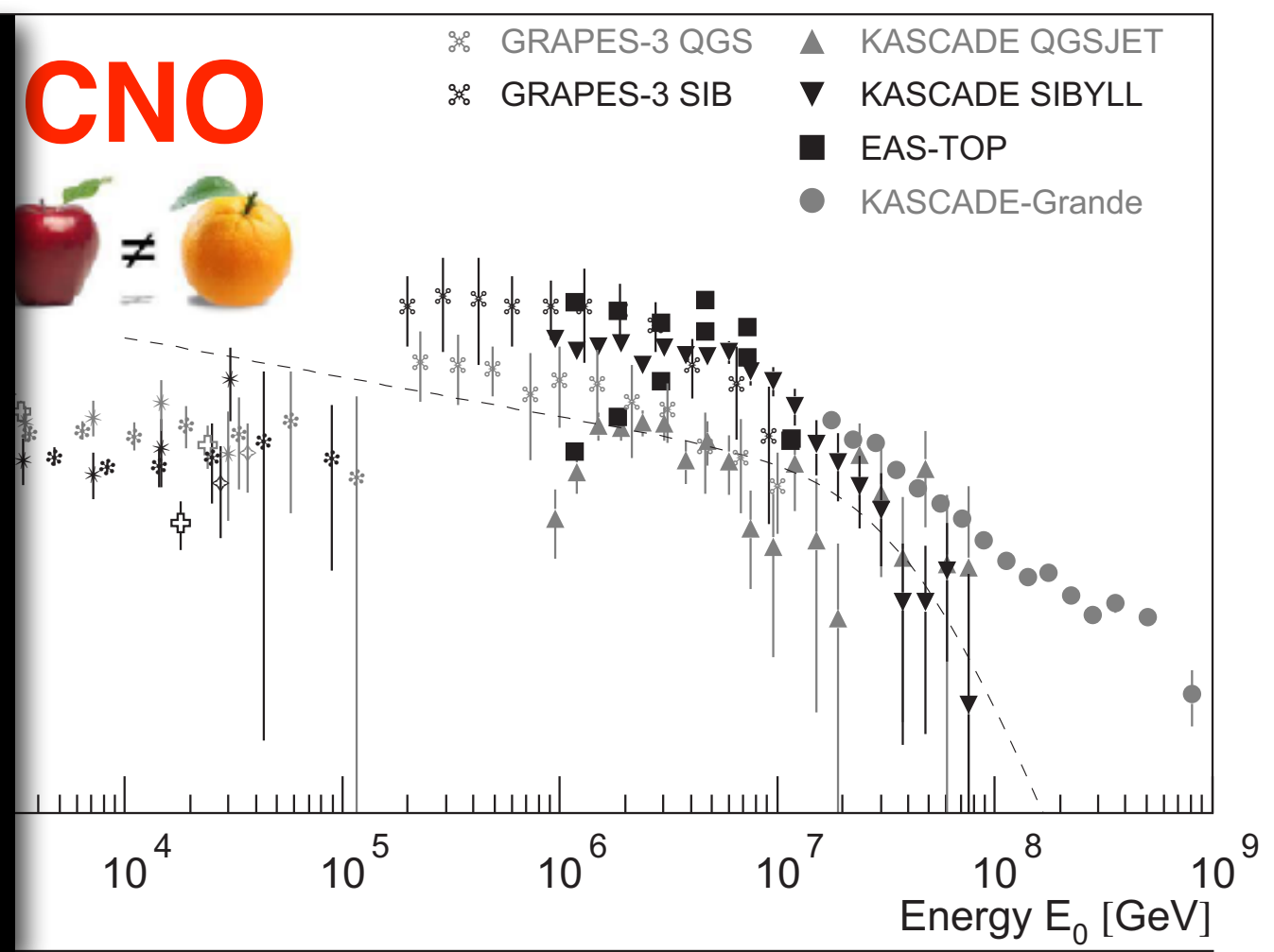
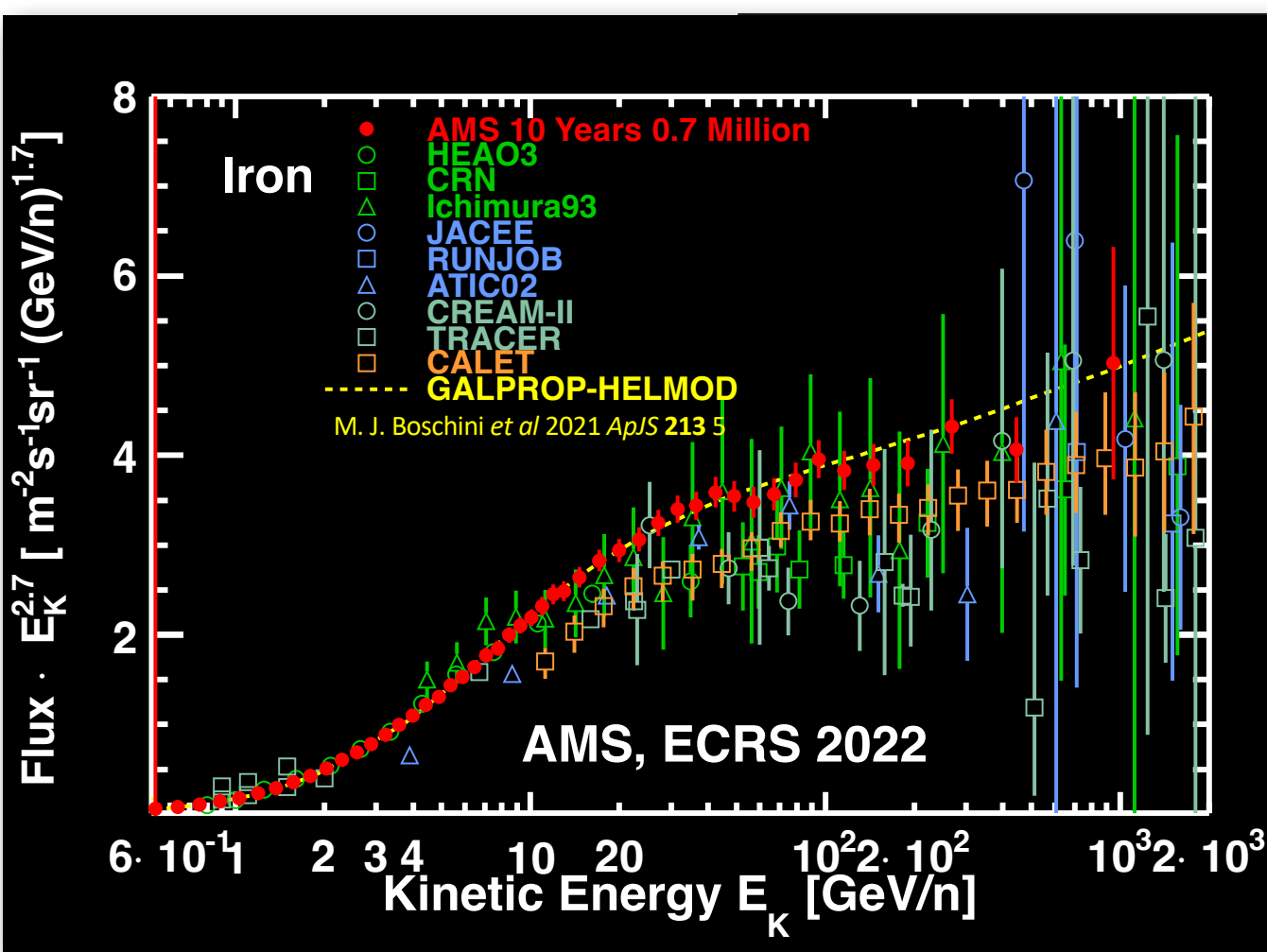






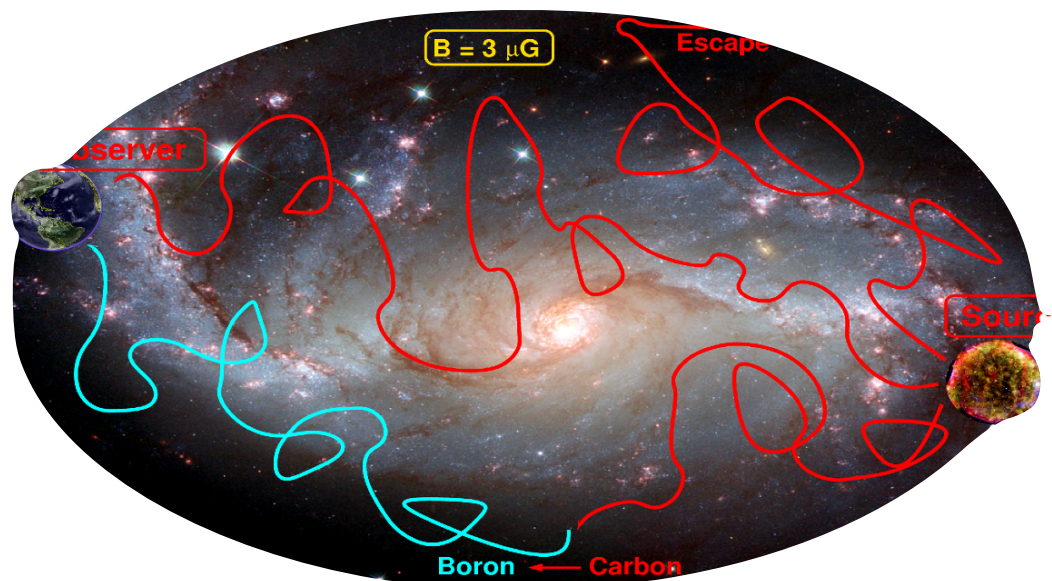






Transport equation for cosmic rays in the Galaxy

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$

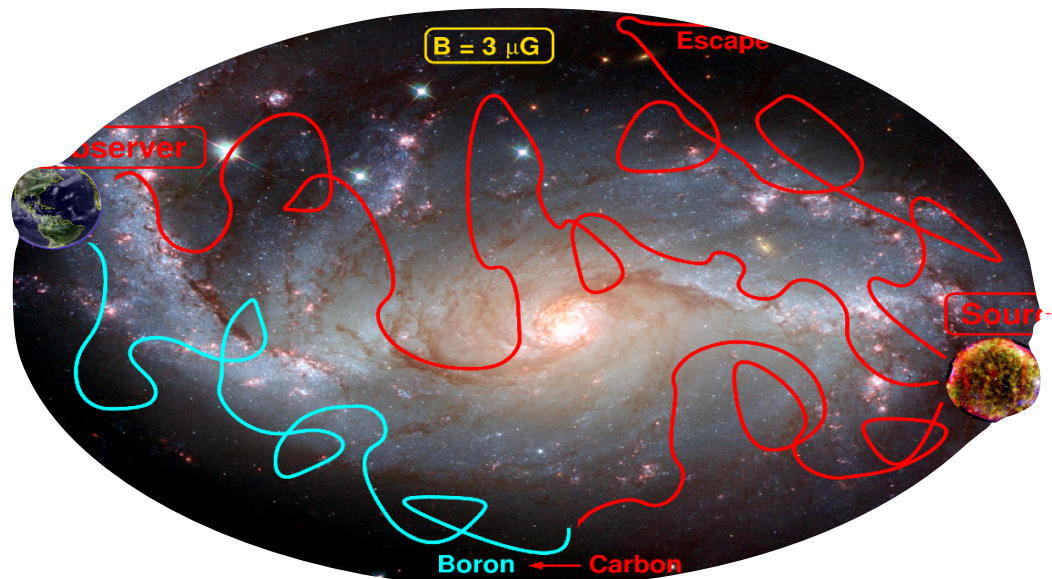


Transport equation for cosmic rays in the Galaxy

diffusion



$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$

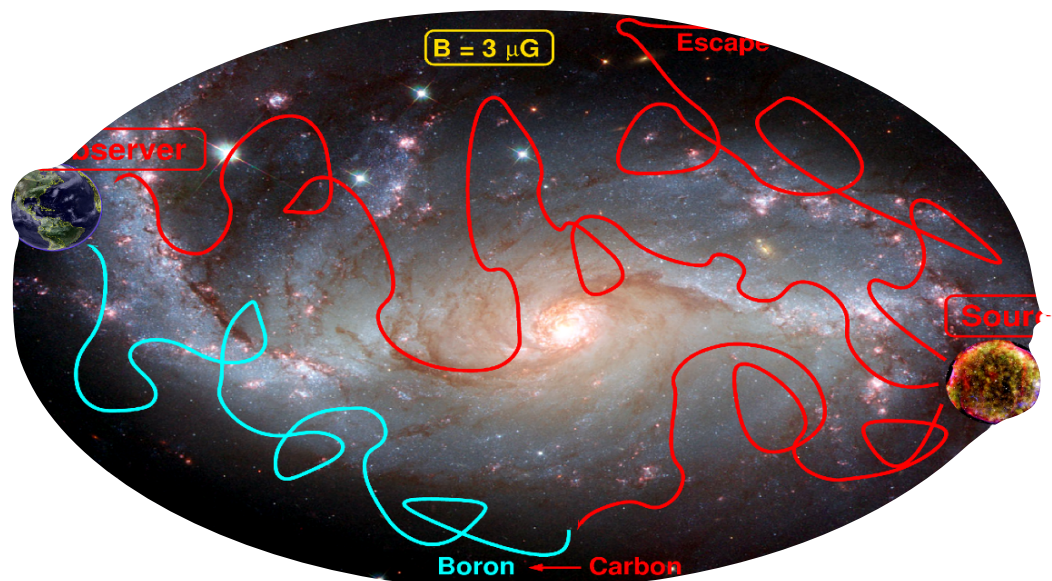


Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$



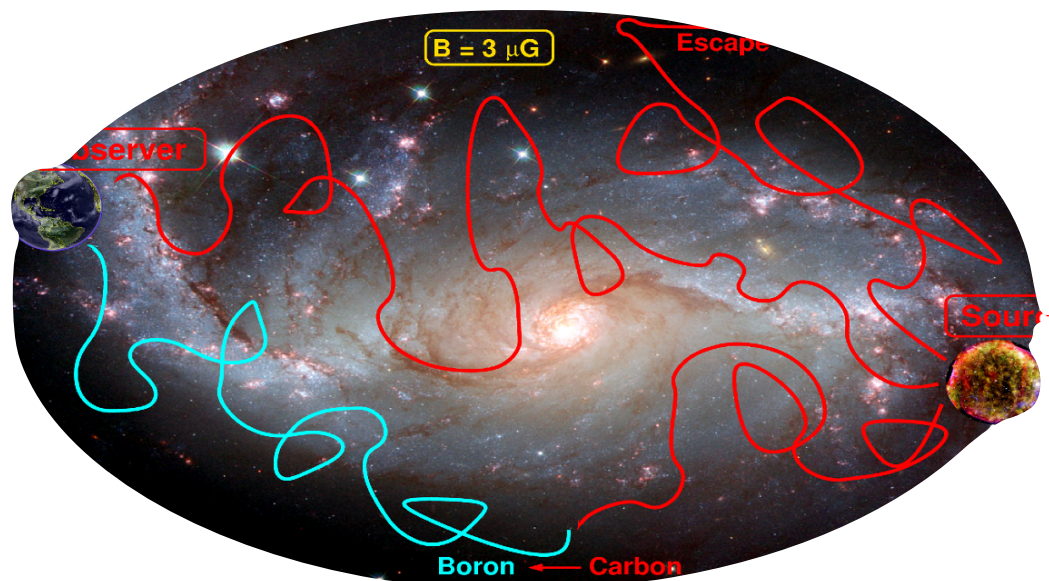
Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$



Transport equation for cosmic rays in the Galaxy

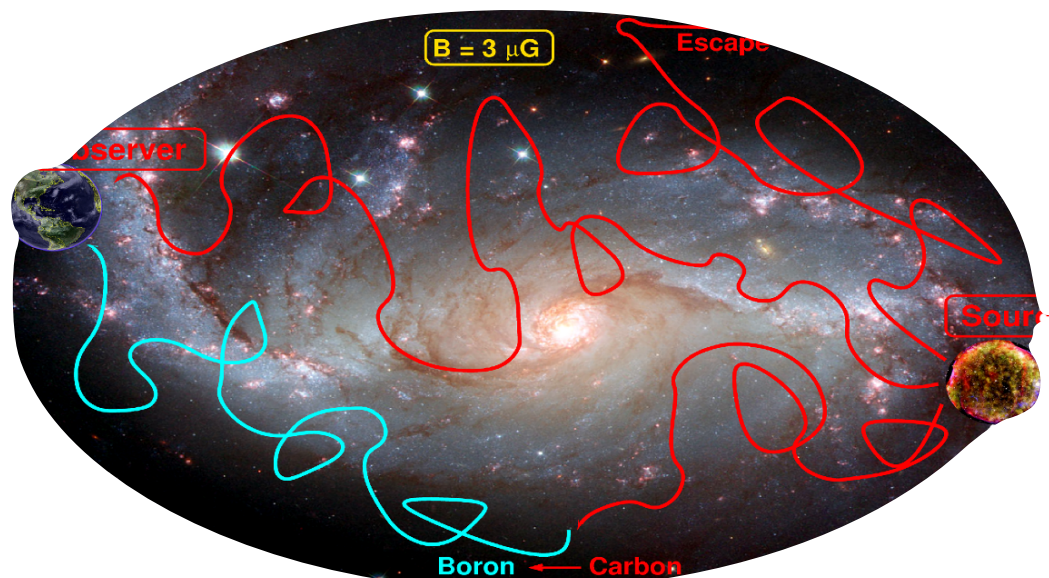
diffusion

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$



Transport equation for cosmic rays in the Galaxy

diffusion

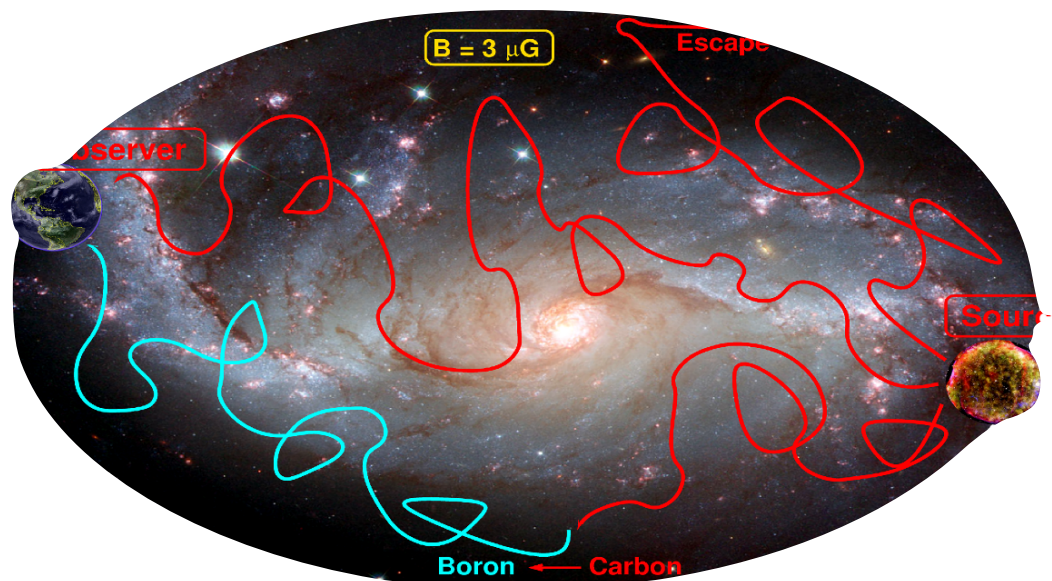
energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$

source term



Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

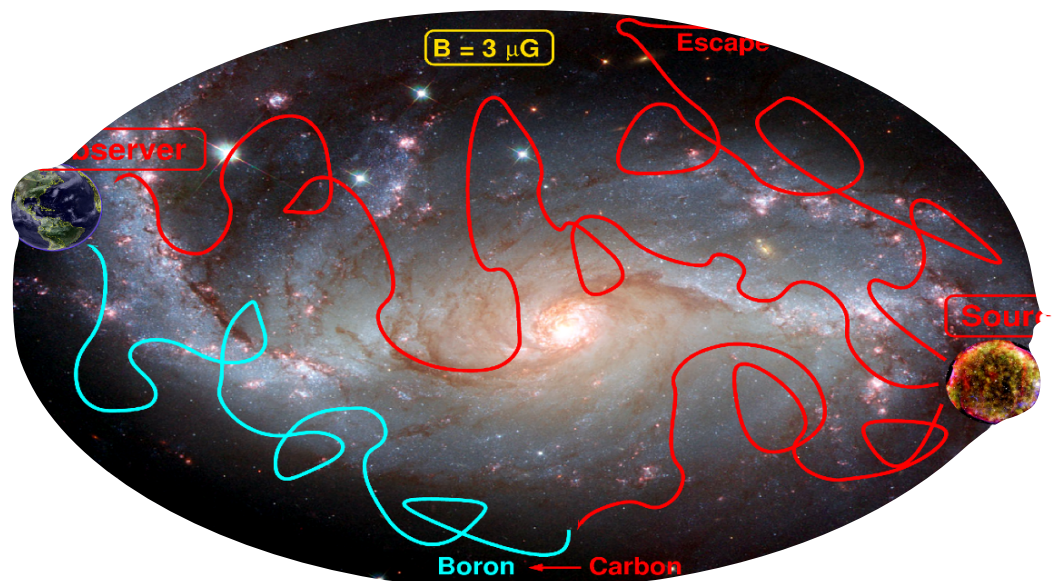
loss through interactions
with ISM (spallation)

loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n \nu \sigma_i N_i - \frac{N_i}{\gamma \tau_i} + Q_i + \sum_{j>i} n \nu \sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j \tau_{ij}}$$

source term

production through spallation
of heavy nuclei



Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

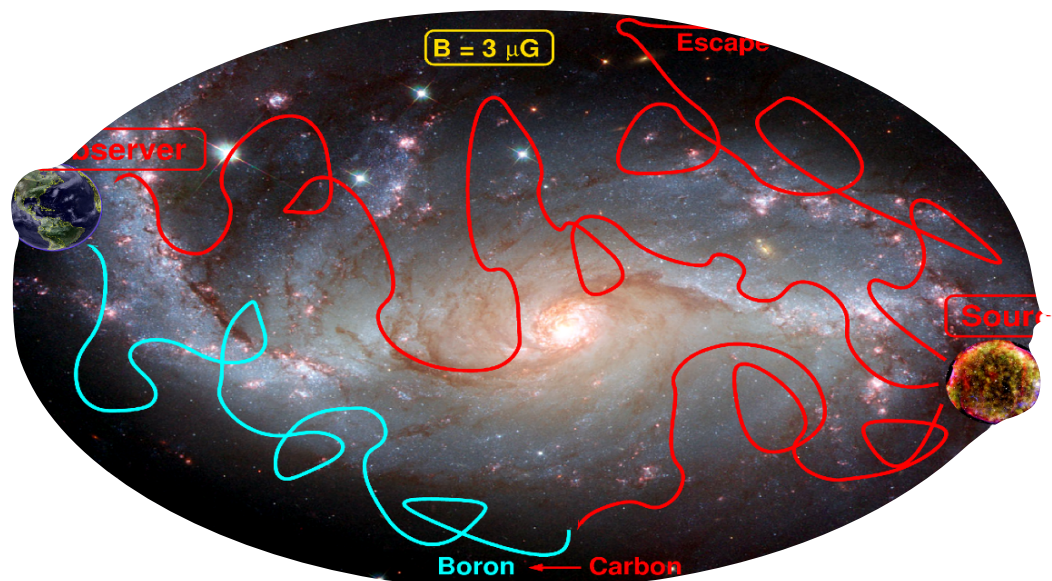
loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$

source term

production through spallation
of heavy nuclei

production through decay
of heavy nuclei

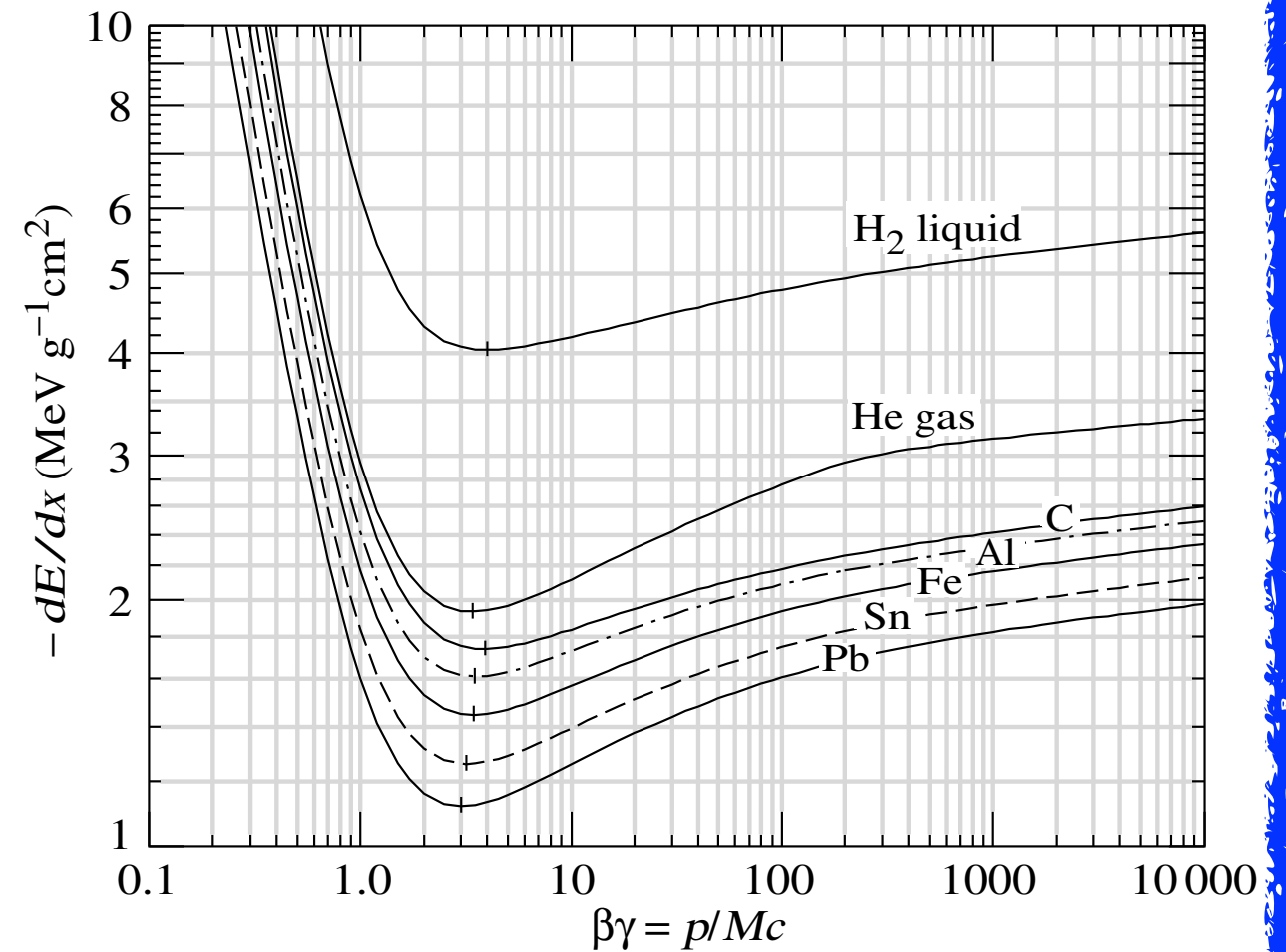


Transport equation for Galactic Cosmic Rays

diffusion

energy loss (Bethe Bloch)

loss through with

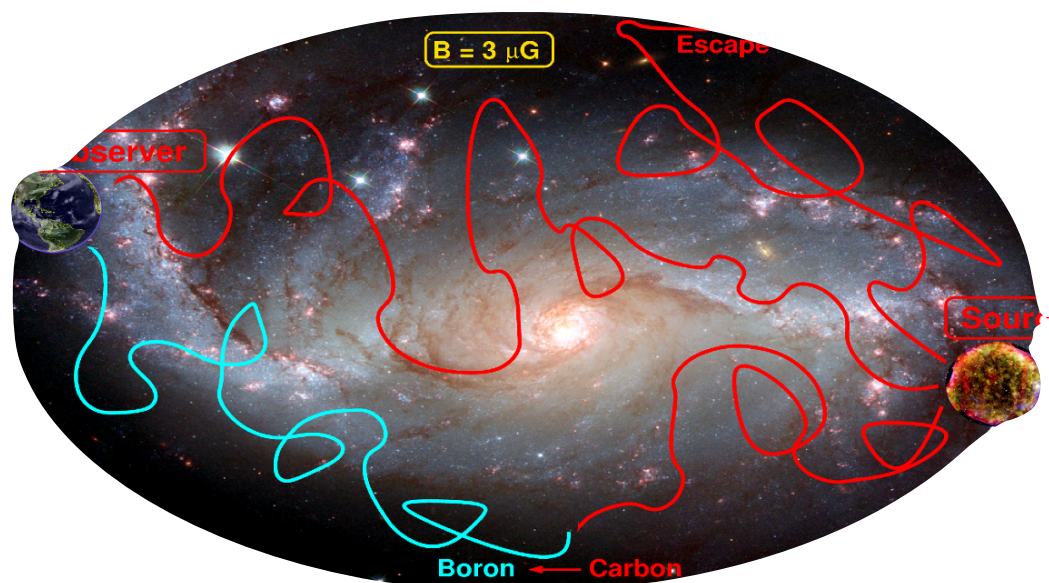


$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E} (E N_i) - n \nu \sigma_i N_i - \frac{N_i}{\gamma \tau_i} + Q_i + \sum_{j>i} n \nu \sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j \tau_{ij}}$$

source term

production through spallation of heavy nuclei

production through decay of heavy nuclei



Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

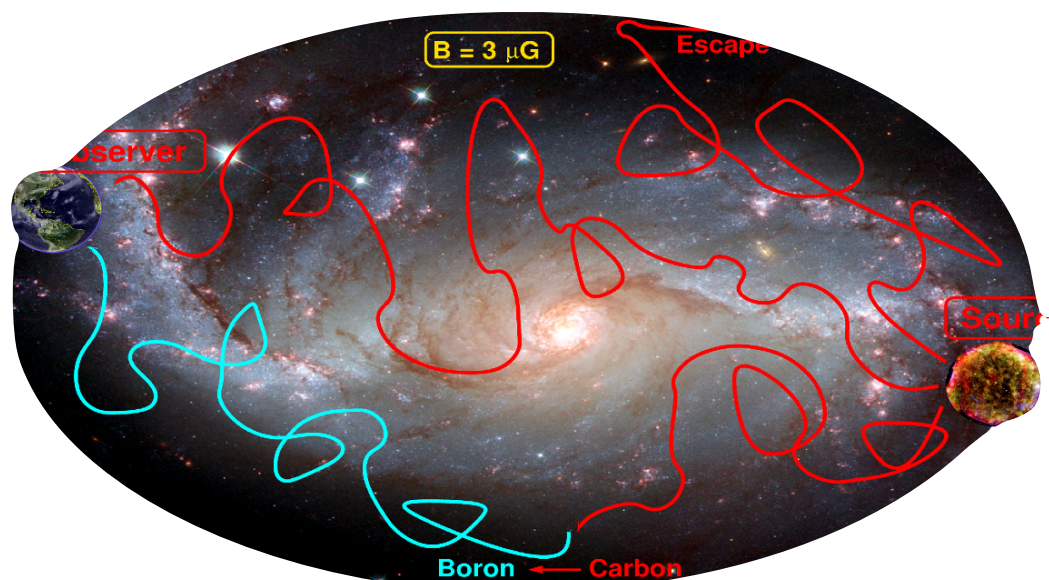
loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E} (E N_i) - n \nu \sigma_i N_i - \frac{N_i}{\gamma \tau_i} + Q_i + \sum_{j>i} n \nu \sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j \tau_{ij}}$$

source term

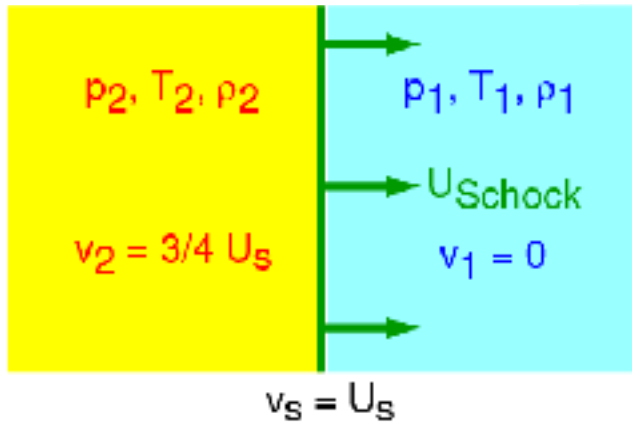
production through spallation
of heavy nuclei

production through decay
of heavy nuclei

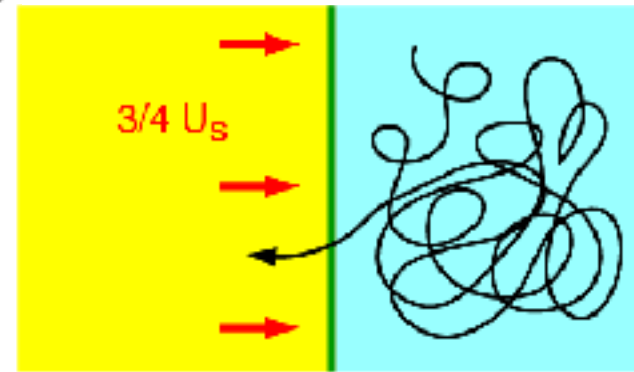


1st order Fermi acceleration at strong shock

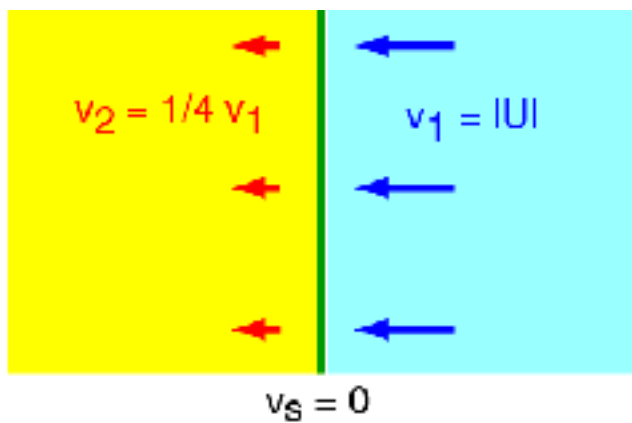
a) rest system of unshocked ISM



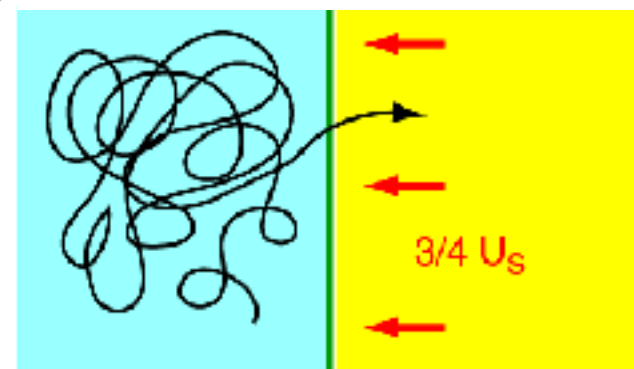
b) rest system of unshocked ISM



c) rest system of shock front

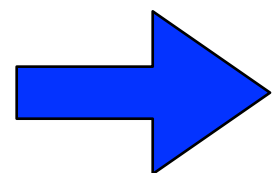


d) rest system of shocked ISM



energy gain

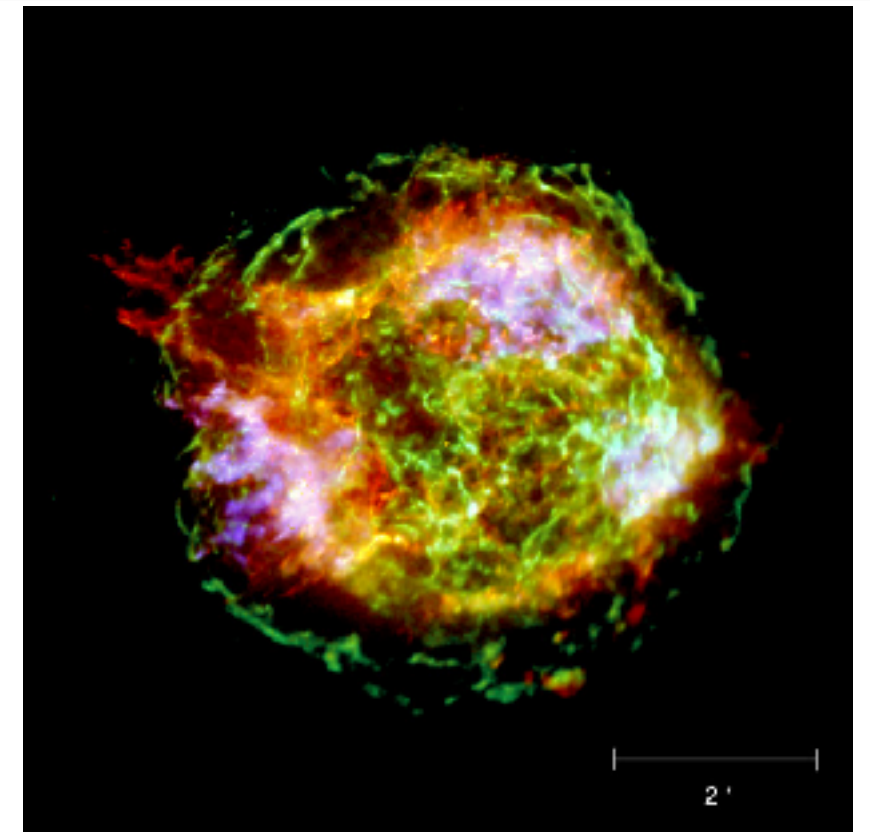
$$\frac{\Delta E}{E} \propto \frac{U_s}{c}$$



$$N(E) dE \propto E^{-2} dE$$

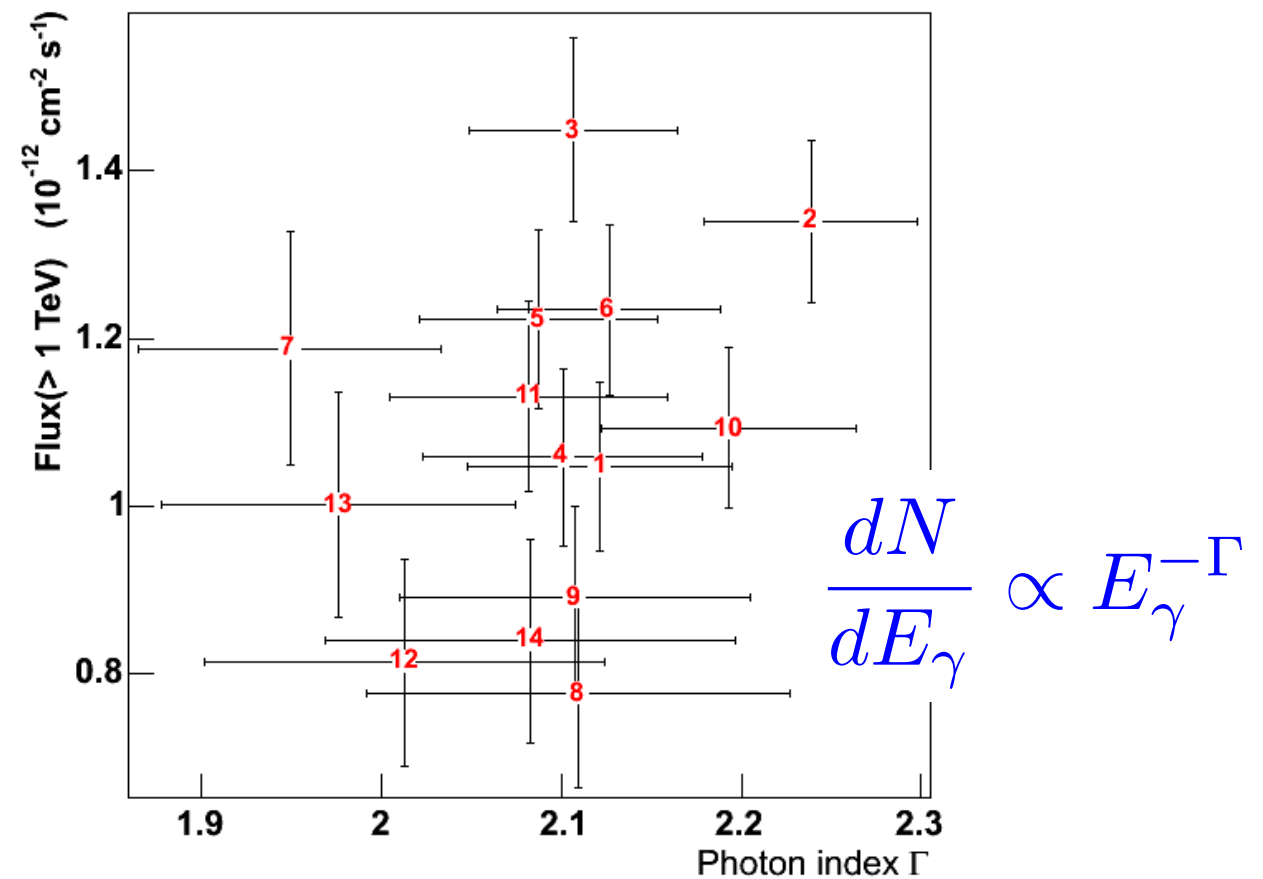
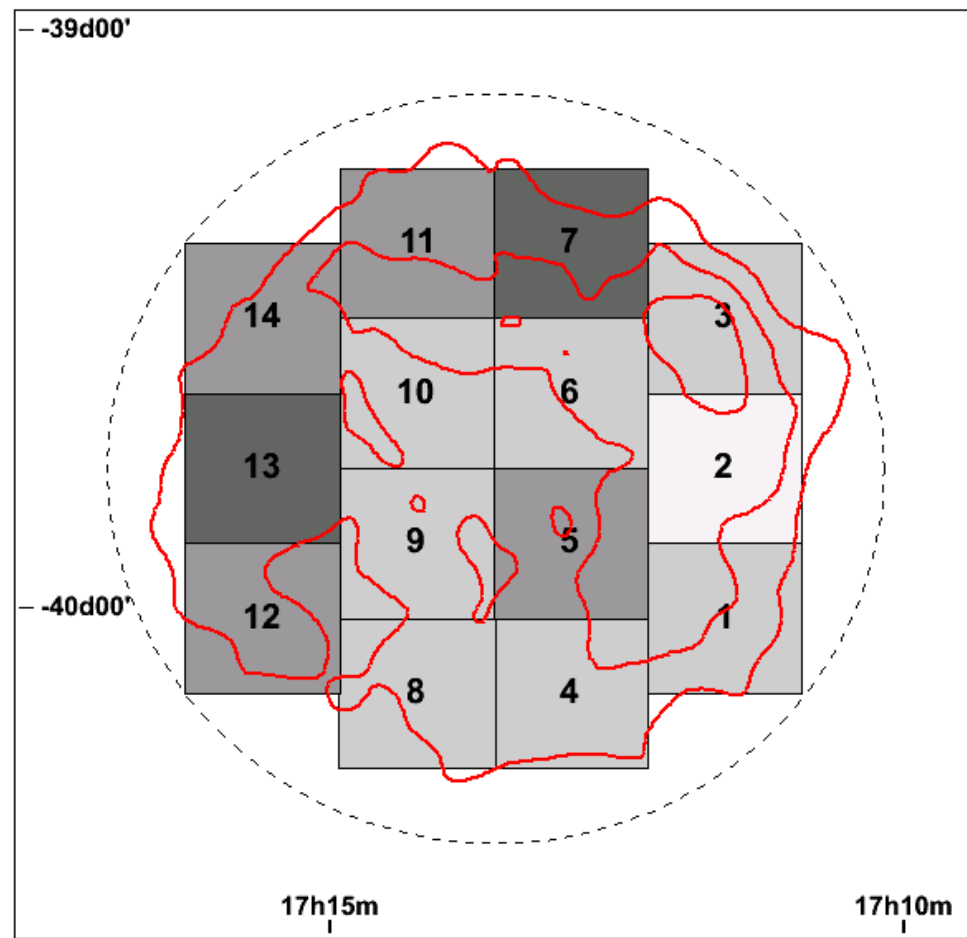
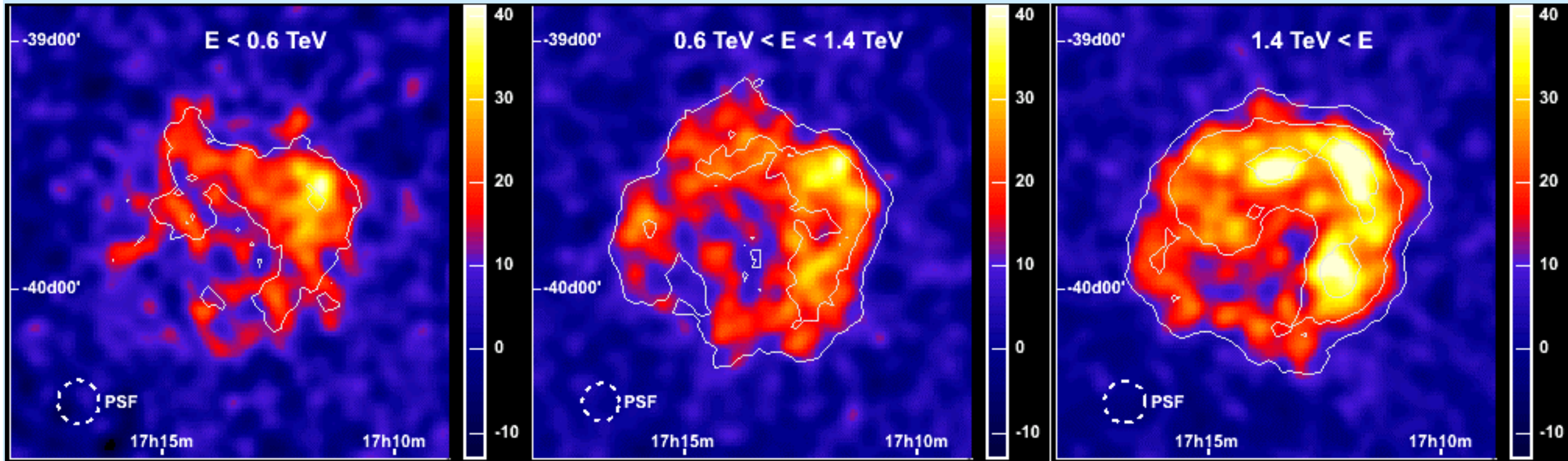
power law with spectral index
-2.0 ... -2.1

Bell, Blanford, Ostriker (1978)



Supernova remnant (SNR)
Cassiopeia A

H.E.S.S. supernova remnant RXJ 1713



Acceleration of cosmic rays at SNR

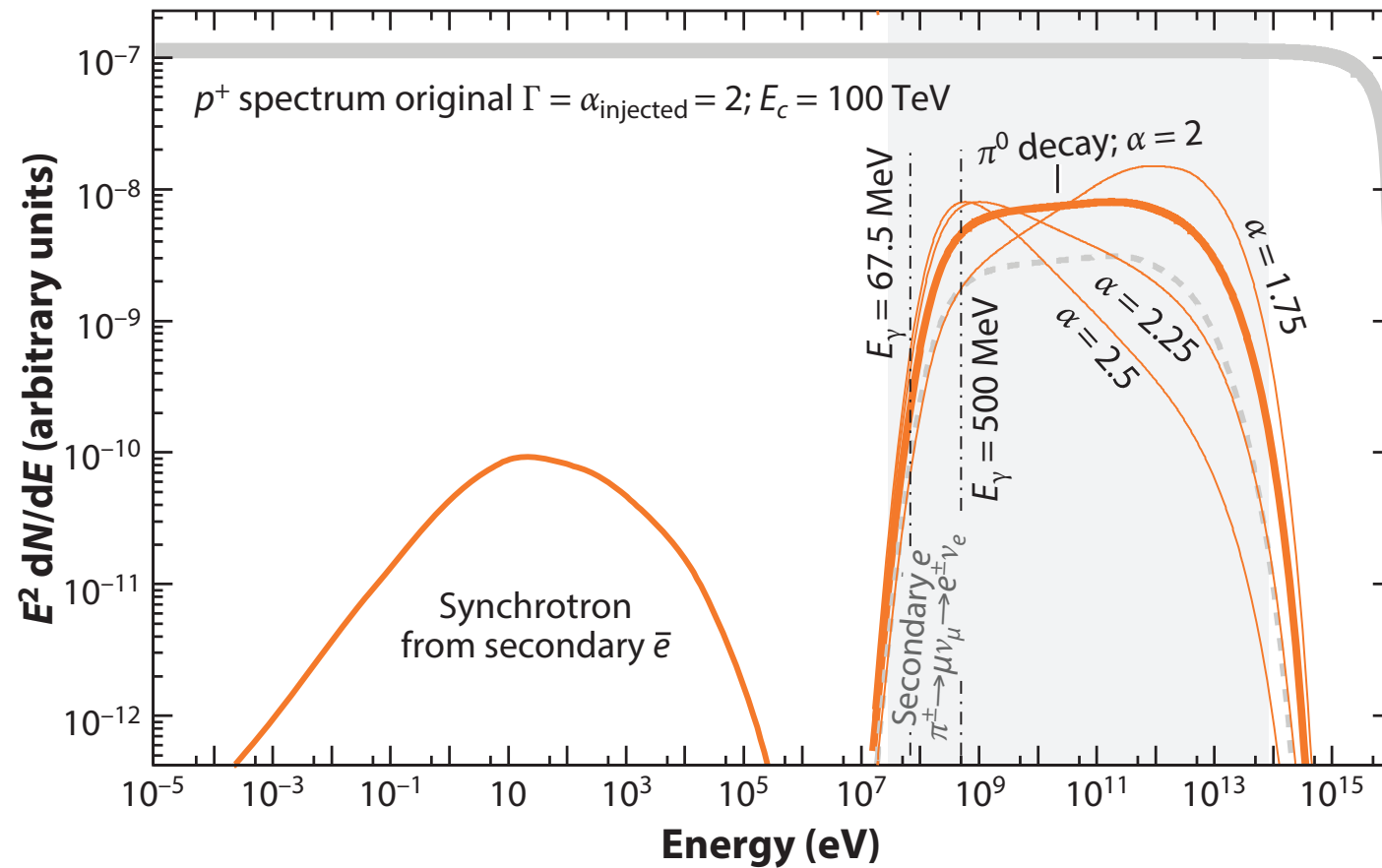


Figure 3

Spectral energy distribution of accelerated protons (power-law index $\alpha_{\text{injected}} = 2.0$ and cutoff at 100 TeV) and γ -rays resulting from inelastic collisions with interstellar material. The dominant emission into photons occurs via the decay $\pi^0 \rightarrow \gamma\gamma$ (solid orange curves). The γ -ray spectrum follows the parent protons' spectrum rather closely in the midenergy range and in the high-energy cutoff region. For all proton indices, the low-energy turnover is a characteristic feature of the pion-decay emission. Also shown is the spectrum of electrons resulting from the inelastic proton-proton interactions via the decay chain $\pi^\pm \rightarrow \mu + \nu_\mu \rightarrow e^\pm \nu_e$ (dashed gray curve). For the synchrotron emission from these so-called secondary electrons, a source with age $t_{\text{age}} = 1,000$ years and $B = 30 \mu\text{G}$ have been assumed. The shaded gray region shows the sensitive range of current γ -ray detectors (*Fermi*-LAT, imaging atmospheric Cherenkov detectors).

The emissivity can be turned into a flux at Earth by an astrophysical accelerator that puts a fraction ϵ_{CR} of its energy output E_{pr} into the acceleration of protons:

$$F_\gamma(>100 \text{ MeV}) = 4.4 \times 10^{-7} \epsilon_{\text{CR}} \frac{E_{\text{pr}}}{10^{51} \text{ erg kpc}} \frac{d^{-2}}{1 \text{ cm}^{-3}} \text{ cm}^{-2} \text{ s}^{-1}. \quad 3.$$

In other words, if the distance d and the density of the interaction region n are known, the amount of energy in protons E_{pr} at the interaction site can be directly inferred from the γ -ray flux F_γ .

Acceleration of cosmic rays at SNR

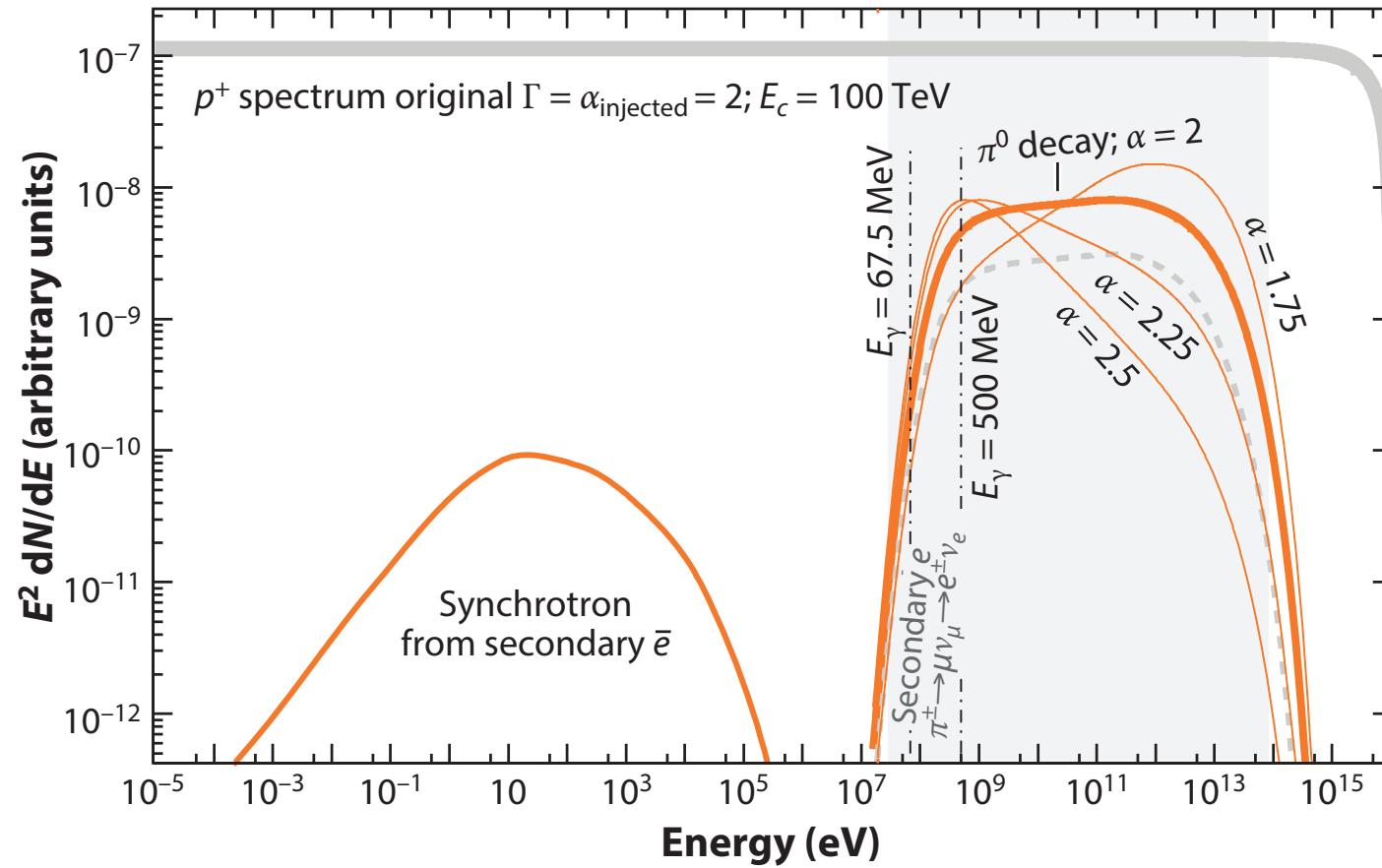


Figure 3

Spectral energy distribution of accelerated protons (power-law index $\alpha_{\text{injected}} = 2.0$ and cutoff at 100 TeV) and γ -rays resulting from inelastic collisions with interstellar material. The dominant emission into photons occurs via the decay $\pi^0 \rightarrow \gamma\gamma$ (solid orange curves). The γ -ray spectrum follows the parent protons' spectrum rather closely in the midenergy range and in the high-energy cutoff region. For all proton indices, the low-energy turnover is a characteristic feature of the pion-decay emission. Also shown is the spectrum of electrons resulting from the inelastic proton-proton interactions via the decay chain $\pi^\pm \rightarrow \mu + \nu_\mu \rightarrow e^\pm \nu_e$ (dashed gray curve). For the synchrotron emission from these so-called secondary electrons, a source with age $t_{\text{age}} = 1,000$ years and $B = 30 \mu\text{G}$ have been assumed. The shaded gray region shows the sensitive range of current γ -ray detectors (*Fermi*-LAT, imaging atmospheric Cherenkov detectors).

The emissivity can be turned into a flux at Earth by an astrophysical accelerator that puts a fraction ϵ_{CR} of its energy output E_{pr} into the acceleration of protons:

$$F_\gamma(>100 \text{ MeV}) = 4.4 \times 10^{-7} \epsilon_{\text{CR}} \frac{E_{\text{pr}}}{10^{51} \text{ erg kpc}} \frac{d^{-2}}{1 \text{ cm}^{-3}} \frac{n}{\text{cm}^{-3}} \text{ cm}^{-2} \text{ s}^{-1}. \quad 3.$$

In other words, if the distance d and the density of the interaction region n are known, the amount of energy in protons E_{pr} at the interaction site can be directly inferred from the γ -ray flux F_γ .

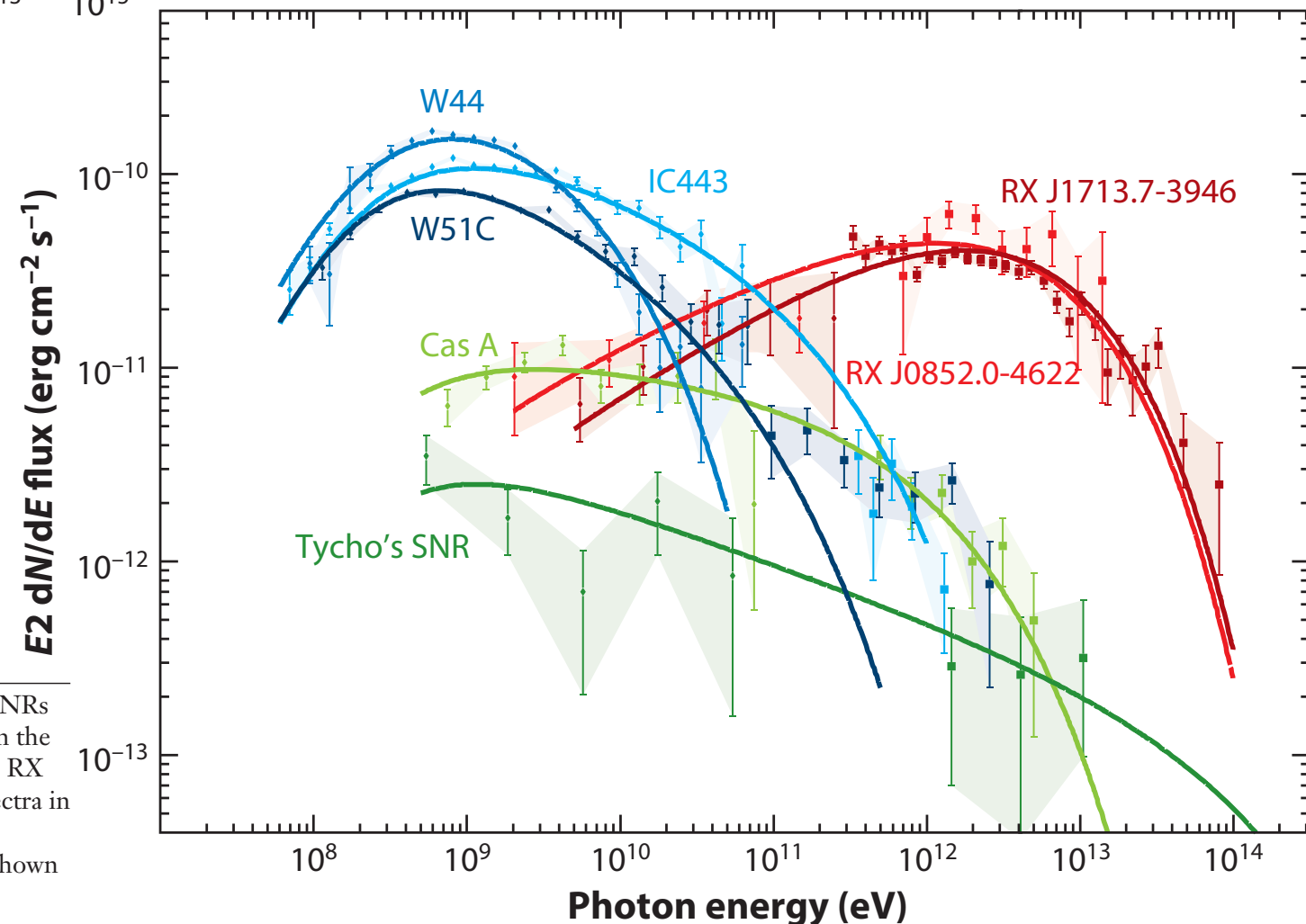


Figure 6

Typical γ -ray energy spectra for several of the most prominent supernova remnants (SNRs). Young SNRs ($<1,000$ years) are shown in green. These typically show smaller γ -ray fluxes but rather hard spectra in the GeV and TeV bands. The older (but still referred to as young) shell-type SNRs RX J1713.7-3946 and RX J0852.0-4622 (Vela Junior) of ages $\sim 2,000$ years are shown in shades of red. These show very hard spectra in the GeV band ($\Gamma = 1.5$) and a peak in the TeV band with an exponential cutoff beyond 10 TeV. The middle-aged SNRs ($\sim 20,000$ years) interacting with molecular clouds (W44, W51C, and IC443) are shown in blue. Also shown are hadronic fits to the data (solid lines).

Ultrahigh-energy photons up to 1.4 petaelectronvolts from 12 γ -ray Galactic sources

see Goodmann, ISGRA 2022

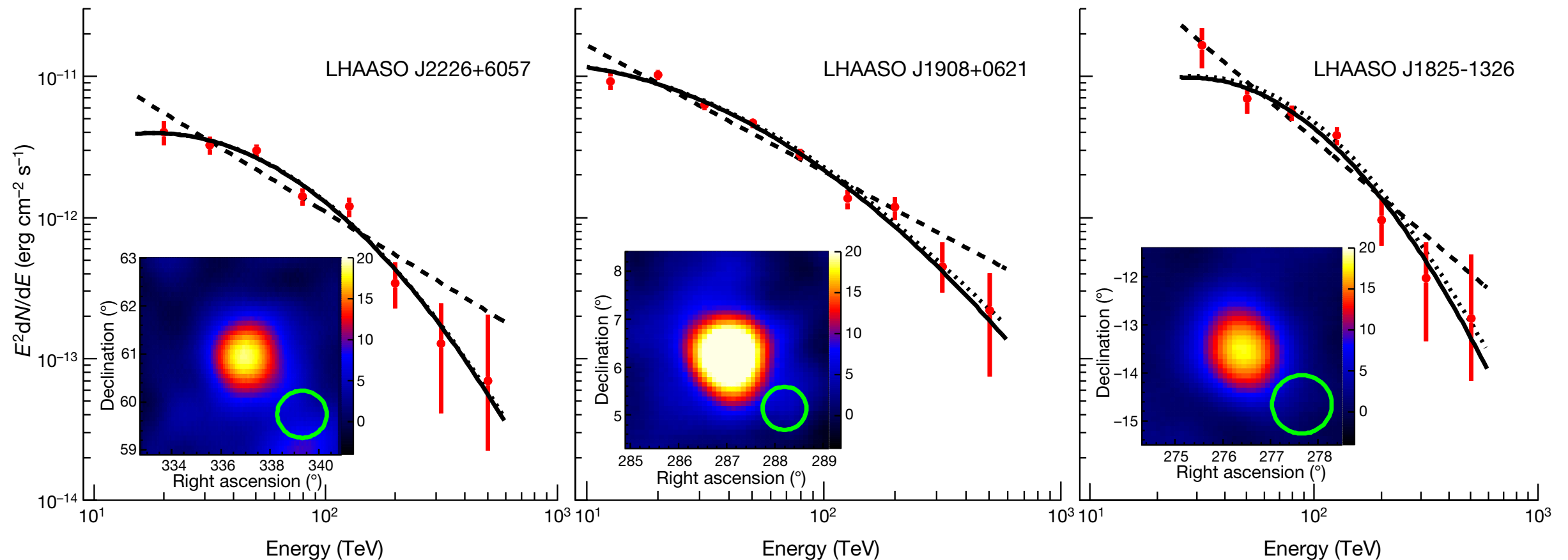


Fig. 1 | Spectral energy distributions and significance maps. a–c, Data are shown for LHAASO J2226+6057 (**a**), LHAASO J1908+0621 (**b**), and LHAASO J1825-1326 (**c**). Spectral fits with a log-parabola function (solid lines) in the form of $[E/(10 \text{ TeV})]^{-a-b \log[E/(10 \text{ TeV})]}$ are compared with the power-law fits $E^{-\Gamma}$ for: $a=1.56$, $b=0.88$ and $\Gamma=3.01$ (**a**); $a=2.27$, $b=0.46$ and $\Gamma=2.89$ (**b**); and $a=0.92$, $b=1.19$ and $\Gamma=3.36$ (**c**). The dotted curves correspond to the log-parabola fits corrected for the interstellar γ - γ absorption (see Methods for the radiation fields and Extended Data Fig. 6 for the opacity curves). The comparison of the power-law (PL) model and the log-parabola (LOG) model with the Akaike Information Criterion²⁰ (AIC) gives: $\text{AIC}_{\text{LOG}}=12.3$ and $\text{AIC}_{\text{PL}}=24.4$ for LHAASO J2226+6057; $\text{AIC}_{\text{LOG}}=15.1$ and $\text{AIC}_{\text{PL}}=30.1$ for LHAASO J1908+0621; and

$\text{AIC}_{\text{LOG}}=11.6$ and $\text{AIC}_{\text{PL}}=14.8$ for LHAASO J1825-1326. The insets show the significance maps of the three sources, obtained for γ -rays above 25 TeV. The colour bars show the square root of test statistics (TS), which is equivalent to the significance. The significance ($\sqrt{\text{TS}}$) maps are smoothed with the Gaussian-type point spread function (PSF) of each source. The size of PSFs (68% contamination regions) are shown at the bottom right of each map. We note that the PSFs of the three sources are slightly different owing to different inclination angles. Namely, the 68% contamination angles are 0.49° for LHAASO J2226+6057, 0.45° for LHAASO J1908+0621 and 0.62° for LHAASO J1825-1326. Error bars represent one standard deviation.

general considerations about accelerators

trajectory of particle in B field

centripetal force = Lorentz force

$$m \frac{v^2}{r} = q \cdot v \cdot B \qquad m \cdot v = p \quad \textbf{momentum}$$

$$\frac{p}{r} = Z \cdot e \cdot B$$

$$r_L = \frac{p}{z \cdot e \cdot B} \quad \textbf{Larmor radius}$$

L dimension of accelerator

$$L > 2 r_L$$

closer look (Hillas 1984): $L > \frac{2r_L}{\beta}$

velocity of scattering centers $\beta = \frac{v}{c}$



$$L > \frac{2 \cdot p}{z \cdot e \cdot B \cdot \beta}$$

$$B \cdot L > \frac{2 \cdot p}{z \cdot e \cdot \beta}$$

Hillas criterion

in astrophysical units

$$r_L = 1.08 \text{ pc} \frac{E_{15}}{Z \cdot B_{\mu G}}$$

$$B_{\mu G} \cdot L_{pc} > \frac{2 \cdot E_{15}}{Z \cdot \beta}$$

**necessary condition
not sufficient**

$$E_{15} < Z \cdot B_{\mu G} \cdot L_{pc} \cdot \frac{\beta}{2}$$

Transport equation for cosmic rays in the Galaxy

diffusion

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

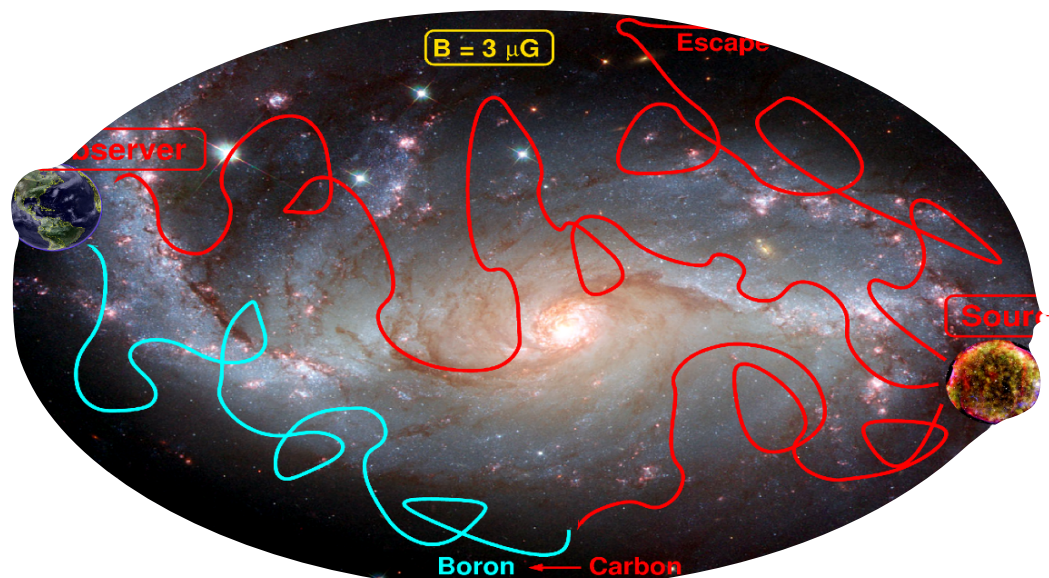
loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E}(b_i N_i) - n\nu\sigma_i N_i - \frac{N_i}{\gamma\tau_i} + Q_i + \sum_{j>i} n\nu\sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j\tau_{ij}}$$

source term

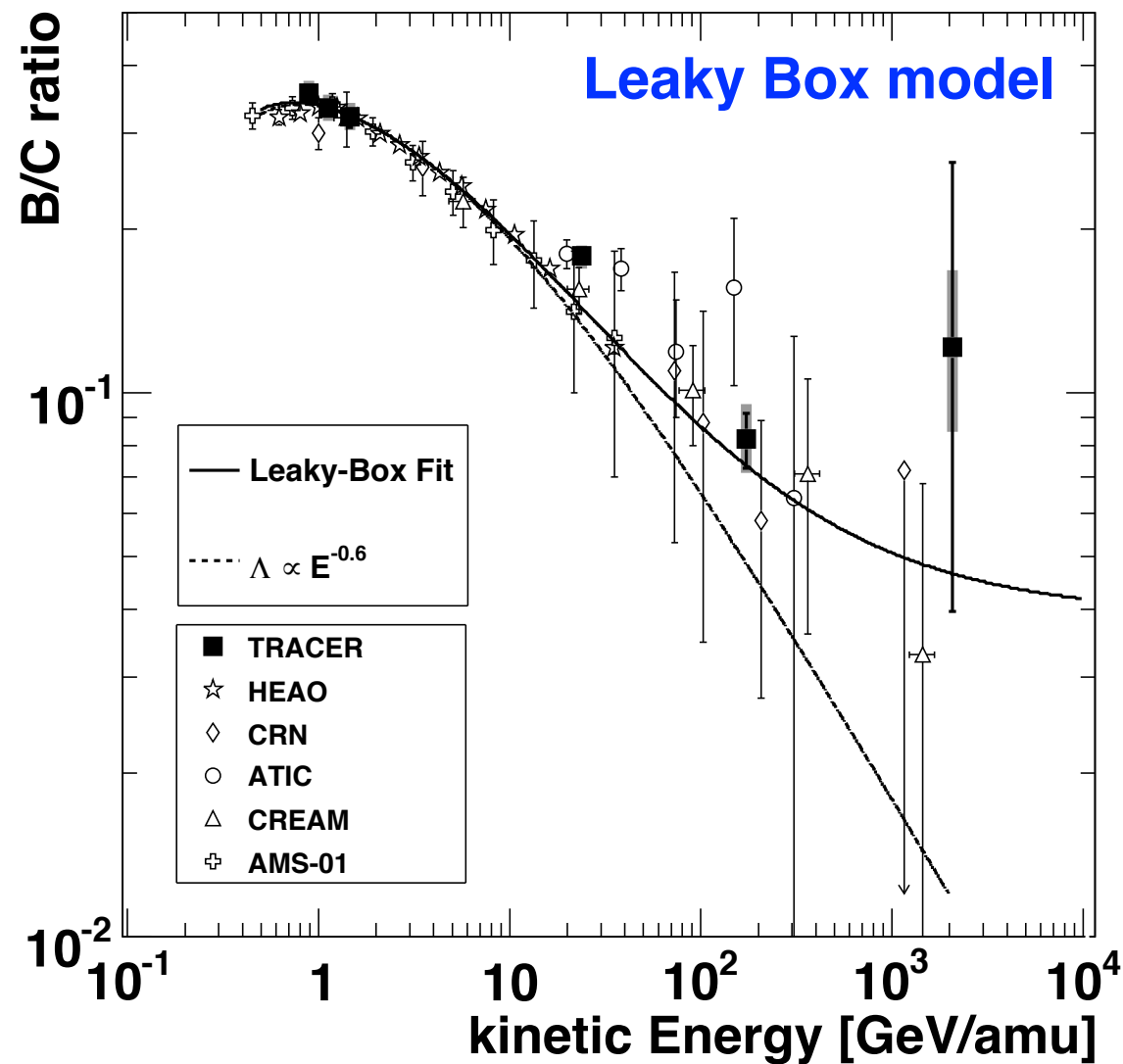
production through spallation
of heavy nuclei

production through decay
of heavy nuclei



Pathlength of cosmic rays in Galaxy

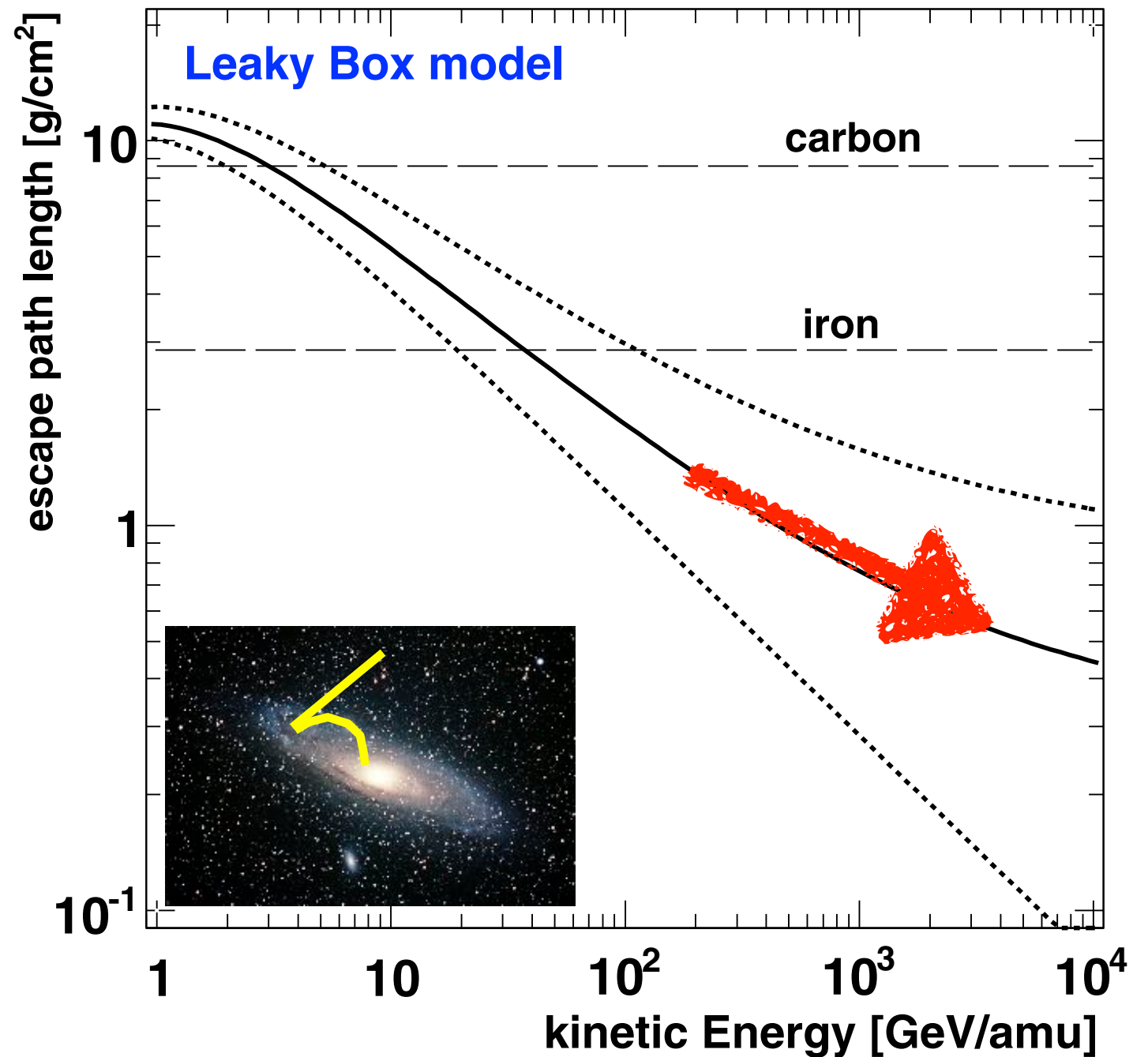
TRACER balloon experiment



Escape Path Length:

$$\Lambda_{esc}(E) = CE^{-\delta} + \Lambda_0$$

- Propagation index:
 $\delta = 0.64 \pm 0.02$.
- Residual path length:
 $\Lambda_0 = 0.7 \pm 0.2 \text{ g/cm}^2$.



$$\Lambda(R) = \frac{26.7\beta}{(\beta R)^\delta + (0.714 \cdot \beta R)^{-1.4}} + \Lambda_0 \text{ g/cm}^2,$$

Pathlength vs. interaction length

pathlength in Galaxy

$$\lambda_{esc} = 5 - 10 \text{ g/cm}^2$$

interaction length

nuclear radius

$$r = r_0 A^{1/3} \quad r_0 = 1.3 \cdot 10^{-13} \text{ cm}$$

cross section

$$\sigma_{p-A} = \pi (r_p + r_0 A^{1/3})^2$$

ISM: protons

$$n = 1/\text{cm}^3 \quad \rho = 1.67 \cdot 10^{-24} \text{ g/cm}^3$$

interaction length

$$\lambda_{p-A} = \frac{\rho}{\sigma_{p-A} \cdot n}$$

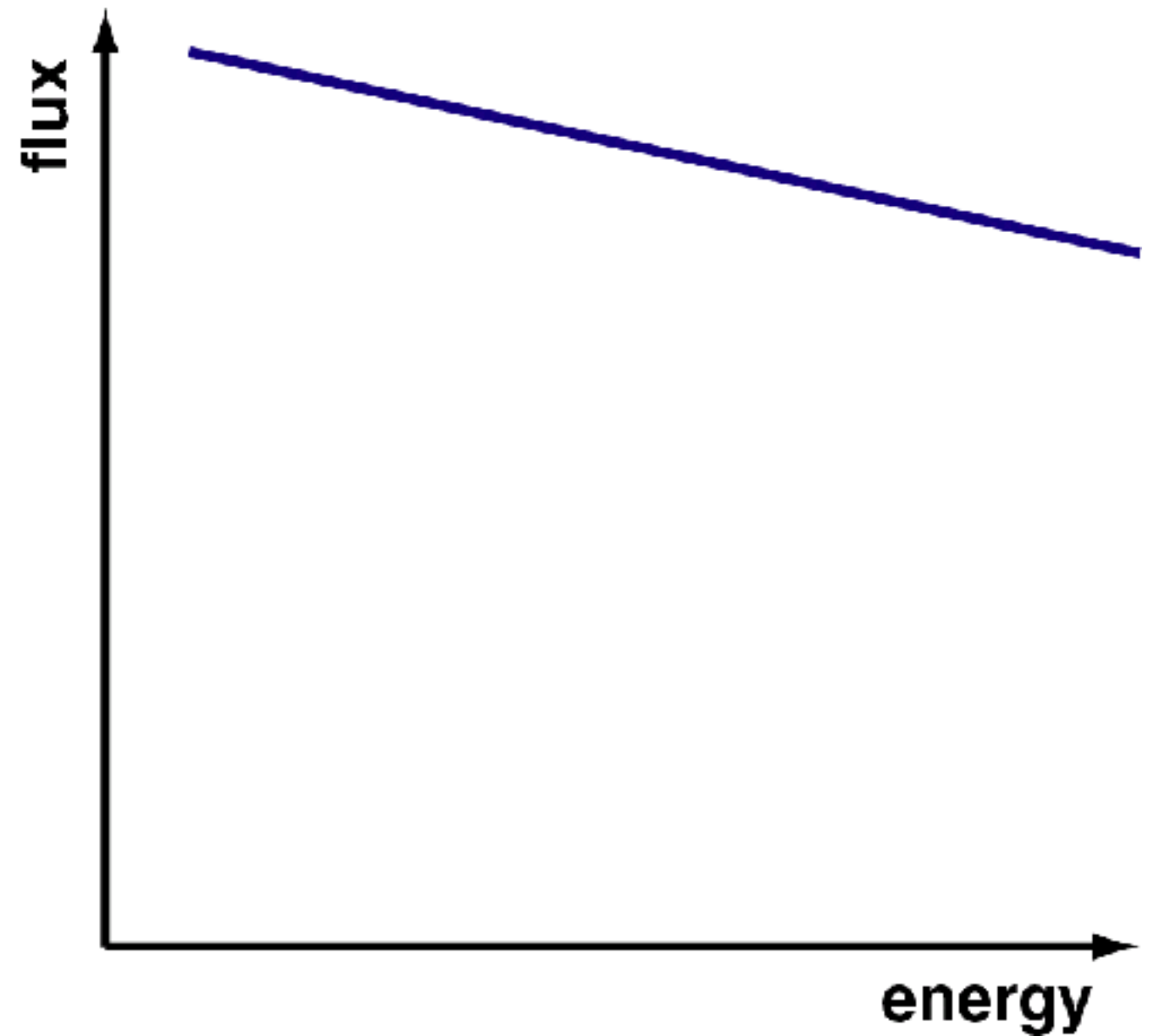
$$\lambda_{p-p} = 21 \text{ g/cm}^2 > \lambda_{esc}$$

$$\lambda_{p-Fe} = 1.6 \text{ g/cm}^2 < \lambda_{esc}$$

Shape of energy spectrum

$$\frac{dN}{dE} \propto E_0^\gamma$$

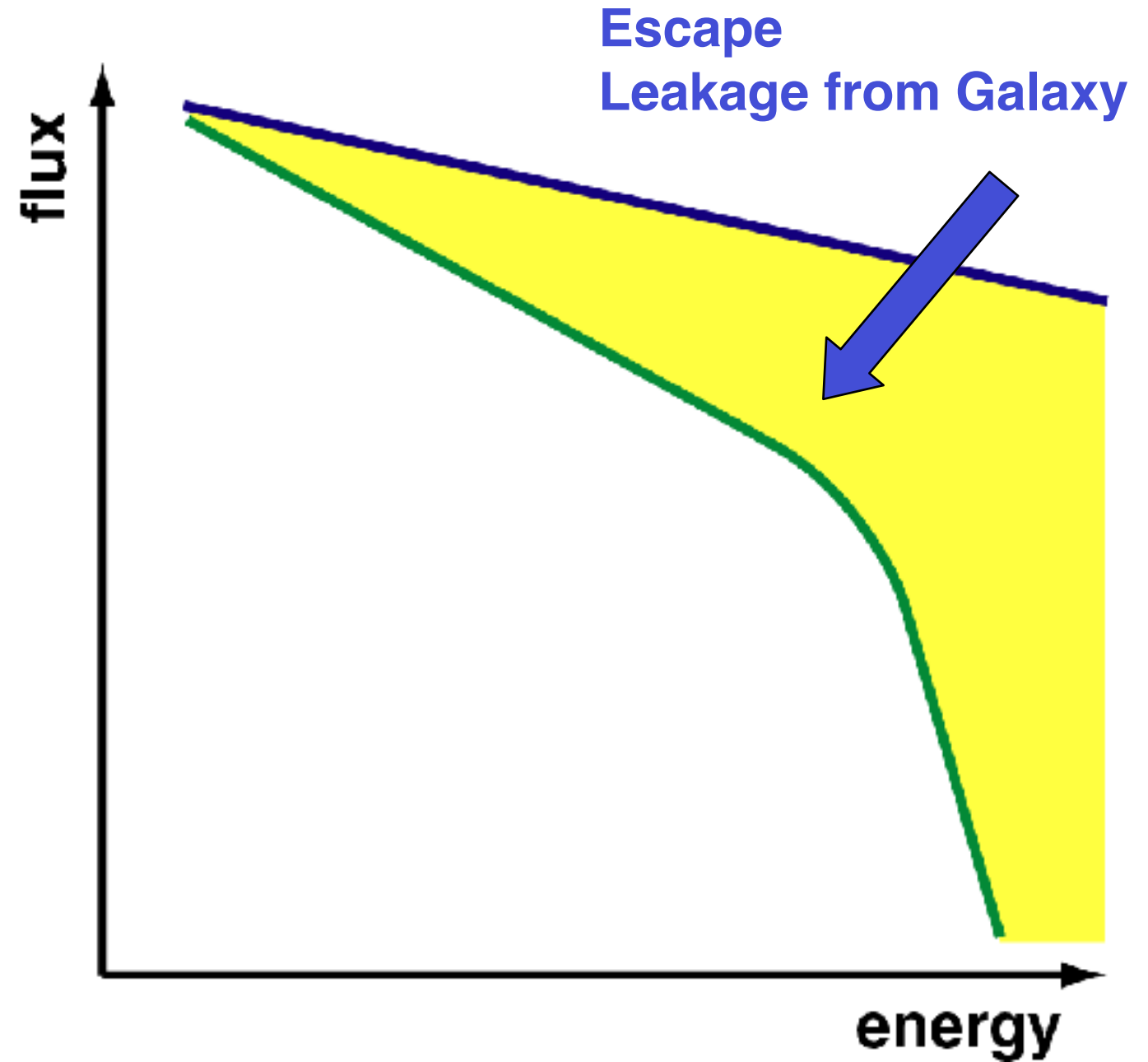
at source $\gamma \sim -2.1$



Shape of energy spectrum

$$\frac{dN}{dE} \propto E_0^\gamma$$

at source $\gamma \sim -2.1$

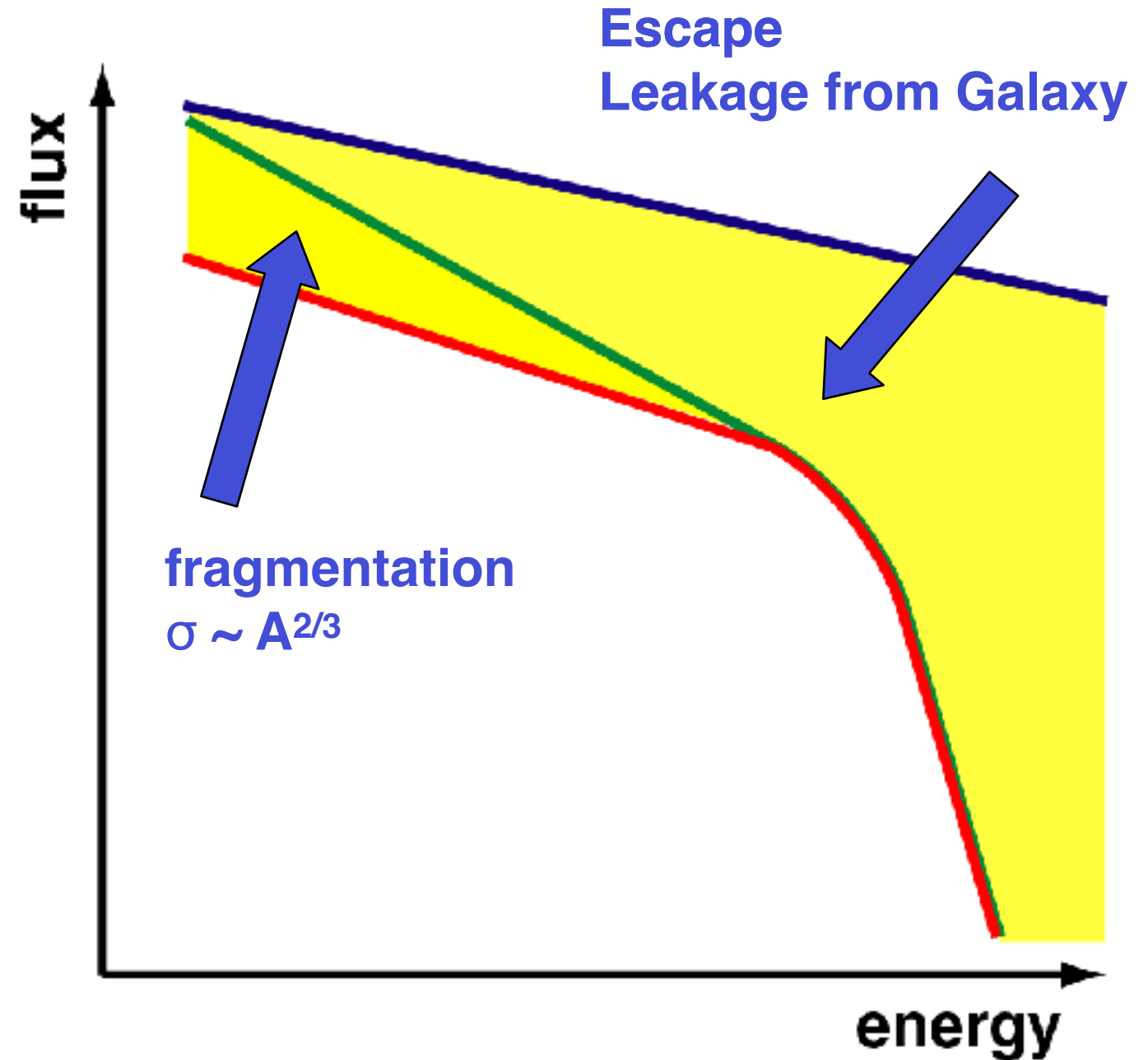


Shape of energy spectrum

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at source $\gamma \sim -2.1$

at Earth $\gamma \sim -2.6$ to -2.7



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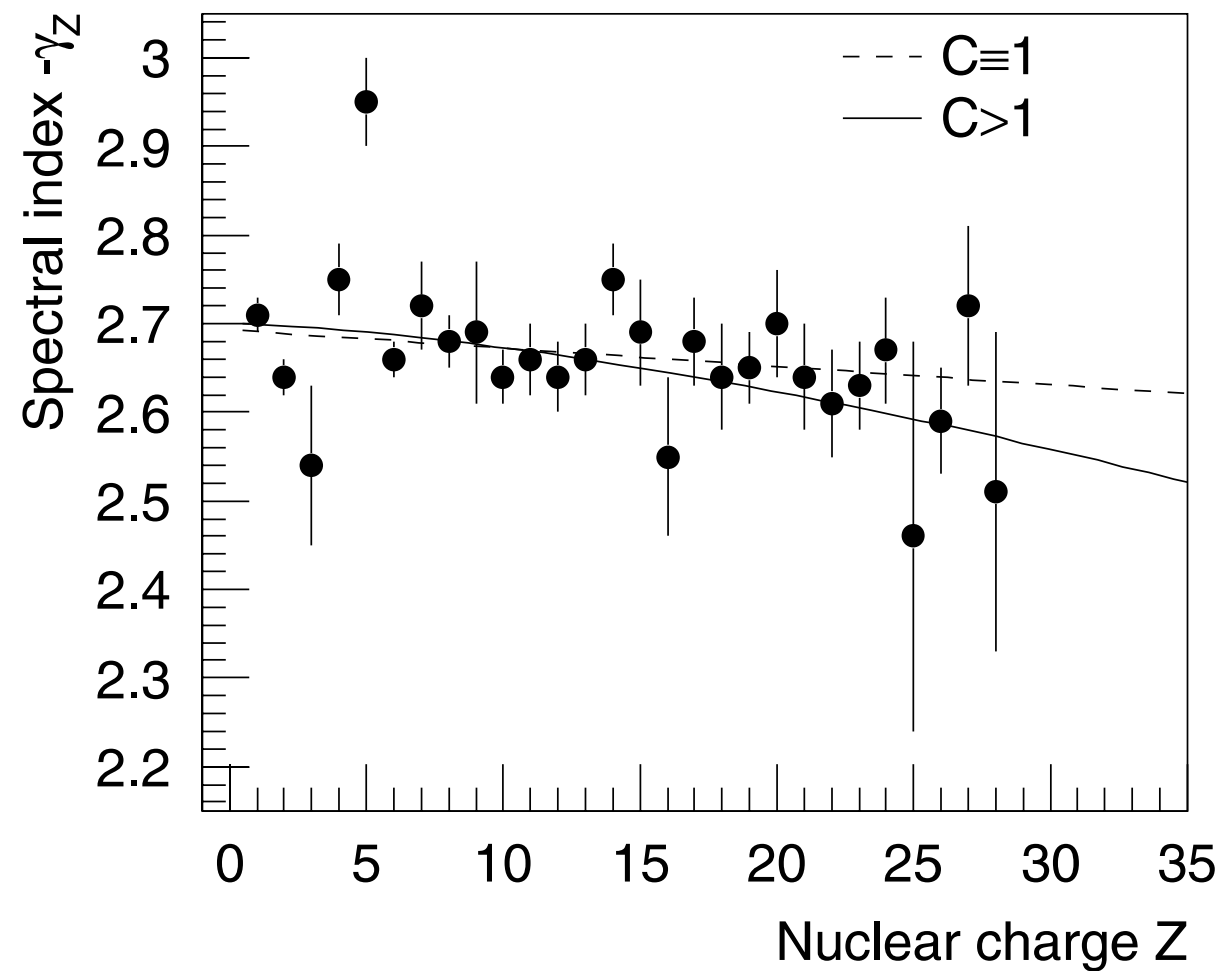
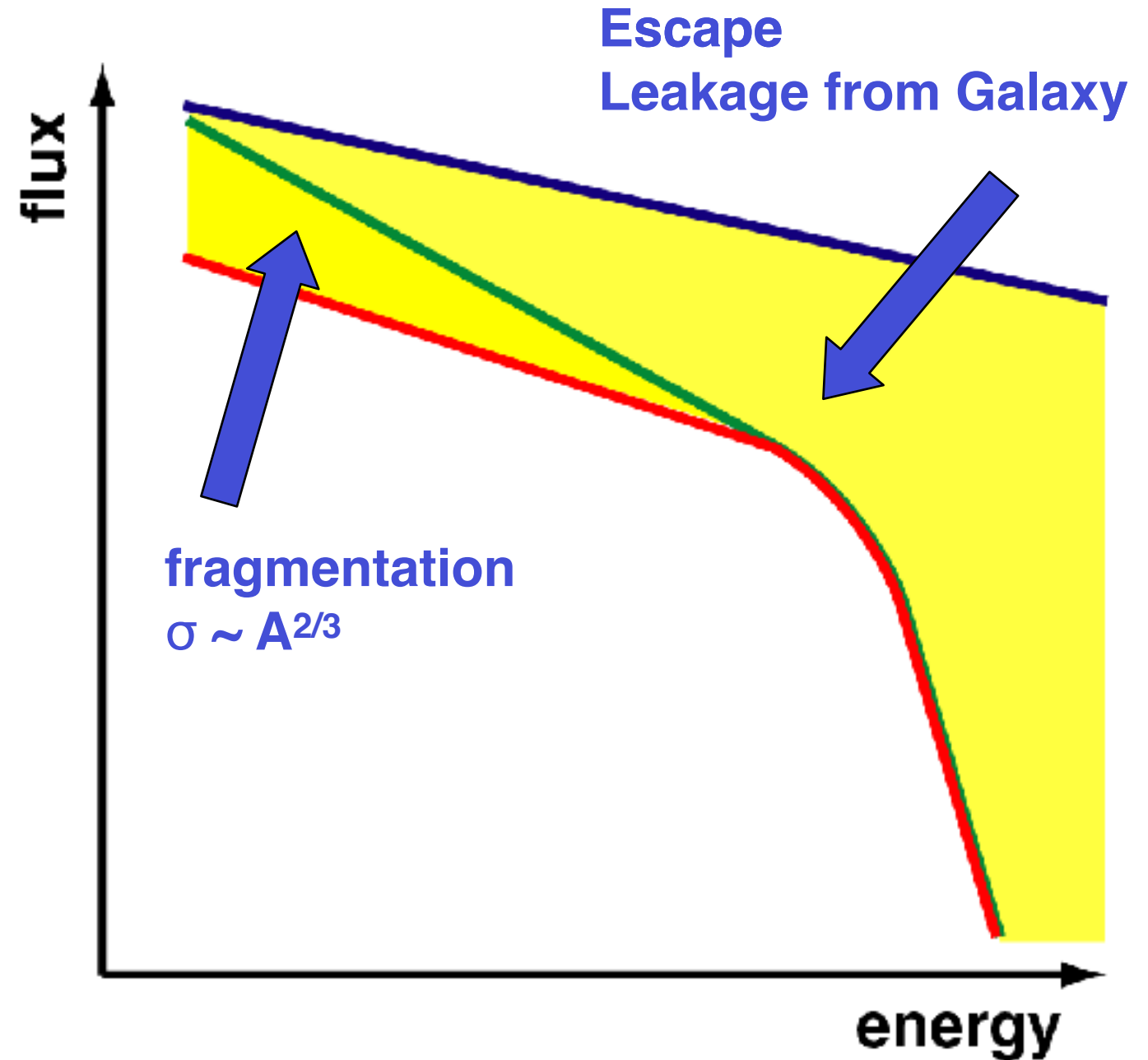


Fig. 5. Spectral index γ_Z versus nuclear charge Z (see Table 1). The solid line represents a three parameter fit according to Eq. (6), the dashed graph a linear fit.



Transport equation for cosmic rays in the Galaxy

diffusion

see Ahlers, ISGRA 2022

also Cannady, ISGRA 2022

energy loss (Bethe Bloch)

loss through interactions
with ISM (spallation)

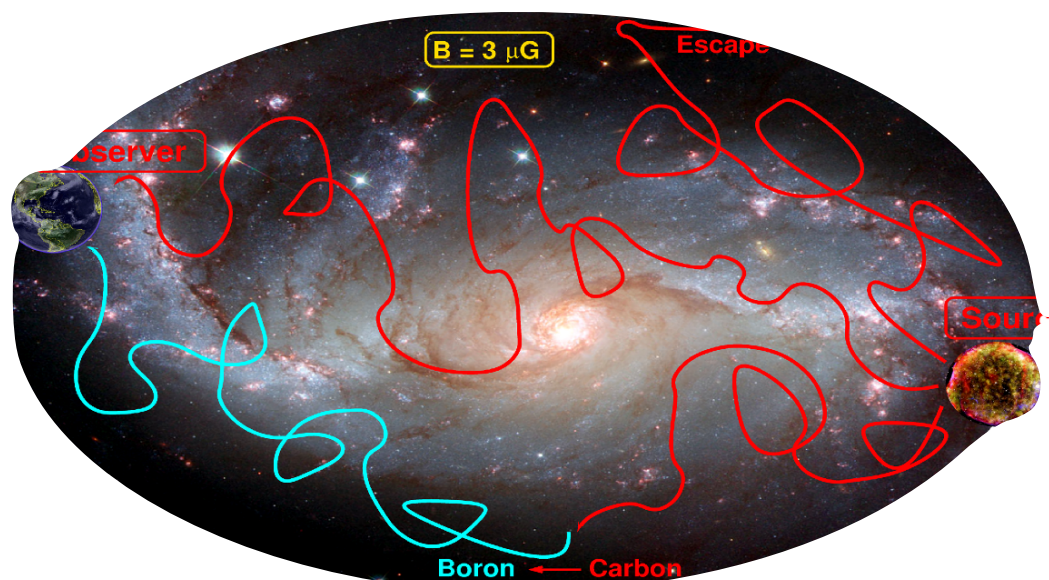
loss through radioactive decay

$$\frac{\partial N_i}{\partial t} = \nabla(D_i \nabla N_i) - \frac{\partial}{\partial E} (b_i N_i) - n v \sigma_i N_i - \frac{N_i}{\tau_i} + Q_i + \sum_{j>i} n v \sigma_{ij} N_j + \sum_{j>i} \frac{N_j}{\gamma_j \tau_{ij}}$$

source term

production through spallation
of heavy nuclei

production through decay
of heavy nuclei



Propagation of super-high-energy cosmic rays in the Galaxy

Jörg R. Hörandel ^{a,*}, Nikolai N. Kalmykov ^b, Aleksei V. Timokhin ^c

The steady-state diffusion equation for the cosmic-ray density $N(r)$ is (neglecting nuclear interactions and energy losses)

$$-\nabla_i D_{ij}(r) \nabla_j N(r) = Q(r). \quad (1)$$

$Q(r)$ is the cosmic-ray source term and $D_{ij}(r)$ the diffusion tensor.

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Under the assumption of azimuthal symmetry and taking into account the predominance of the toroidal component of the magnetic field, Eq. (1) is presented in cylindrical coordinates as

$$\left[-\frac{1}{r} \frac{\partial}{\partial r} r D_{\perp} \frac{\partial}{\partial r} - \frac{\partial}{\partial z} D_{\perp} \frac{\partial}{\partial z} - \frac{\partial}{\partial z} D_A \frac{\partial}{\partial r} + \frac{1}{r} \frac{\partial}{\partial r} r D_A \frac{\partial}{\partial z} \right] N(r, z) = Q(r, z), \quad (2)$$

where $N(r, z)$ is the cosmic-ray density averaged over the large-scale fluctuations with a characteristic scale $L \sim 100$ pc [3]. $D_{\perp} \propto E^m$ is the diffusion coefficient, where m is much less than one ($m \approx 0.2$), and $D_A \propto E$ the Hall diffusion coefficient. The influence of Hall diffusion becomes predominant at high energies ($>10^{15}$ eV). The sharp

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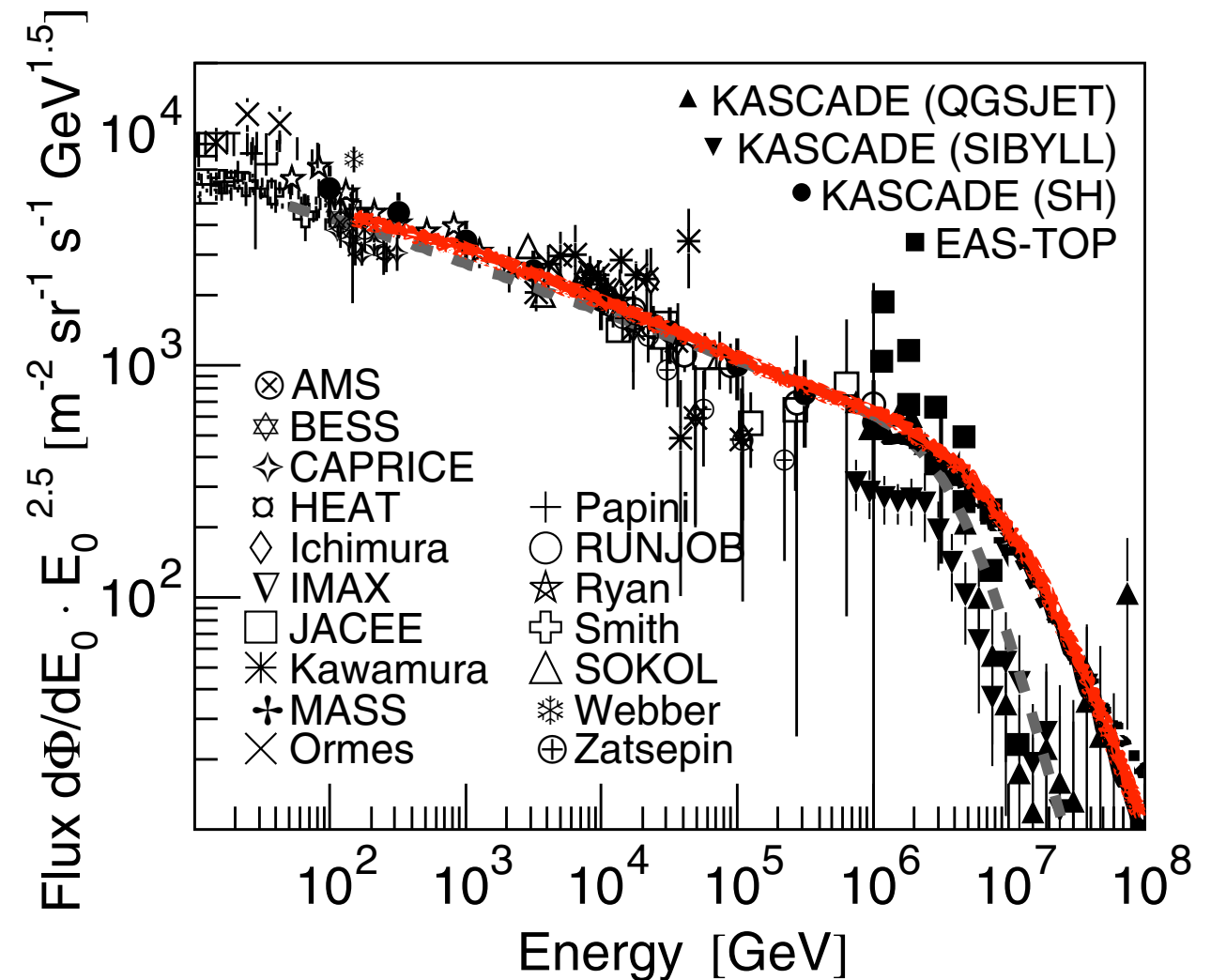


Fig. 7. Proton flux as obtained from various measurements, for references see [28], compared to the spectra shown in Fig. 6 (black lines) and the *polygono* model [26] (grey, dashed line).

Origin of the knee? JRH, Astropart. Phys. 21 (2004) 241 (updated)

Acceleration (SNR)

- .. in SNR
- .. in SNR + radio galaxies
- .. in oblique shocks
- .. in variety of SNR
- Single source model
- Reacceleration in galactic wind

Berezhko & Ksenofontov
Stanev ..
Kobayakawa ..
Sveshnikova
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Acceleration (SNR)

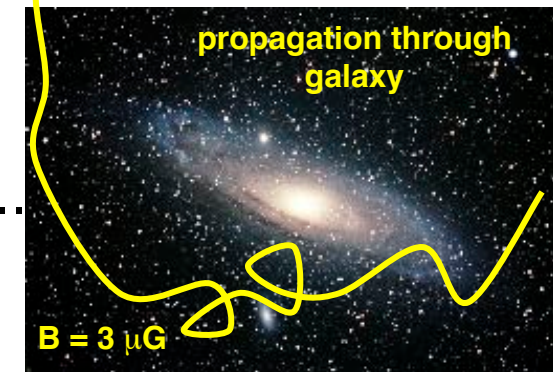
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Leakage from Galaxy

- Minimum pathlength model
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- Diffusion in turbulent magnetic fields
- Diffusion and drift

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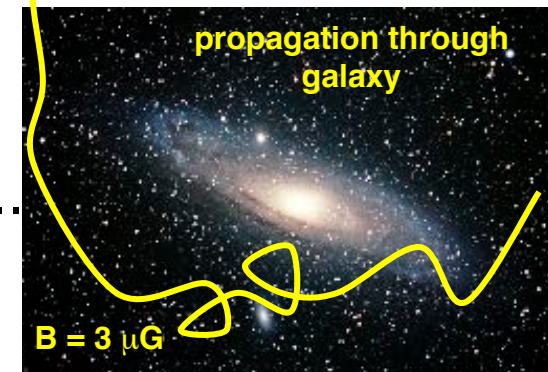
γ -ray bursts

- Cannonball model
- Acceleration in GRB + diffusion
- Acceleration in GRB $E_{\max} \sim A$

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Swordy
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Interaction with background particles

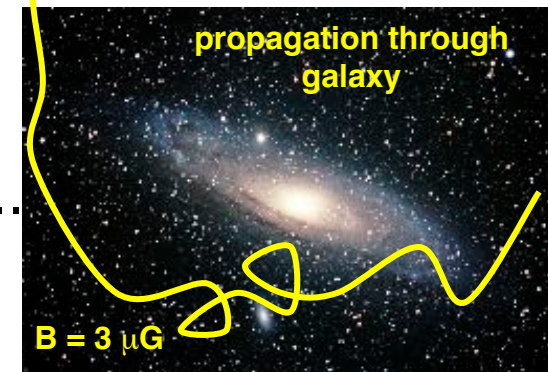
- Diffusion model + photo-disintegration Tkaczyk
- Interaction with neutrinos in galactic halo
- Photo-disintegration (optical and UV photons)

Berezhko & Ksenofontov
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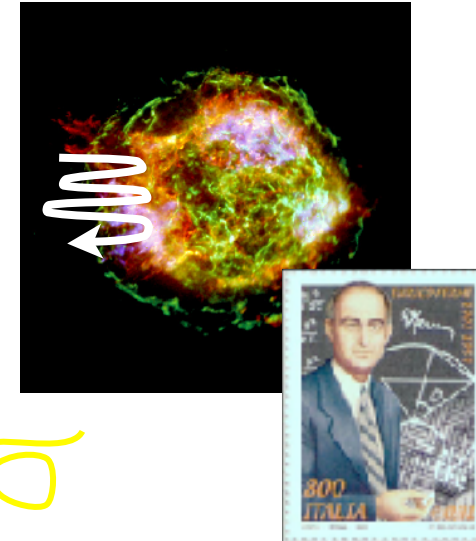
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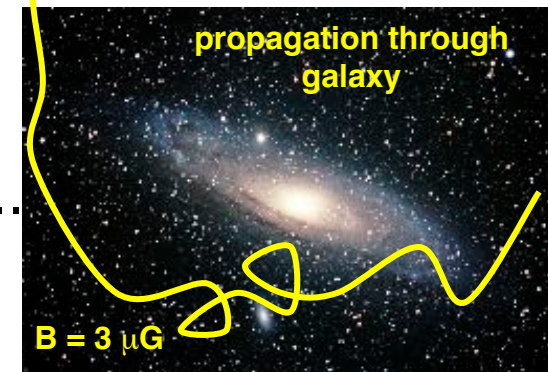
Particle physics in atmosphere

- Gravitons, SUSY

Berezhko & Ksenofontov
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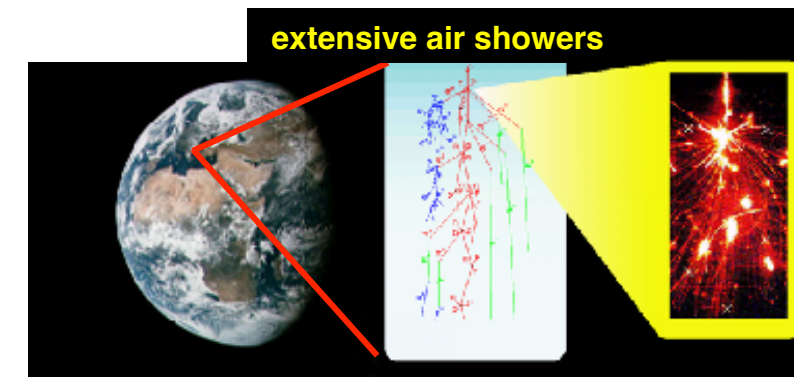
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Dova ..
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Kazanas & Nicolaidis

Origin of the knee? JRH, Astropart. Phys. 21 (2004) 241 (updated)

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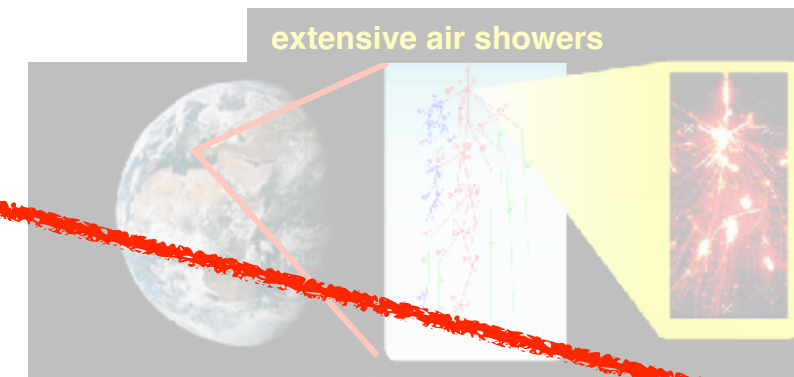
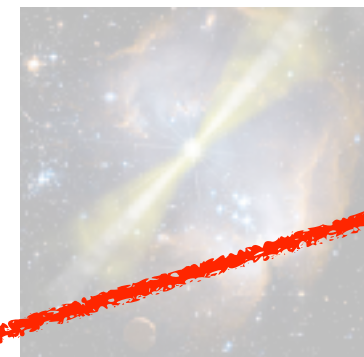
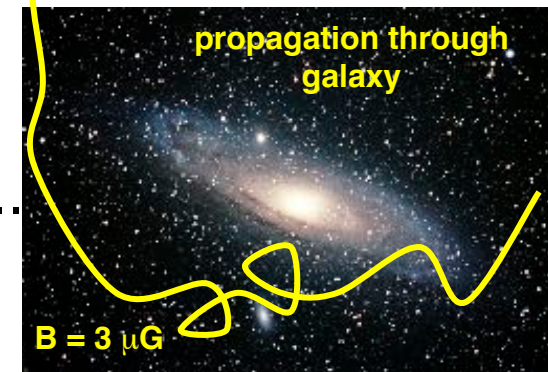
Berezhko & Ksenofontov
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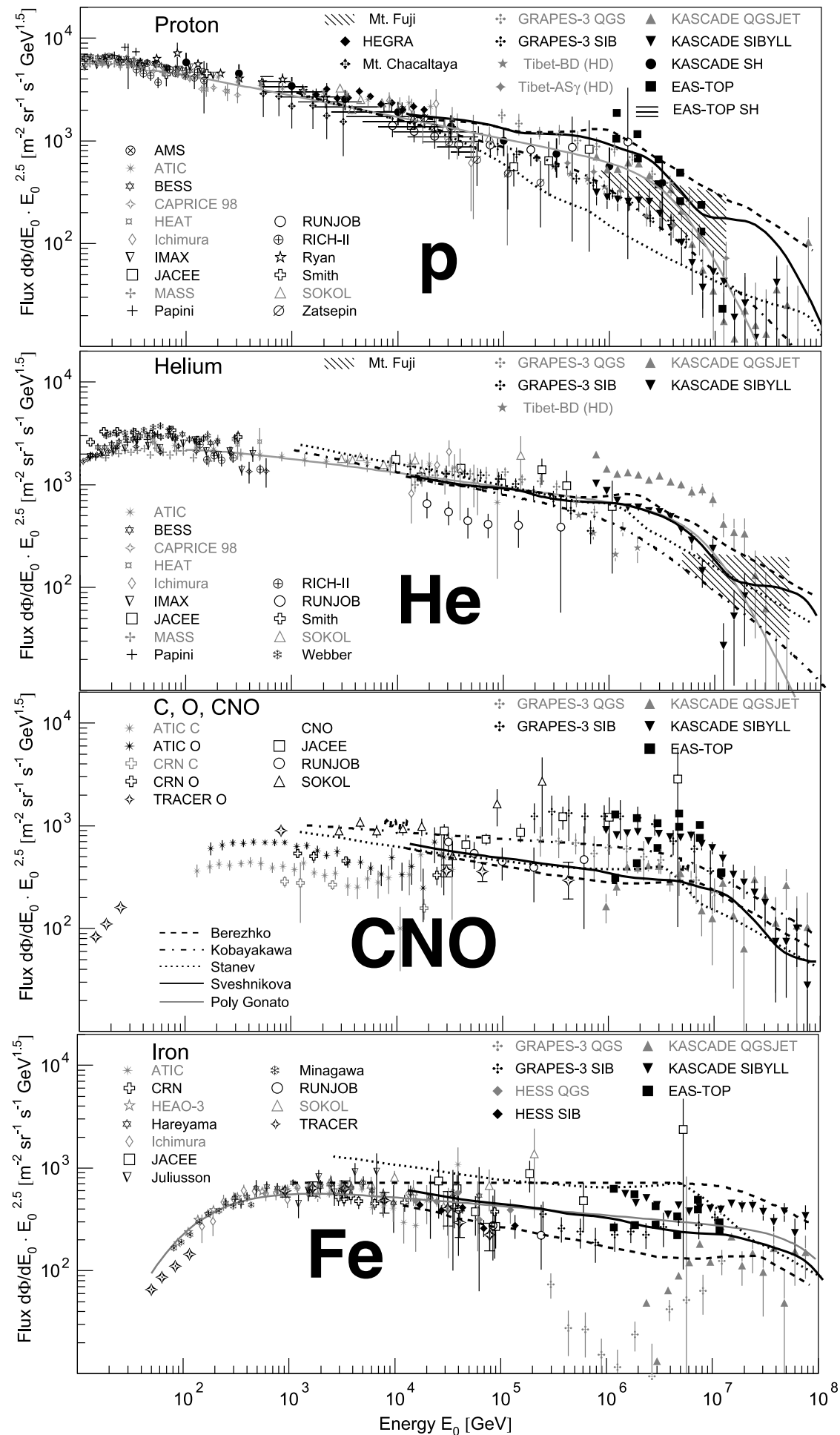
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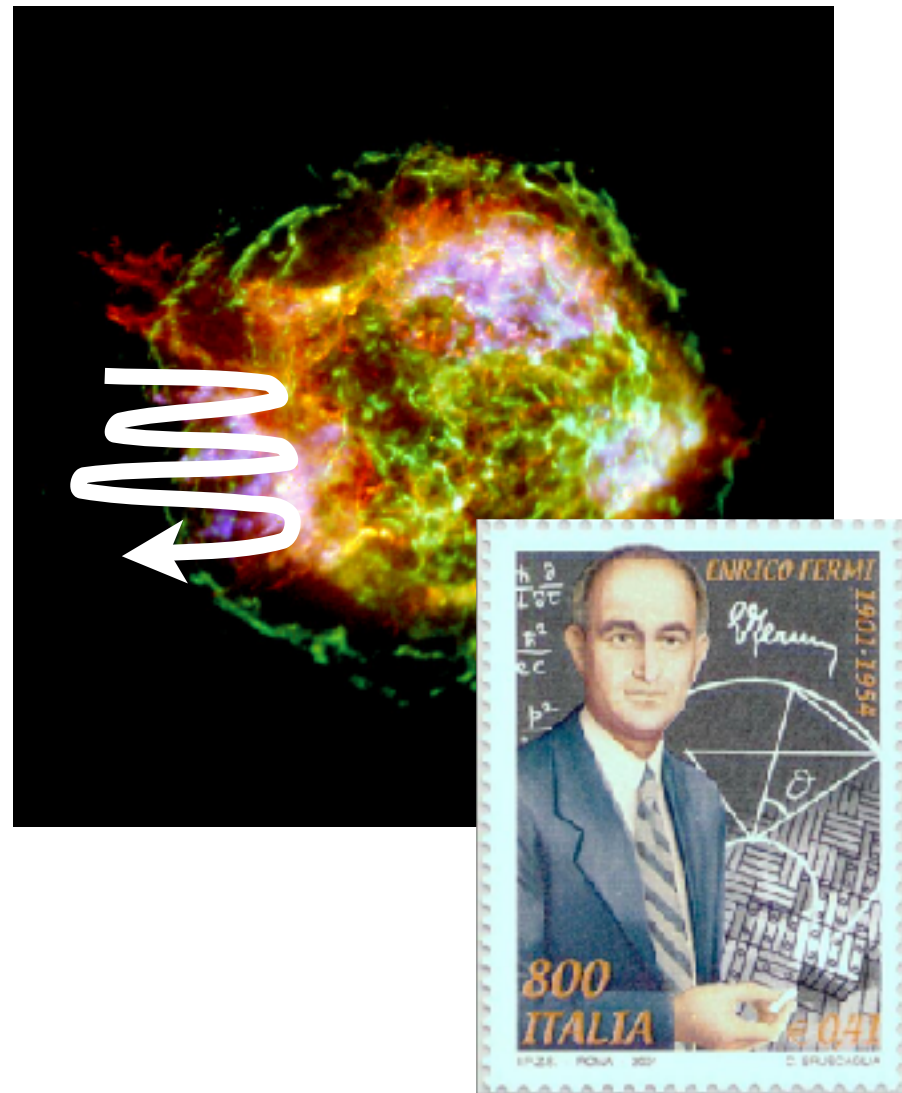




maximum energy

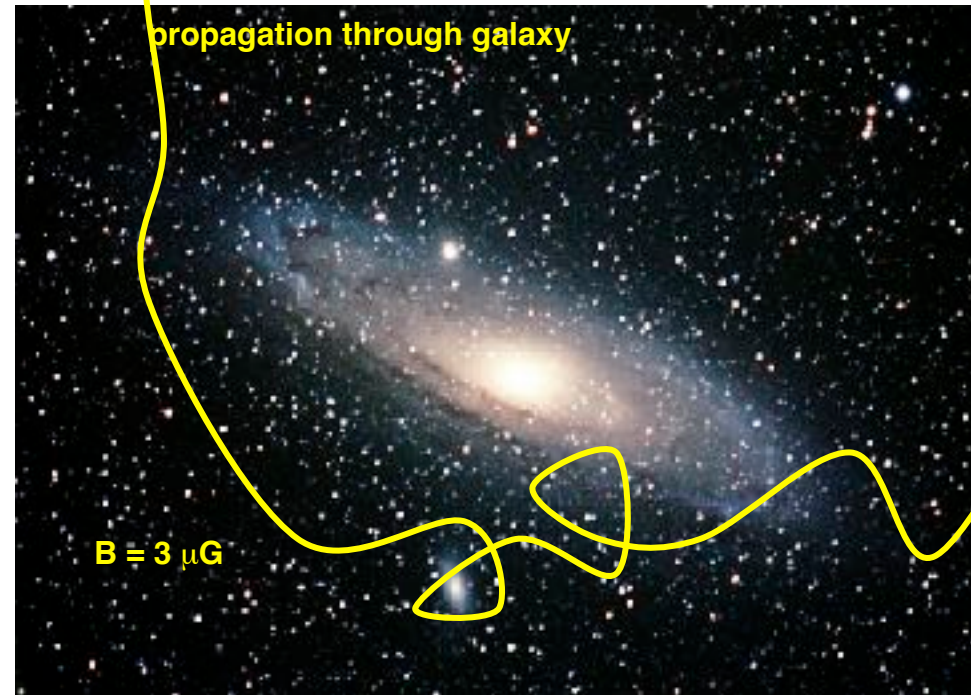
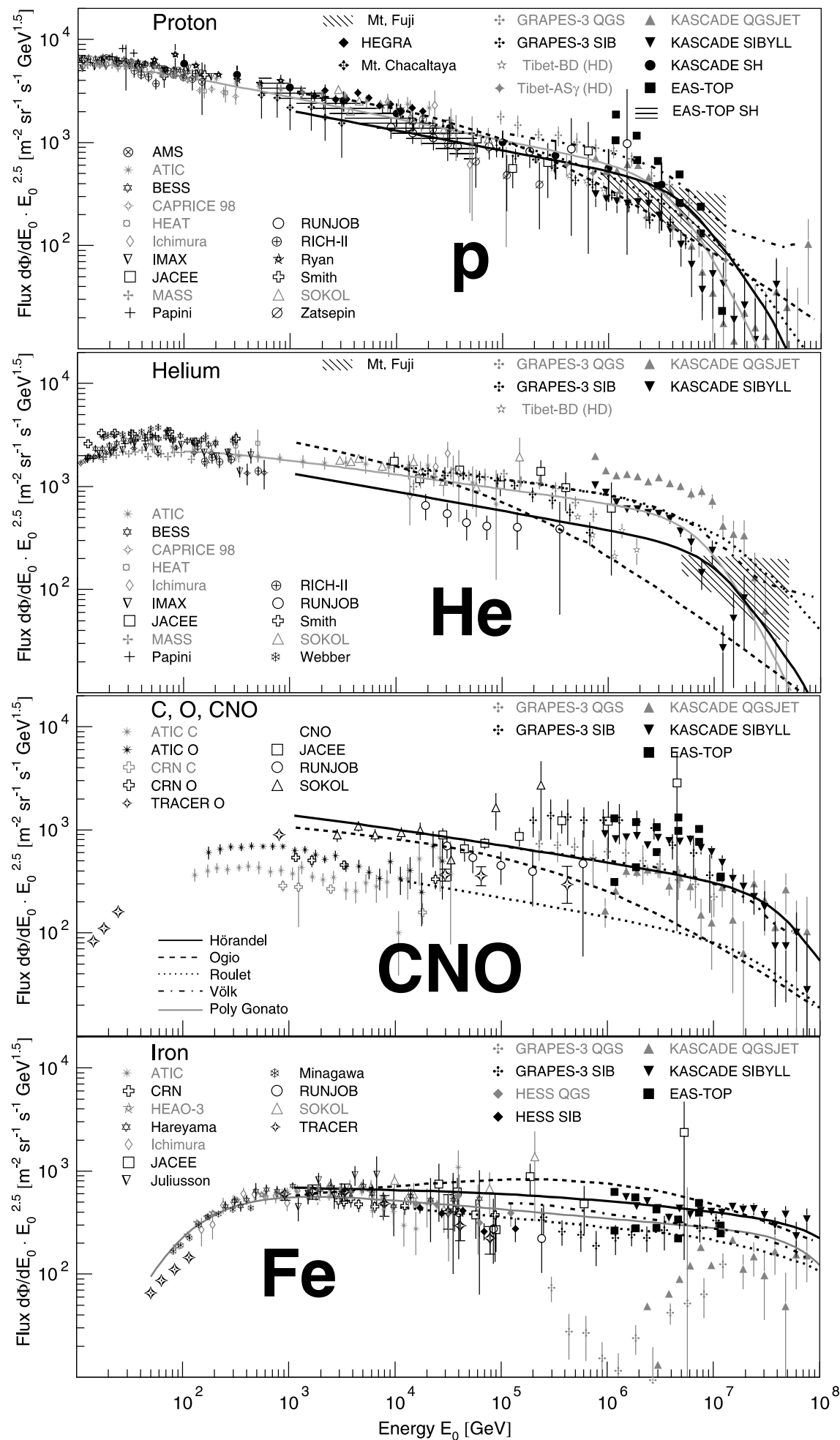
$$E_{max} \propto B \cdot Z$$

$$E_{max} \approx Z \cdot 100 \text{ TeV} \dots Z \cdot 5 \text{ PeV}$$



leakage from Galaxy

$$E_k \propto Z$$



Transition to extragalactic CR component

J. Blümer et al. / Progress in Particle and Nuclear Physics 63 (2009) 293–338

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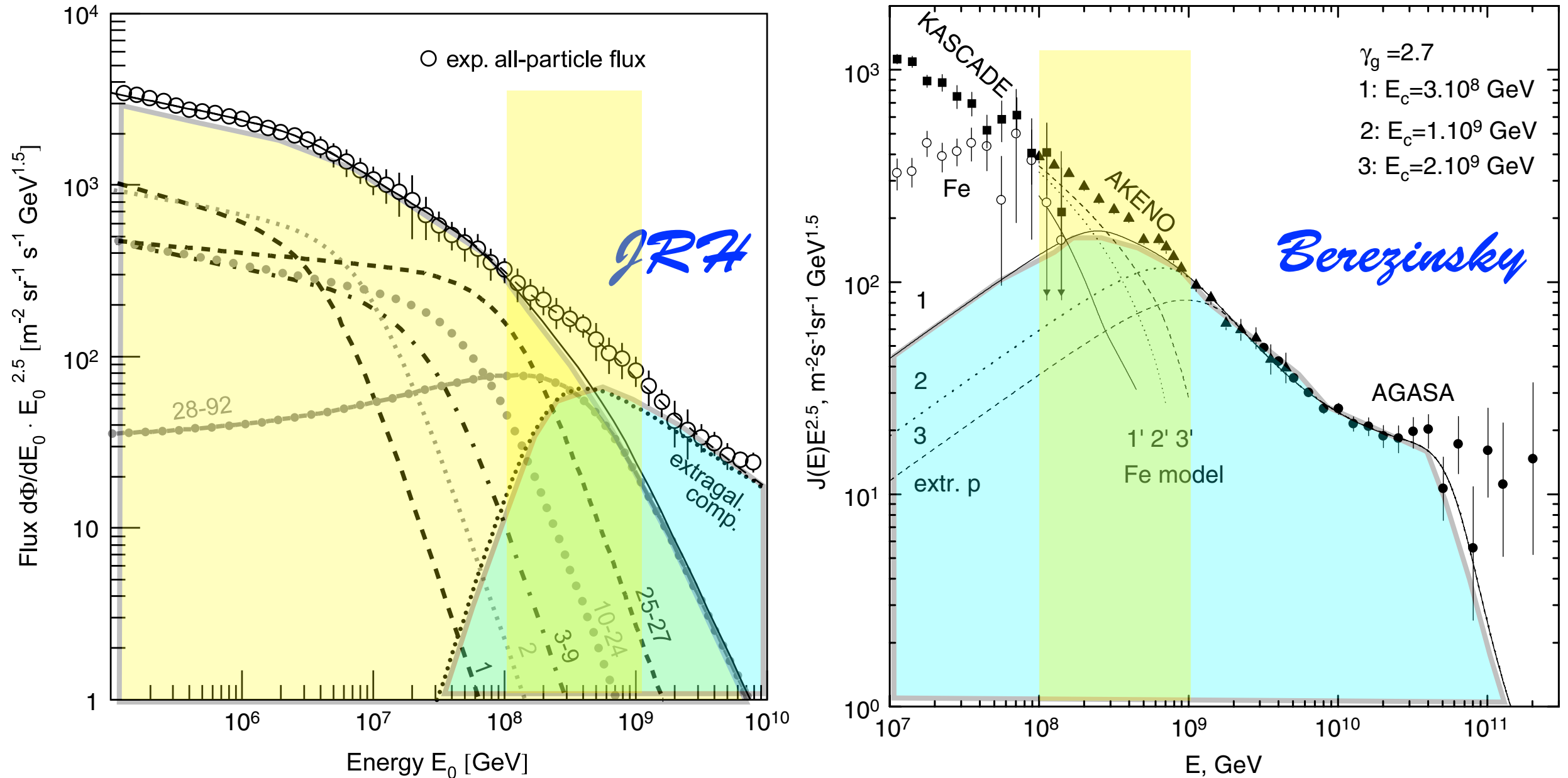
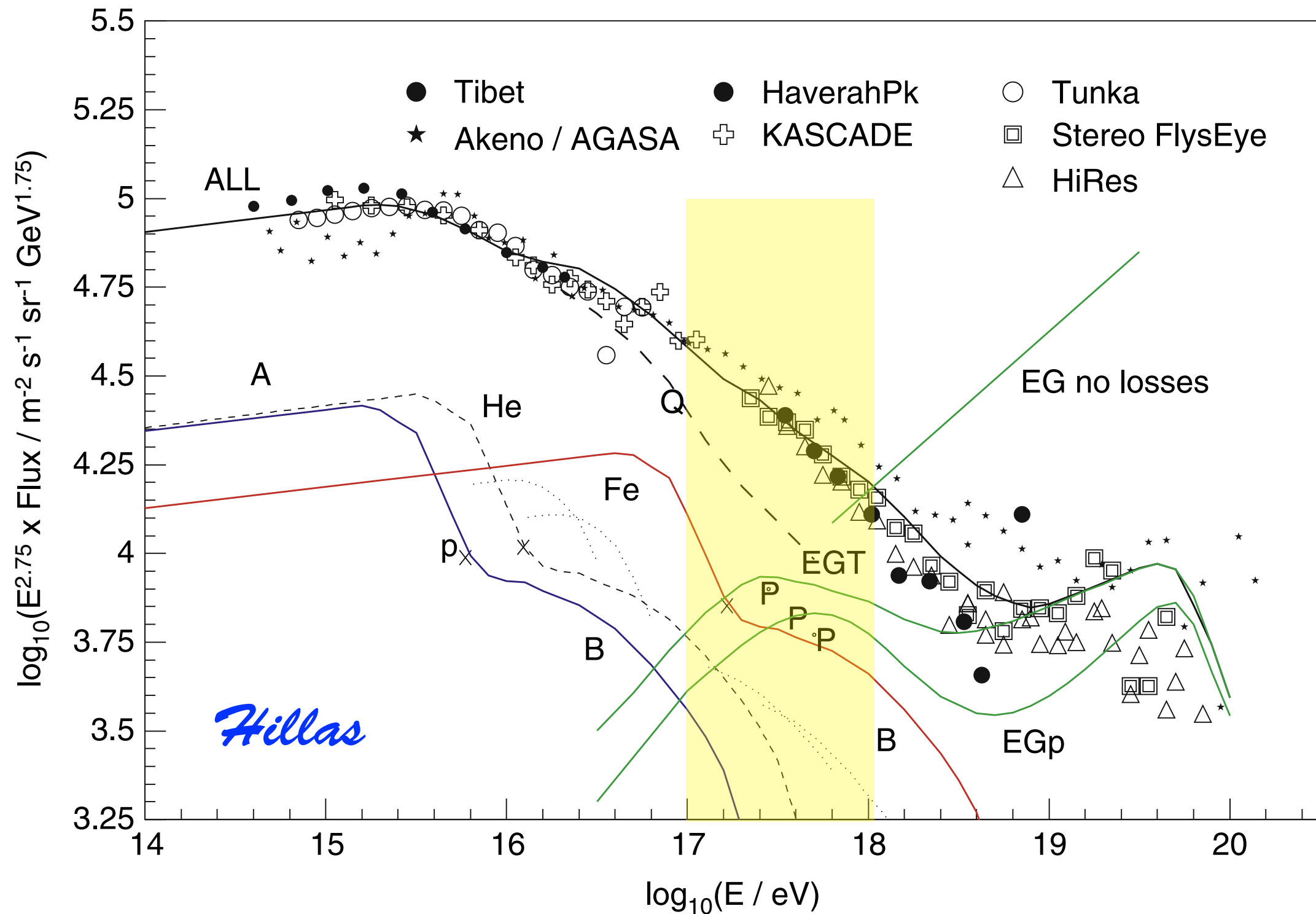


Fig. 26. *Left panel:* Cosmic-ray energy spectra according to the poly-gonato model [2]. The spectra for groups of elements are labeled by their respective nuclear charge numbers. The sum of all elements yields the galactic all-particle spectrum (—) which is compared to the average measured flux. In addition, a hypothetical extragalactic component is shown to account for the observed all-particle flux (---). *Right panel:* Transition from galactic to extragalactic cosmic rays according to Berezhinsky et al. [451]. Calculated spectra of extragalactic protons (curves 1, 2, 3) and of galactic iron nuclei (curves 1', 2', 3') are compared with the all-particle spectrum from the Akeno and AGASA experiments. KASCADE data are shown as filled squares for the all-particle flux and as open circles for the flux of iron nuclei.

Transition to extragalactic CR component



„classical“ supernovae + additional component

Contribution of (regular) SNR-CR to all-particle spectrum

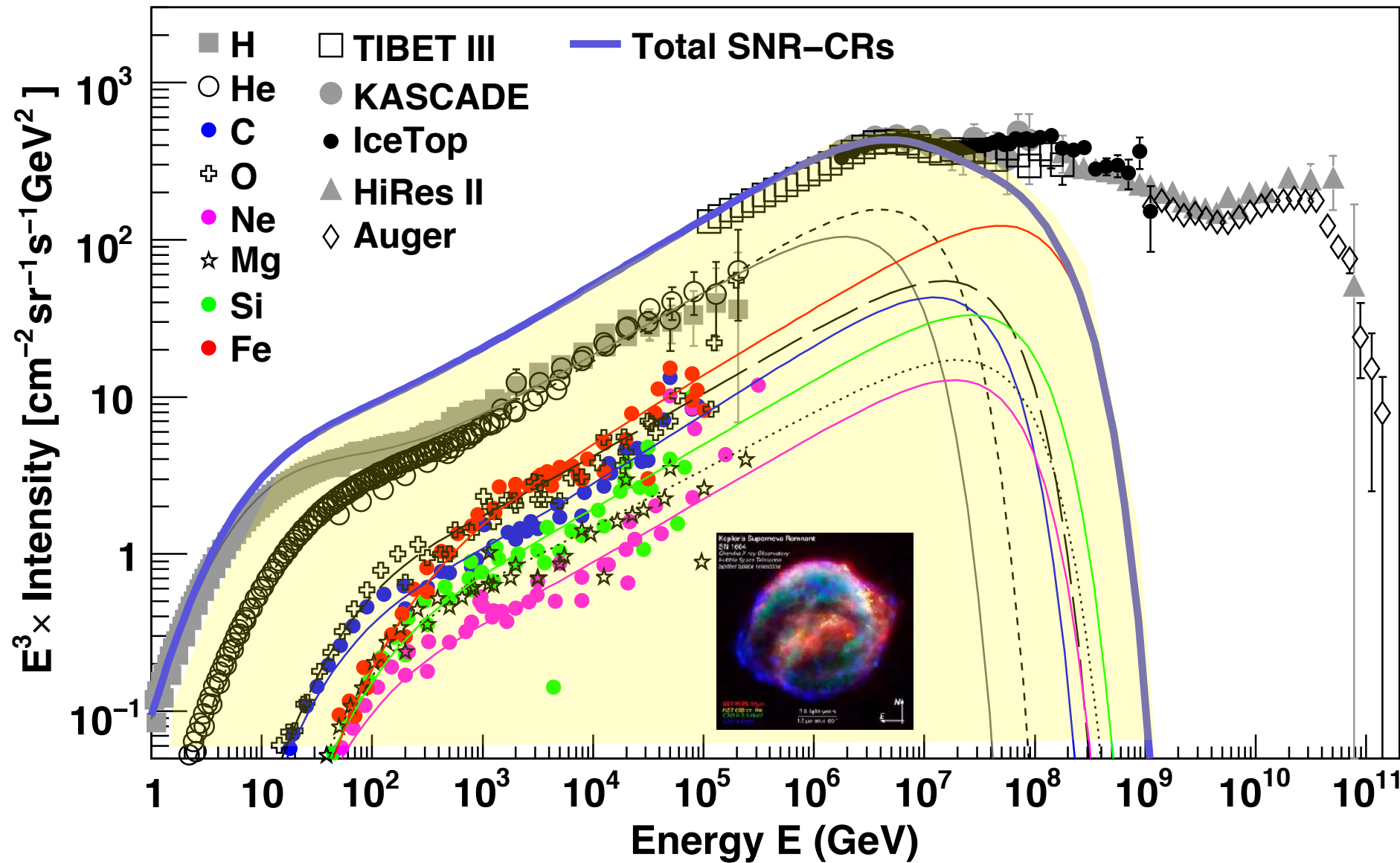


Fig. 2. Contribution of SNR-CRs to the all-particle cosmic-ray spectrum. The thin lines represent spectra for the individual elements, and the thick-solid line represents the total contribution. The calculation assumes an exponential cut-off energy for protons at $E_c = 4.5 \times 10^6$ GeV. Other model parameters, and the low-energy data are the same as in Figure 1. Error bars are shown only for the proton and helium data. High-energy data: KASCADE (Antoni et al. 2005), IceTop (Aartsen et al. 2013), Tibet III (Amenomori et al. 2008), the Pierre Auger Observatory (Schulz et al. 2013), and HiRes II (Abbasi et al. 2009).

~8% of mechanical power of SN --> CRs

Contribution of (regular) SNR-CR to all-particle spectrum

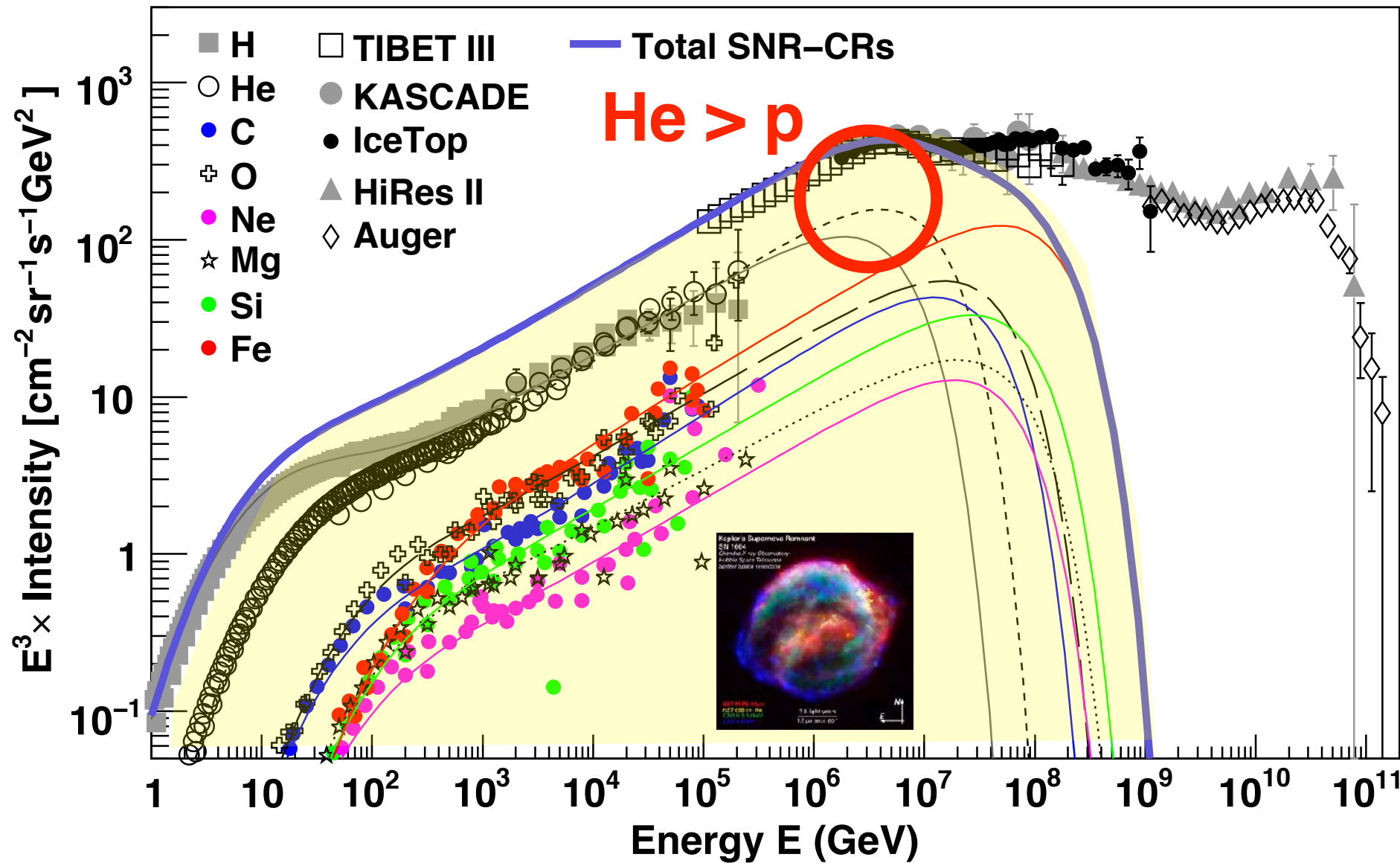


Fig. 2. Contribution of SNR-CRs to the all-particle cosmic-ray spectrum. The thin lines represent spectra for the individual elements, and the thick-solid line represents the total contribution. The calculation assumes an exponential cut-off energy for protons at $E_c = 4.5 \times 10^6$ GeV. Other model parameters, and the low-energy data are the same as in Figure 1. Error bars are shown only for the proton and helium data. High-energy data: KASCADE (Antoni et al. 2005), IceTop (Aartsen et al. 2013), Tibet III (Amenomori et al. 2008), the Pierre Auger Observatory (Schulz et al. 2013), and HiRes II (Abbasi et al. 2009).

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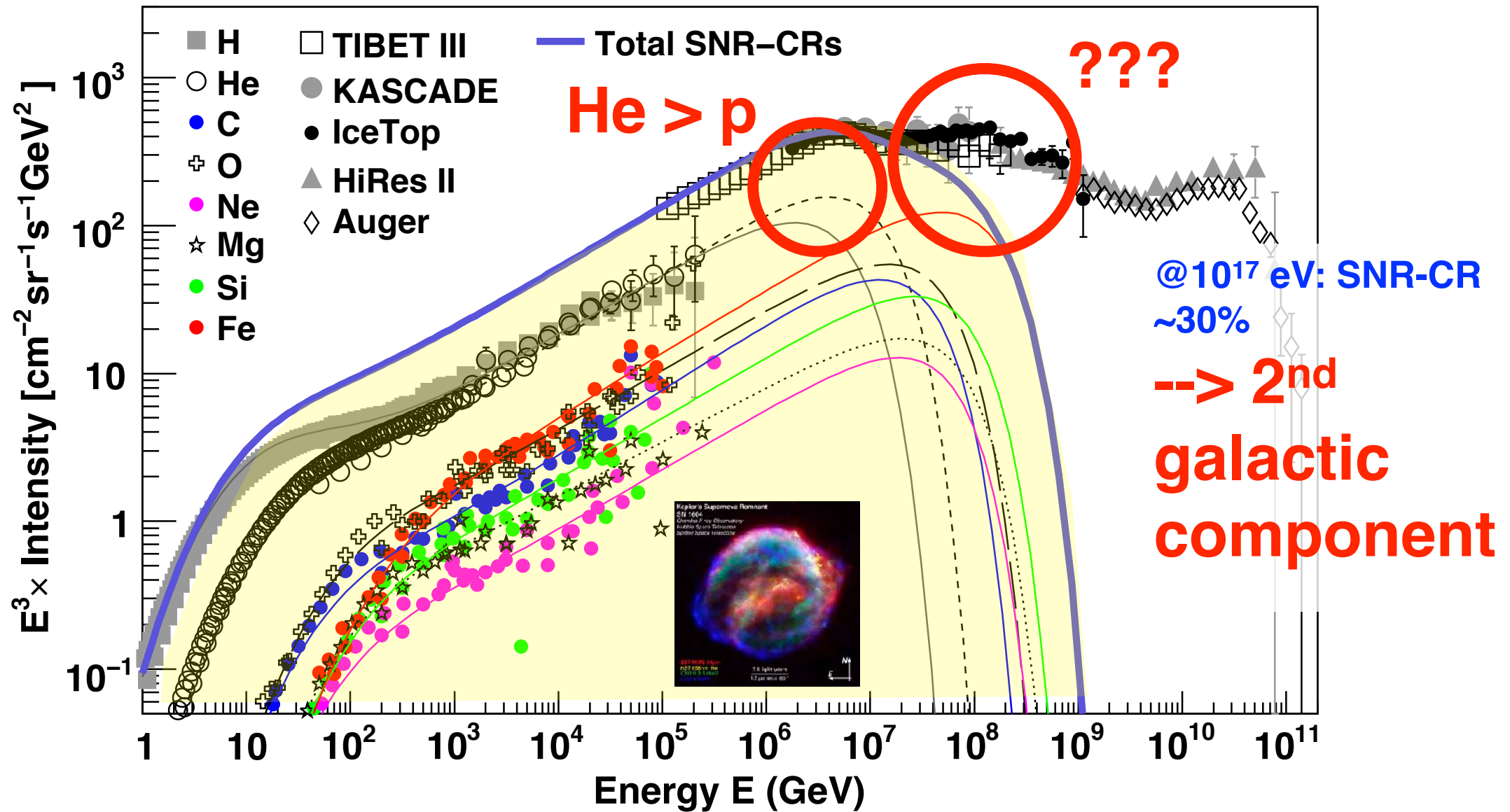
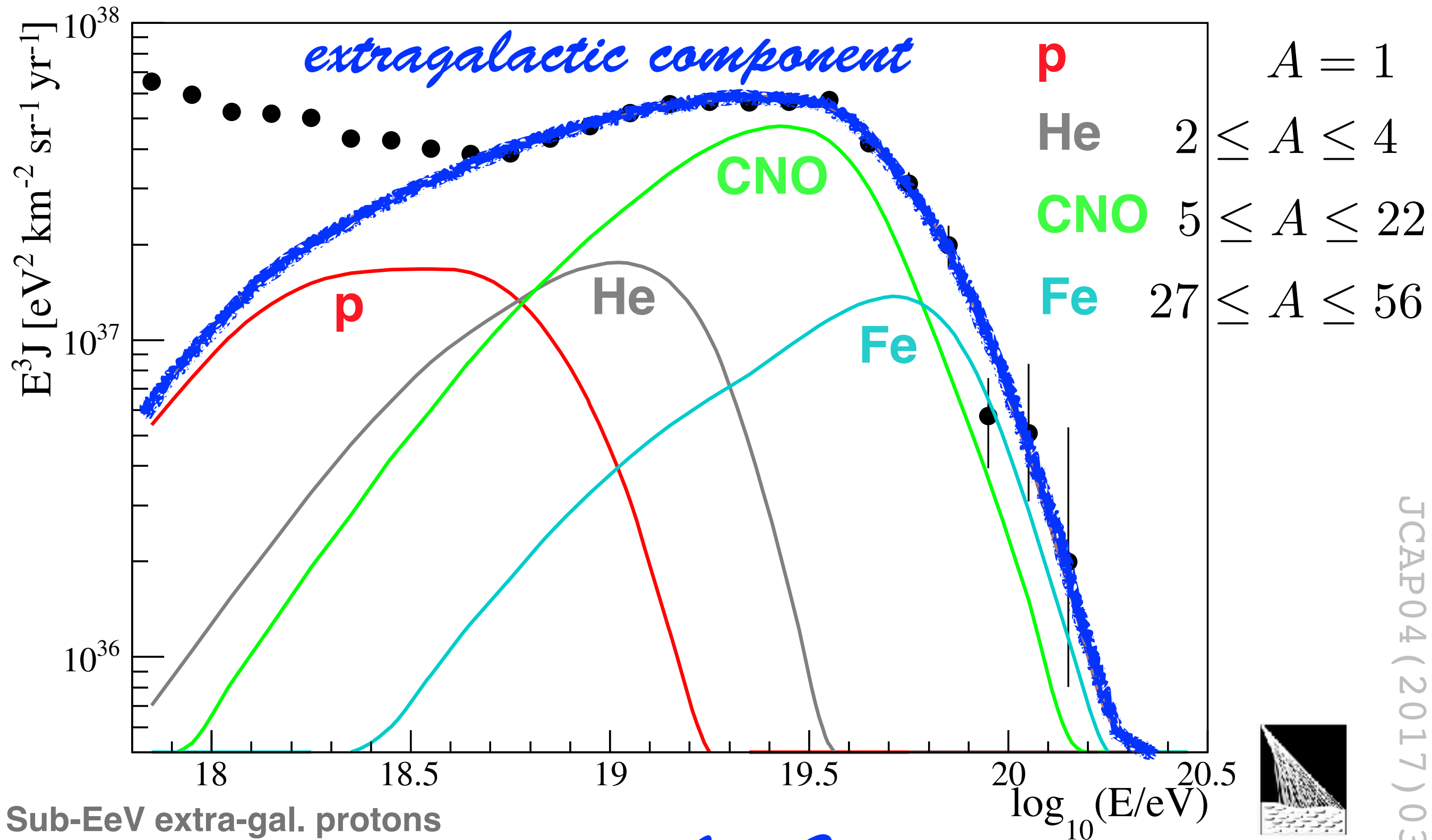


Fig. 2. Contribution of SNR-CRs to the all-particle cosmic-ray spectrum. The thin lines represent spectra for the individual elements, and the thick-solid line represents the total contribution. The calculation assumes an exponential cut-off energy for protons at $E_c = 4.5 \times 10^6$ GeV. Other model parameters, and the low-energy data are the same as in Figure 1. Error bars are shown only for the proton and helium data. High-energy data: KASCADE (Antoni et al. 2005), IceTop (Aartsen et al. 2013), Tibet III (Amenomori et al. 2008), the Pierre Auger Observatory (Schulz et al. 2013), and HiRes II (Abbasi et al. 2009).

~8% of mechanical power of SN --> CRs

Combined fit of spectrum and
composition data as measured by the
Pierre Auger Observatory



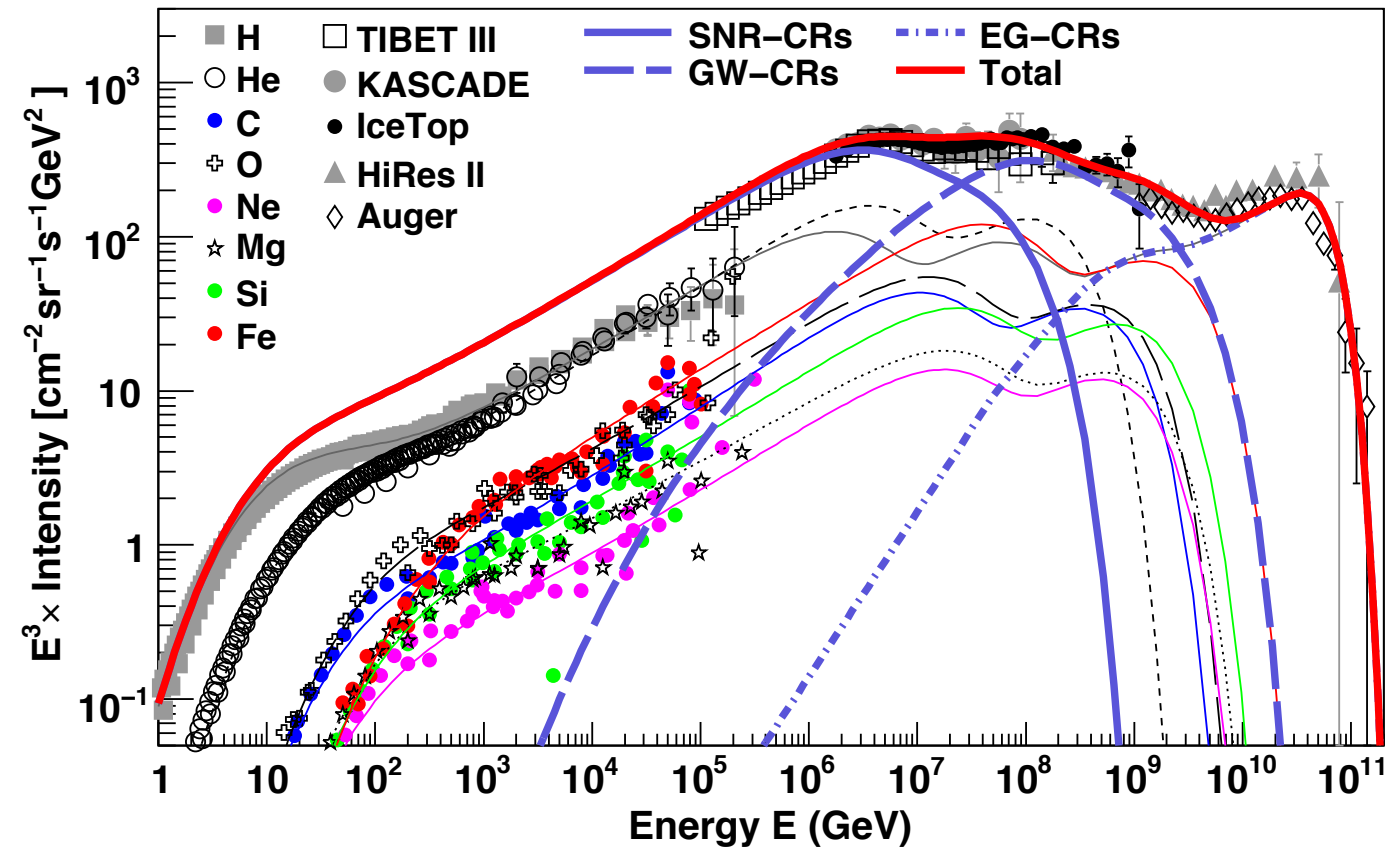
Sub-EeV extra-gal. protons
from interactions of heavier
nuclei

see A. Castellina

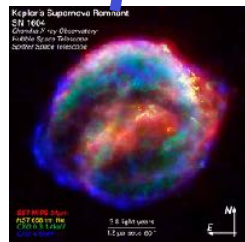
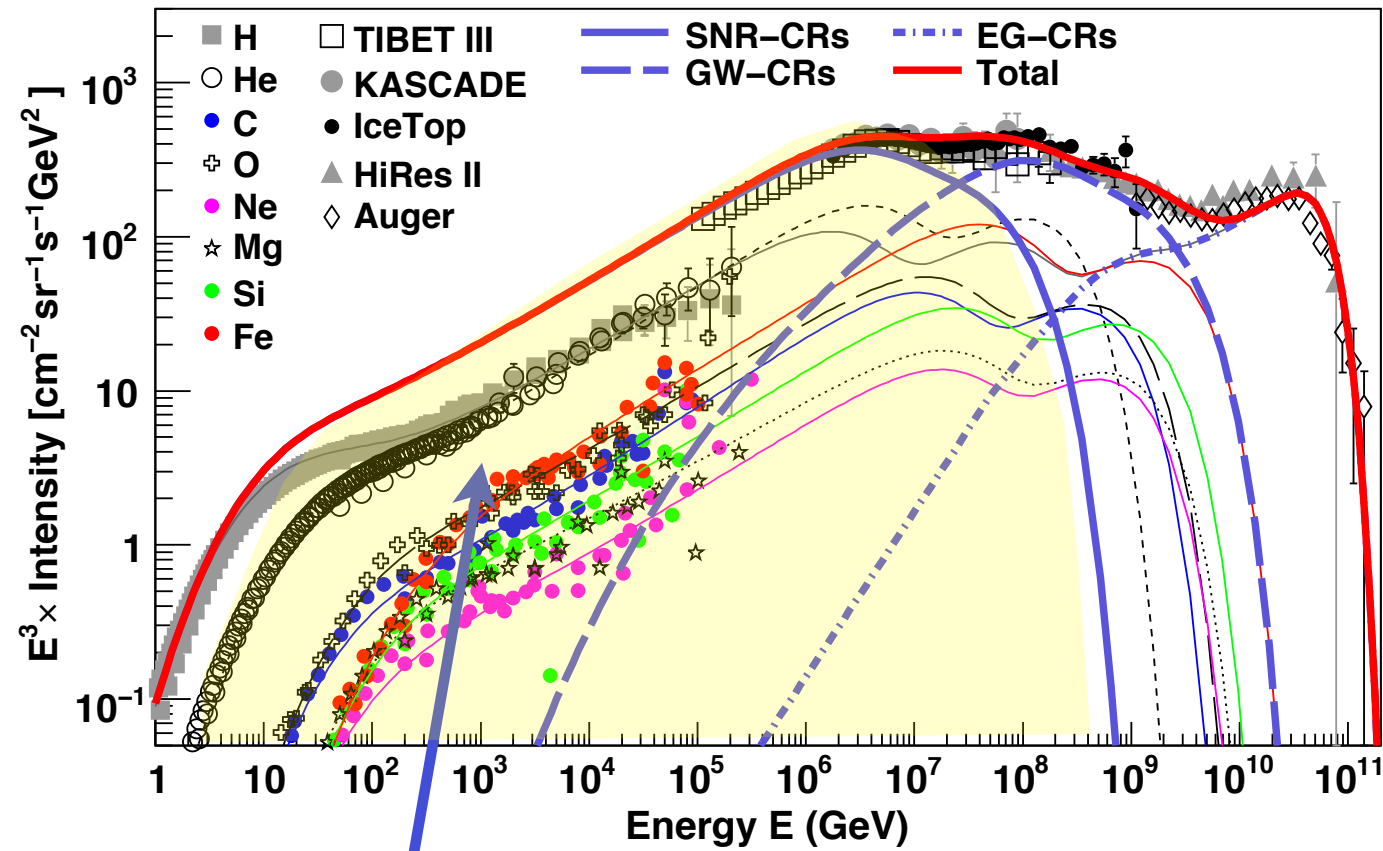


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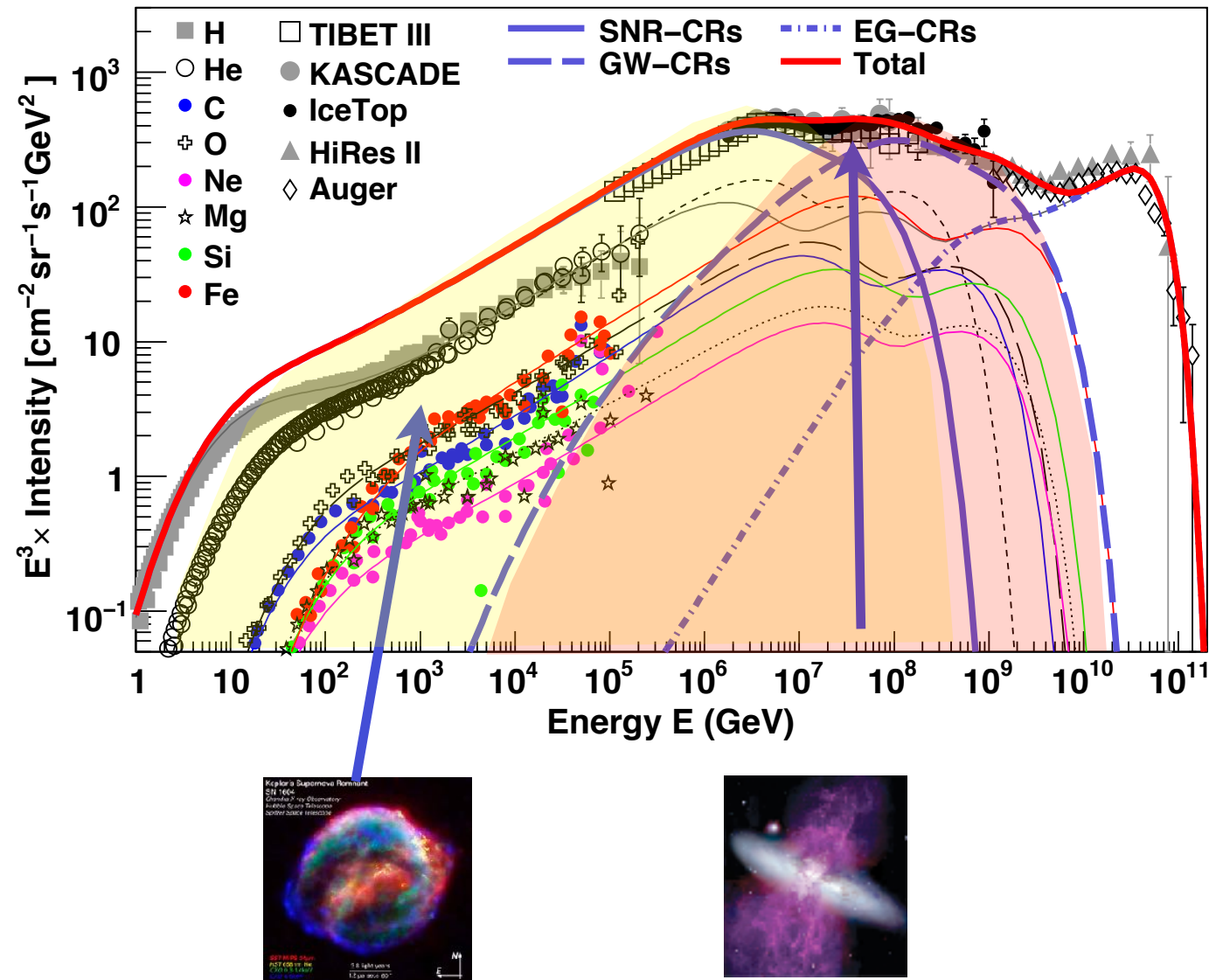
all-particle spectra including 2nd galactic component



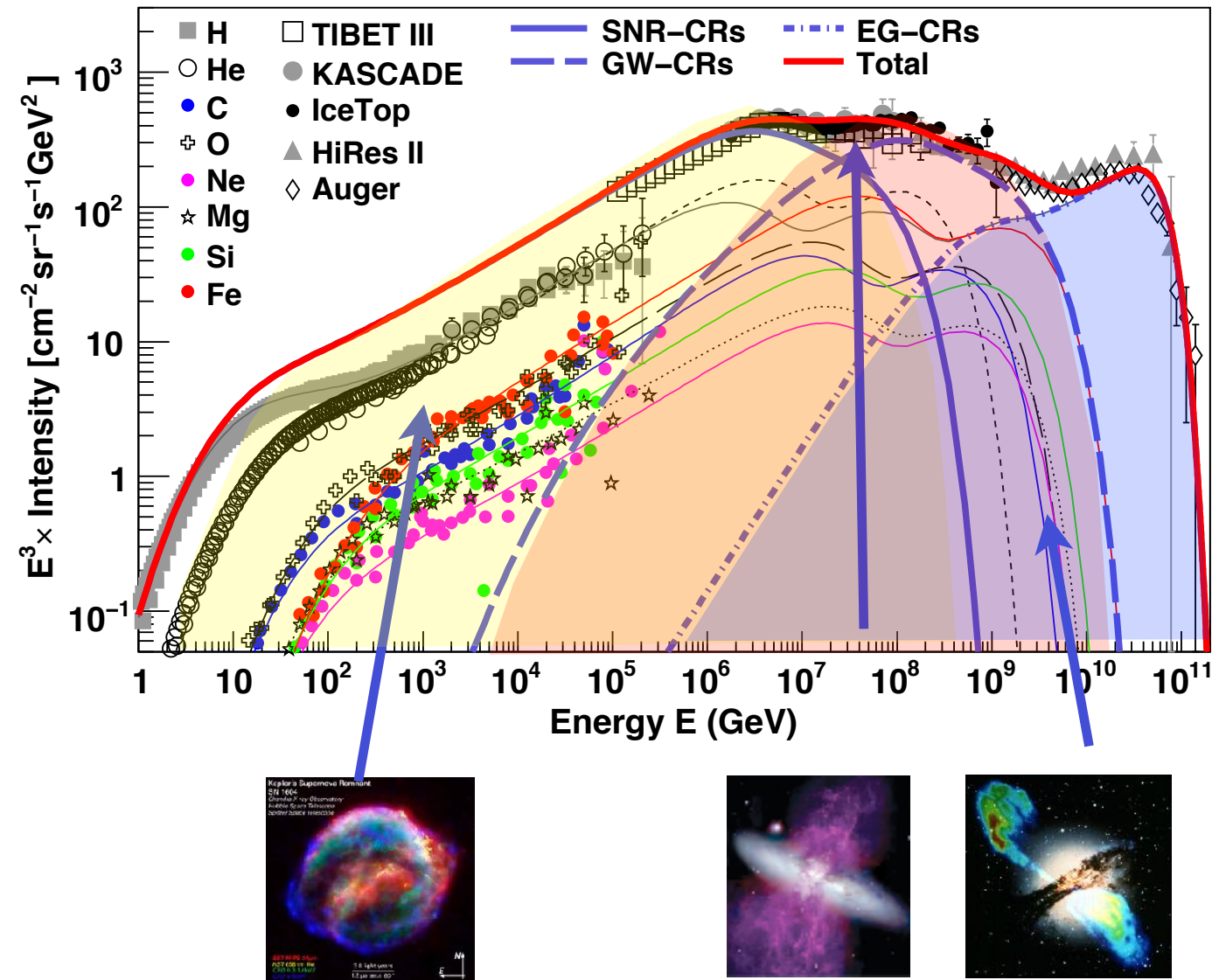
all-particle spectra including 2nd galactic component



all-particle spectra including 2nd galactic component



all-particle spectra including 2nd galactic component



all-particle spectra including 2nd galactic component

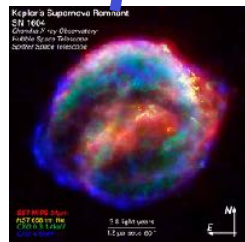
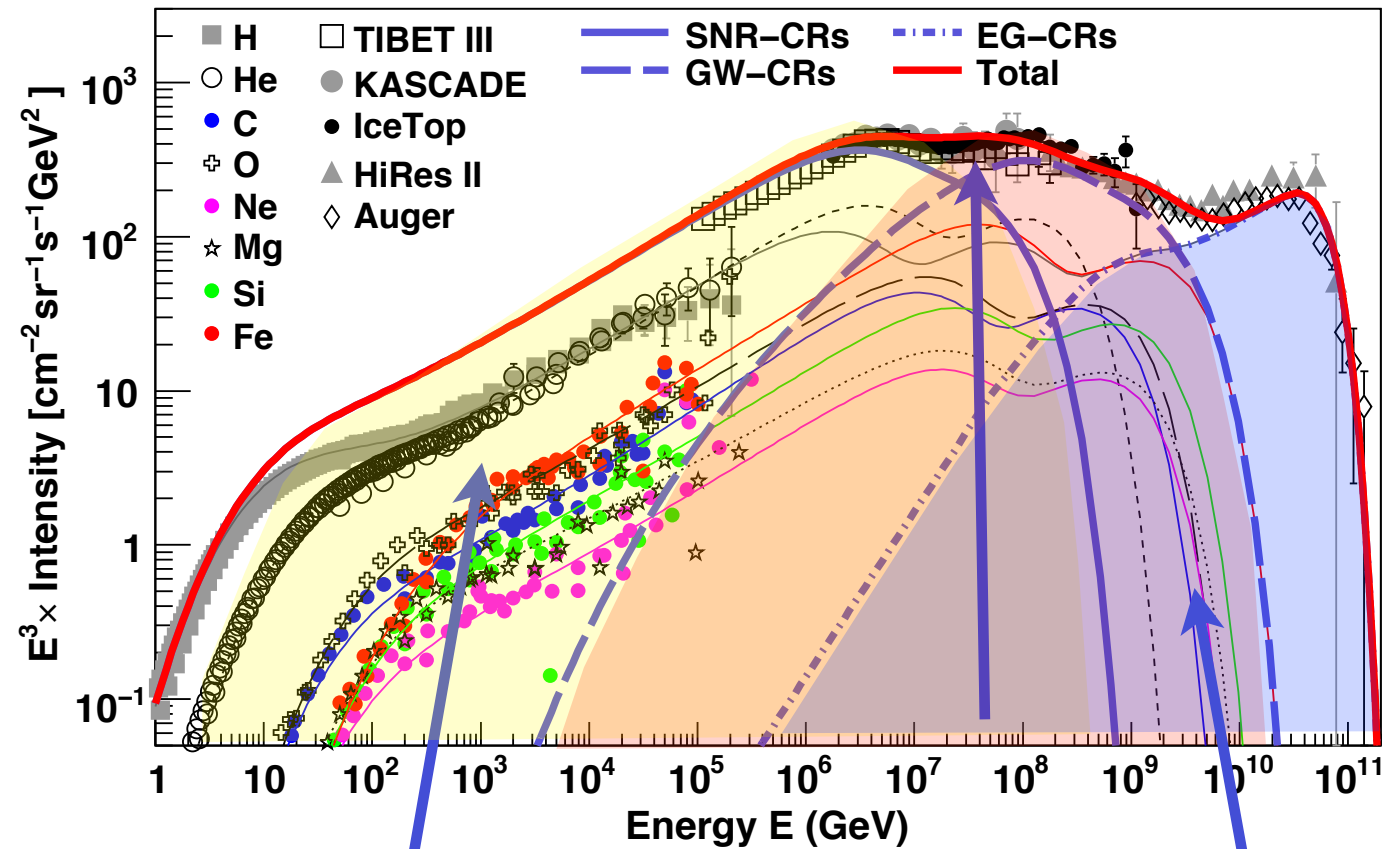
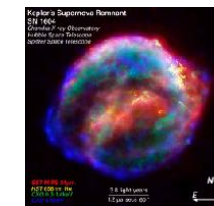
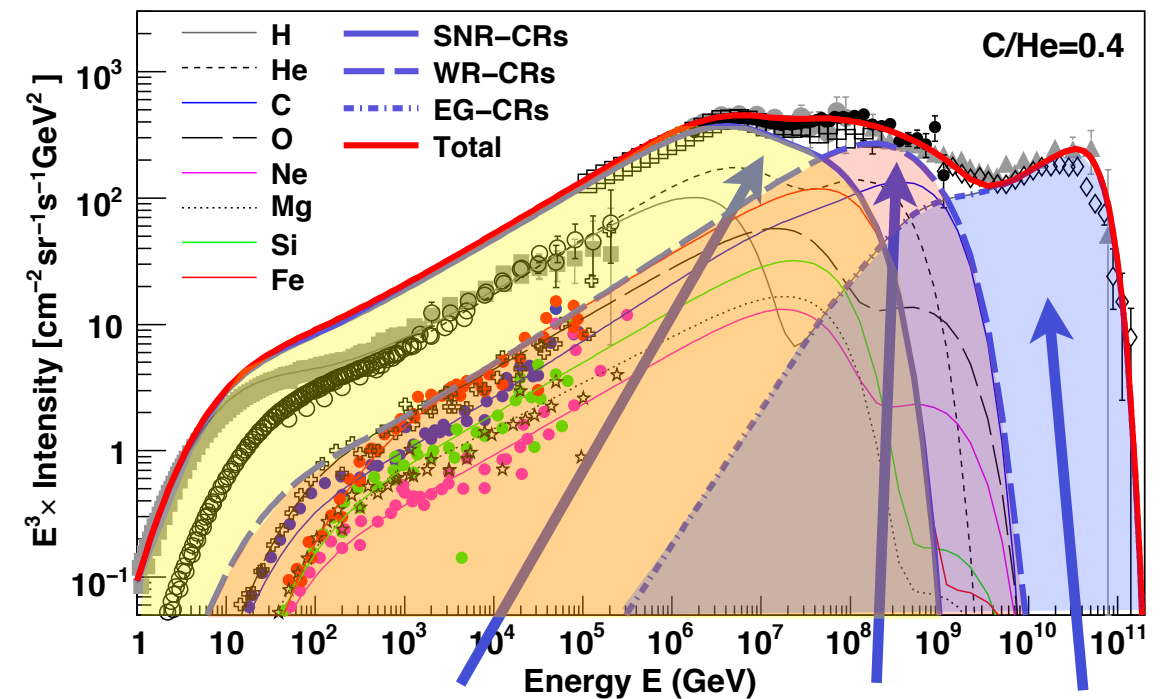
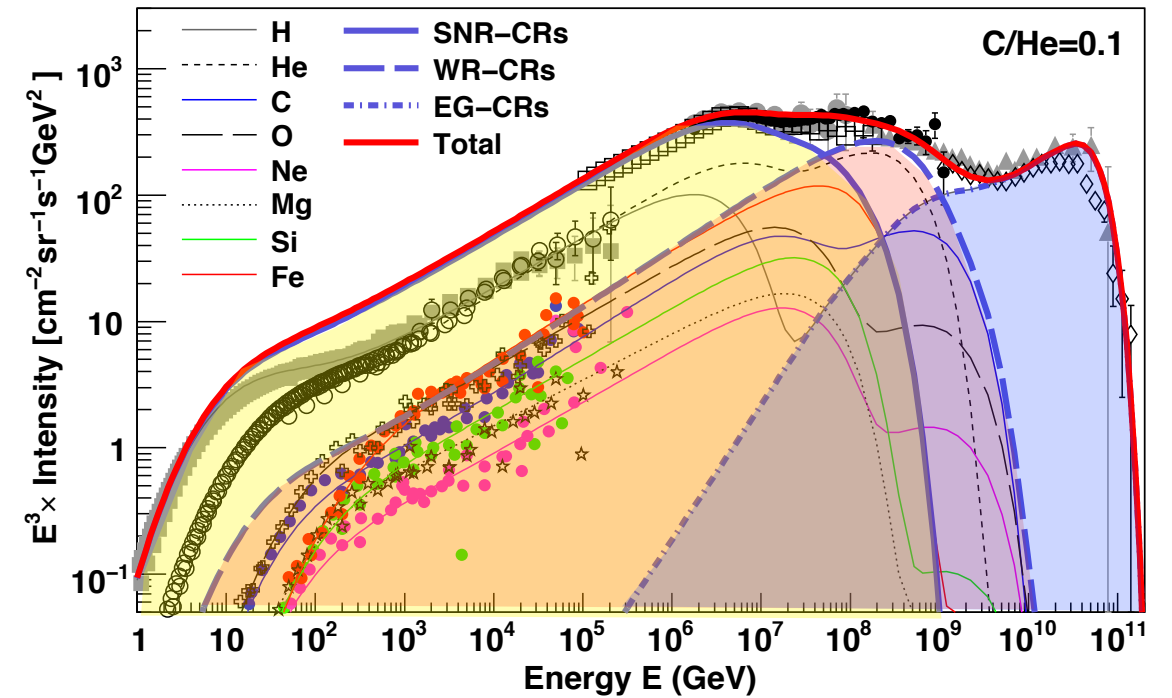


Table 3. Injection energy of SNR-CRs used in the calculation of all-particle spectrum in the WR-CR model (Figure 6).

Particle type	C/He = 0.1 $f(\times 10^{49} \text{ ergs})$	C/He = 0.4 $f(\times 10^{49} \text{ ergs})$
Proton	8.11	8.11
Helium	0.67	0.78
Carbon	2.11×10^{-2}	0.73×10^{-2}
Oxygen	2.94×10^{-2}	2.94×10^{-2}
Neon	4.41×10^{-3}	4.41×10^{-3}
Magnesium	6.03×10^{-3}	6.03×10^{-3}
Silicon	5.84×10^{-3}	5.84×10^{-3}
Iron	5.77×10^{-3}	5.77×10^{-3}



all-particle spectra including 2nd galactic component

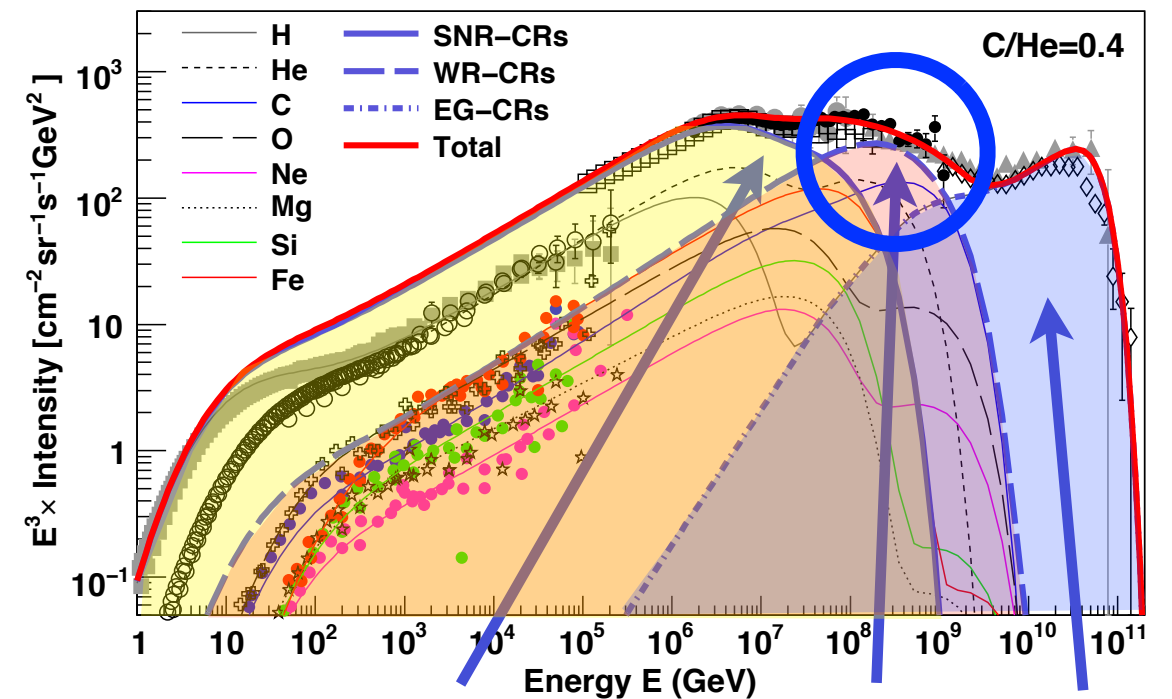
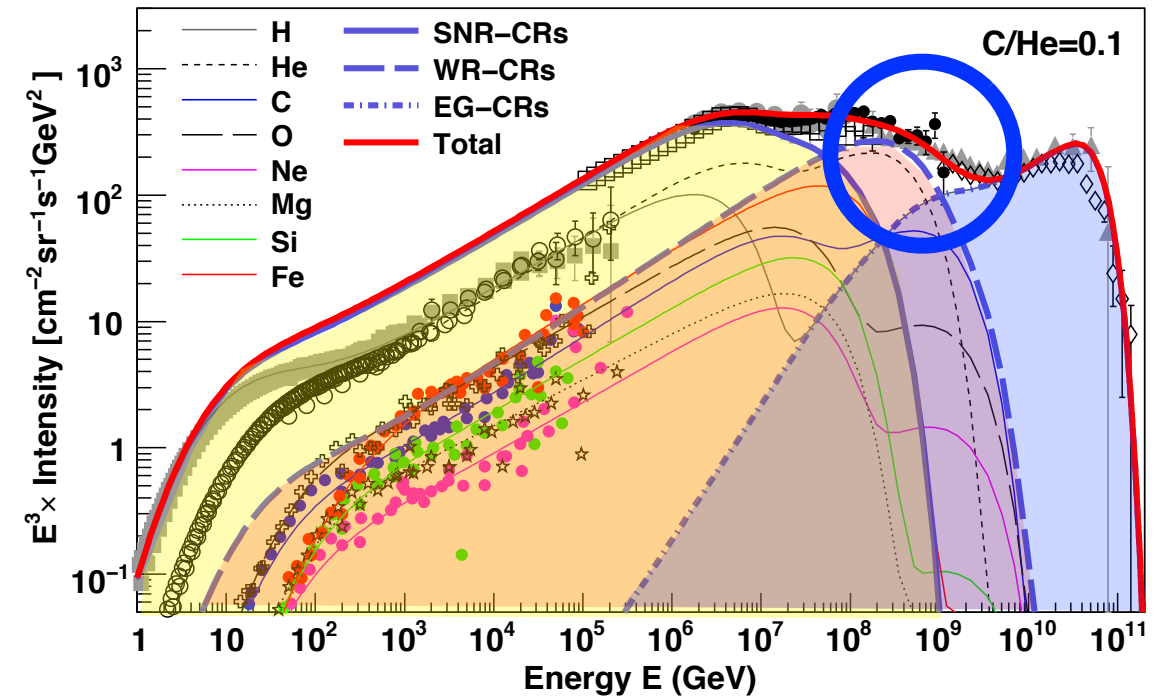
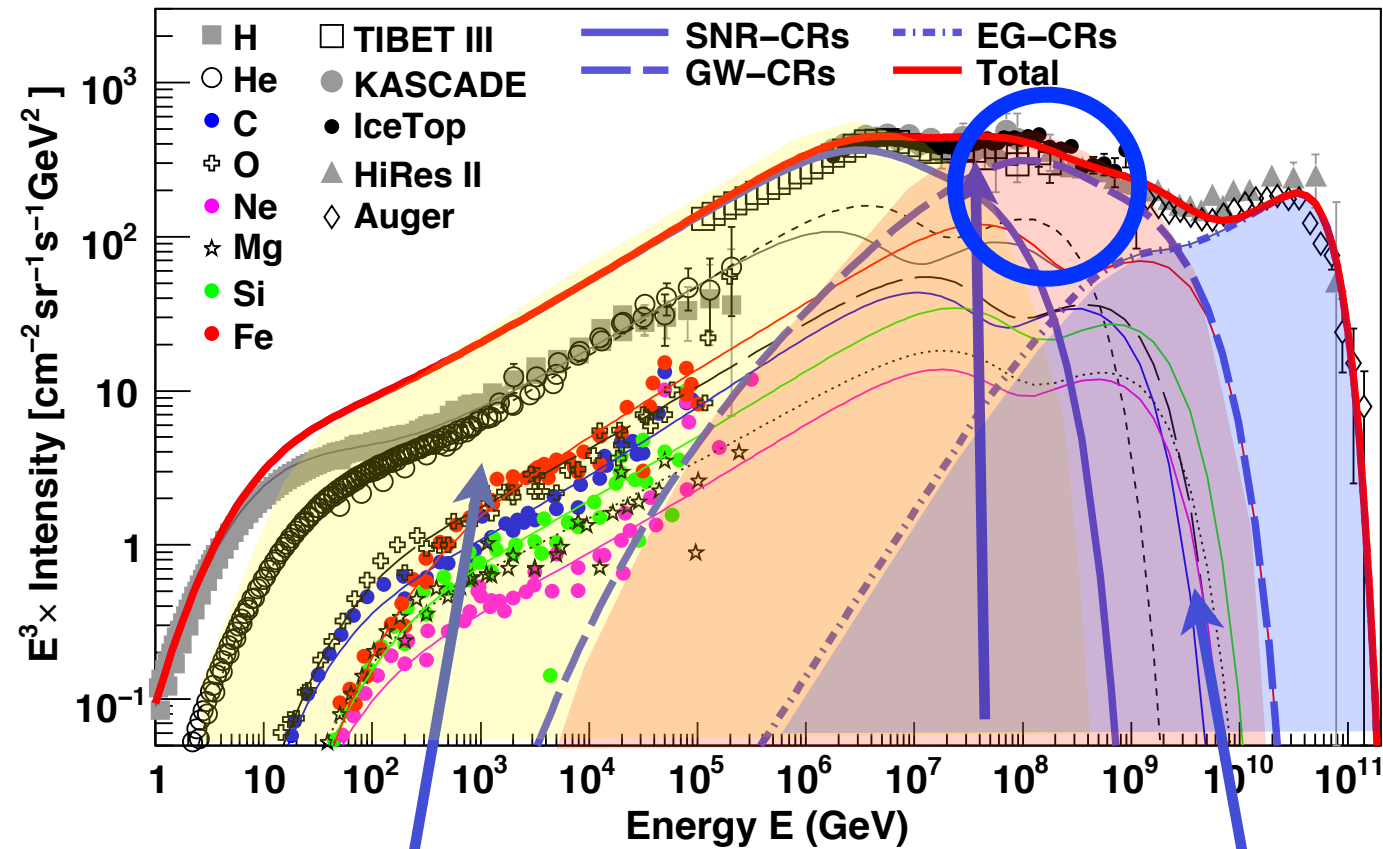


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Mean logarithmic mass ($\ln A$)

WR-CR (C/He=0.4) + EG scenarios

$$\langle \ln A \rangle \equiv \sum_i r_i \ln A_i, \quad \langle \ln A \rangle = \frac{X_{\max}^{\text{meas}} - X_{\max}^p}{X_{\max}^{\text{Fe}} - X_{\max}^p} \cdot \ln A_{\text{Fe}}.$$

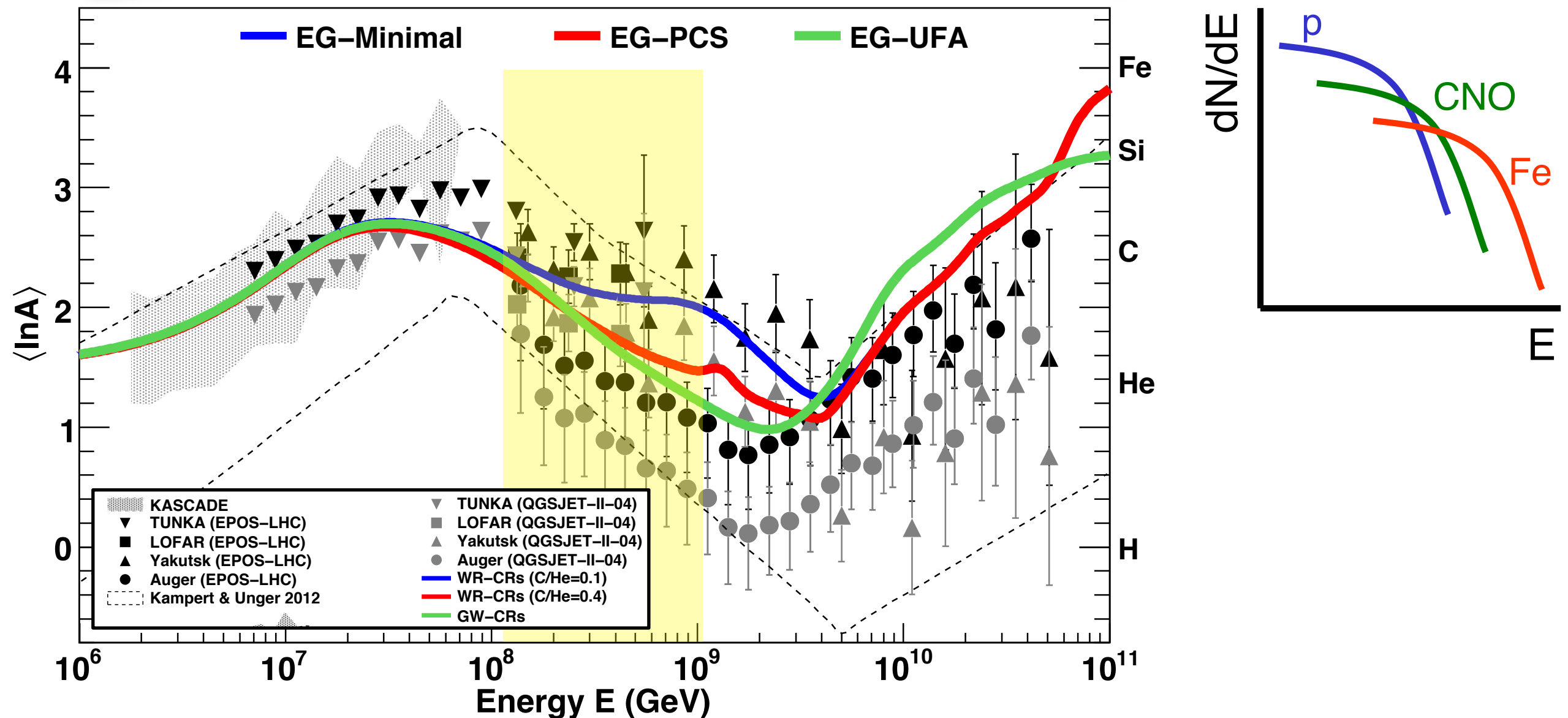


Fig. 11. Mean logarithmic mass for the three different EG-CR models combined with the WR-CR (C/He = 0.4) model. Data are the same as in Figure 8. Results obtained using WR-CR (C/He = 0.1) model are shown in Appendix B.

Cosmic rays at the knee

Results and implications

- knee in all-particle spectrum at ~ 4.5 PeV caused by fall-off of light elements (p, He)
- experimental (world) data indicate rigidity-dependent fall-off of individual elements
(in particular unfolding by KASCADE[-Grande] and IceCube/Top)
- spectrum above knee is superposition of individual spectra (elemental knees)
 - > fine structure in all-particle spectrum
 - > end of galactic CR component
- astrophysical origin of knee:
combination of maximum energy attained in sources (Supernovae) (Hillas criterion)
and leakage from Galaxy
- 2nd galactic component at $\sim 10^{17}$ eV?
- extra-galactic origin $> 10^{18}$ eV



Nikhef

