

Analytical fits for parameter estimation of inspiralling MBH binaries in LISA

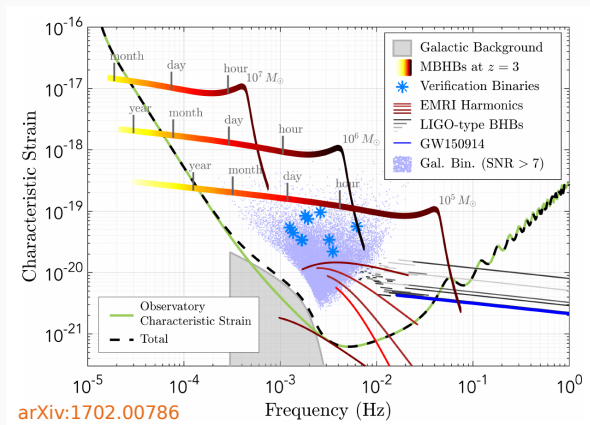
Alberto Mangiagli

In collaboration with: Antoine Klein, Matteo Bonetti, Alberto Sesana, Michael Katz, Sylvain Marsat, Stanislav Babak, Marta Volonteri, Monica Colpi

Università degli Studi di Milano-Bicocca

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Overview



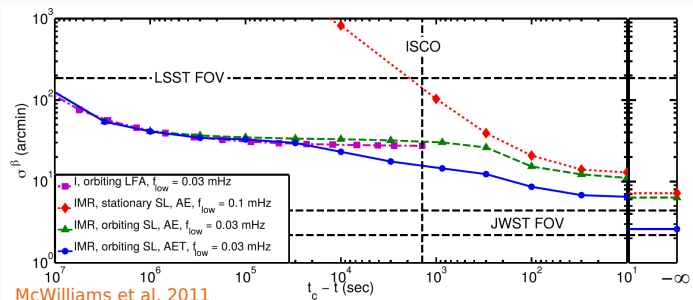
MBHBs are key sources for Multi-Messenger Astrophysics

- Detected weeks prior coalescence → early warnings
- Likely occurring in gas-rich environment → EM counterparts
- At least $\simeq 10$ events per year expected → statistics

Parameter estimation

Science outcomes depends on LISA ability to estimate source parameters

- MCMC** (Babak et al.2010, Marsat et al.2020)
 - Bayesian formalism
 - Computational expensive \rightarrow few selected cases
- Fisher matrix** (Lang&Hughes 2008, Kocsis et al.2008, Klein et al.2016)
 - Reproduce MCMC results only in the high-SNR limit
 - Computational cheap \rightarrow large parameter space



Problems

- old LISA design in past inspiral studies
- Both methods require large set of simulations

Aims (AM et al. 2020, in preparation)

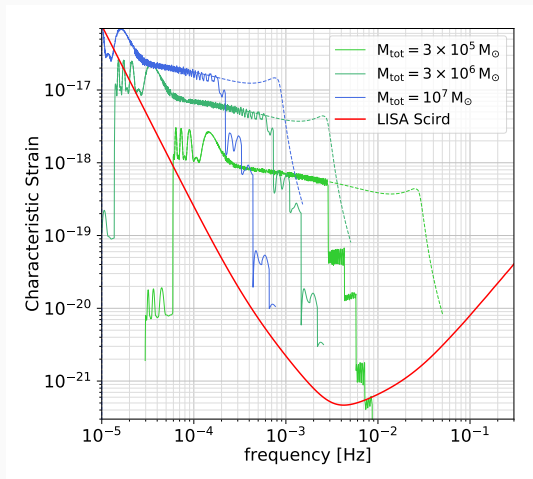
- Performance of current LISA design for '*on the fly*' estimates
- Analytical formulae to describe how parameter estimates improve during the inspiral $\rightarrow \Delta\Omega = \mathcal{F}(t_c, M_{\text{tot}}, z)$?

Parameter space

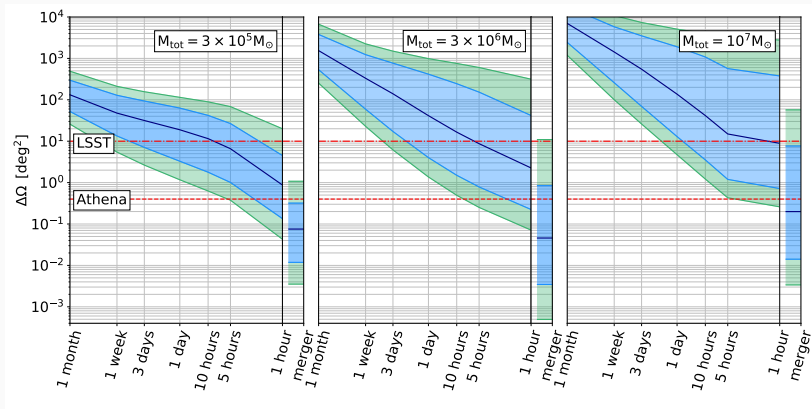
- $M_{\text{tot}} = 10^5, 3 \times 10^5, 5 \times 10^5, 7.5 \times 10^5, 10^6, \dots, 3 \times 10^7 M_{\odot}$
- $z = 0.1, 0.3, 0.5, 1, 2, 3, 4$
- 1 month, 1 week, 3 days, 1 day, 10 hrs, 5, hrs and 1 hr from merger

Examples of simulated signals

- Fisher matrix with inspiral precessing waveform (Klein et al. 2014)
- PhenomC to rescale $\Delta\Omega$ at merger



Sky position uncertainties at $z = 1$



$\Delta\Omega \simeq$ telescope FOV only **close to merger**
}

< 10 hrs

LSST

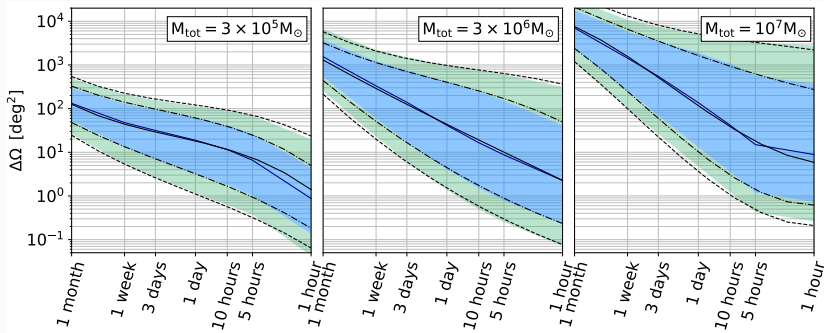
merger

Athena

Large distributions \rightarrow strong dependence from true binary position

Analytical fits

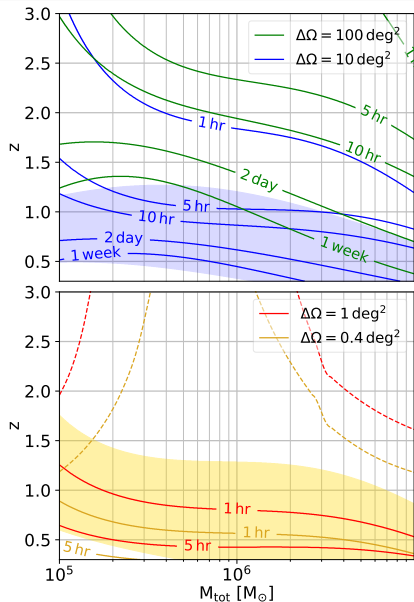
Few input parameters \rightarrow Time left before merger, M_{tot} and z



$$\text{Fits for } \begin{cases} M_{\text{tot}} \in [10^5, 10^7] M_{\odot} \\ z \in [0.3, 3] \end{cases}$$

Also for luminosity distance, chirp mass and mass-ratio

Time left before merger



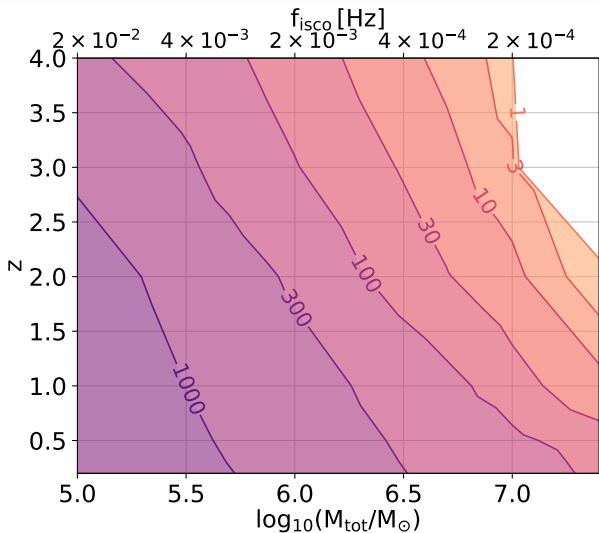
For $M_{\text{tot}} = 10^6 M_{\odot}$:

- $10 \text{ deg}^2 \begin{cases} 5 \text{ hrs} & \rightarrow z < 1 \\ 1 \text{ week} & \rightarrow z < 0.5 \end{cases}$
- $100 \text{ deg}^2 \begin{cases} 5 \text{ hrs} & \rightarrow z \lesssim 2.4 \\ 1 \text{ week} & \rightarrow z < 1 \end{cases}$

For all masses:

- $\Delta\Omega < 1 \text{ deg}^2$ close to merger
- Large uncertainties

Number of cycles from detection ...



Parameter estimation 'on the fly' for LISA MBHBs:

- Adopted LISA current design
- Sky localization uncertainties (also for d_L , chirp mass and mass-ratio)
- Sky uncertainties \simeq telescopes FOV only close to merger but large uncertainties
- compare few cases with MCMC simulations (work in progress)

Analytical fits for parameter estimates

- Valid for $M_{\text{tot}} \in [10^5, 10^7] M_{\odot}$ and $z \in [0.3, 3]$
- Independent fits for uncertainties at merger
- fits also for d_L , chirp mass and mass-ratio
- Release data

Thanks