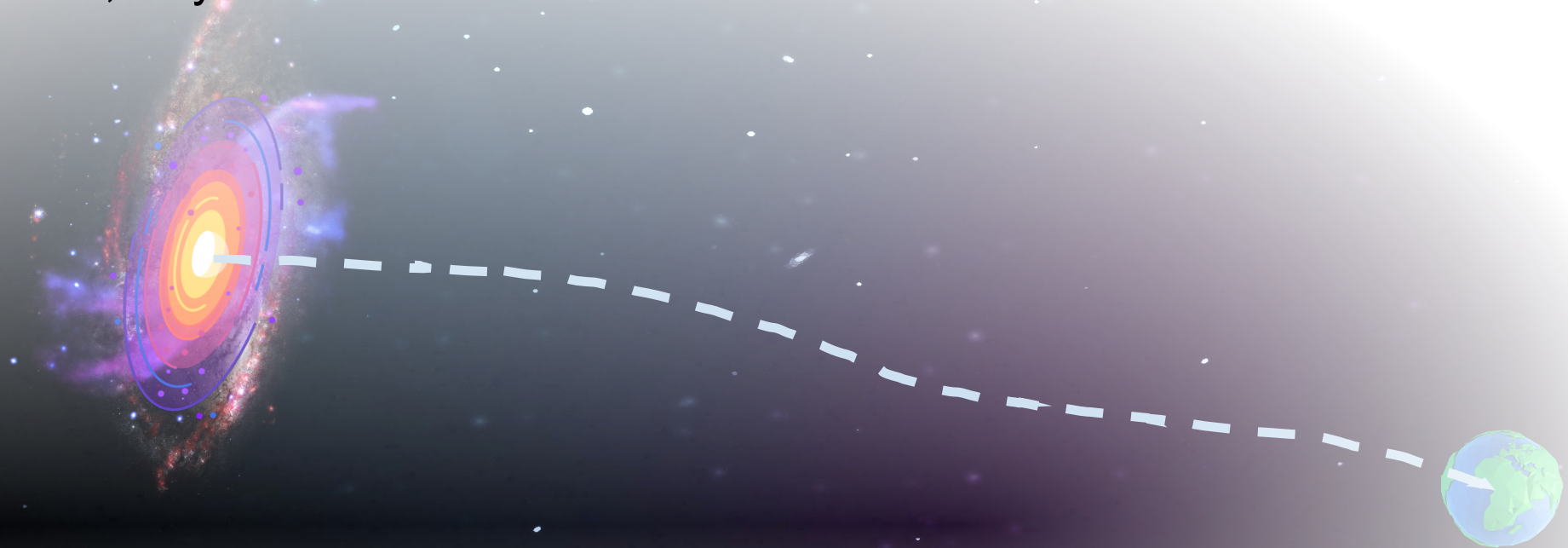


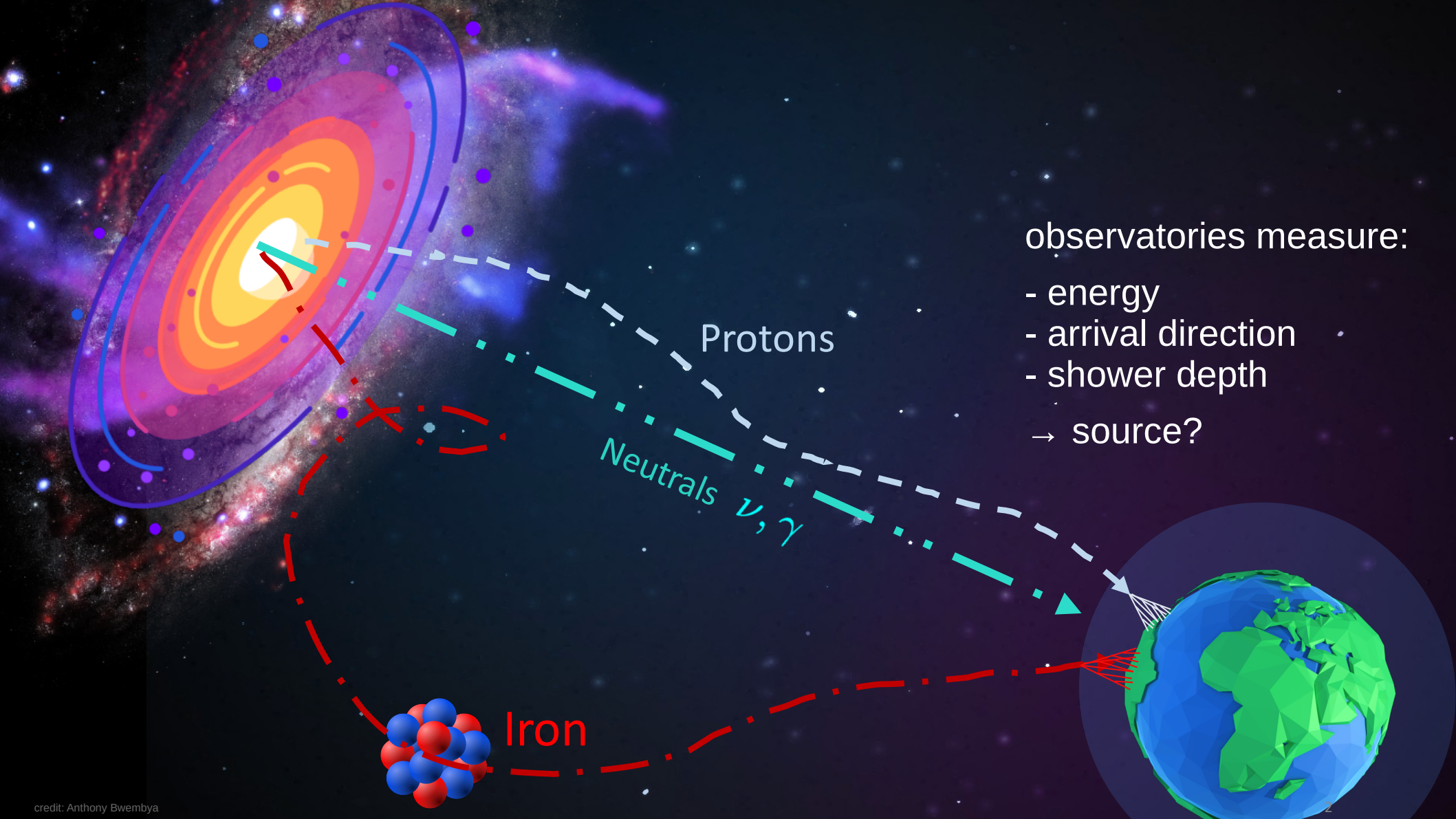
Sources of ultra-high-energy cosmic rays and how to infer them from data

Teresa Bister

Erice, July 2024

Radboud University





observatories measure:

- energy
 - arrival direction
 - shower depth
- source?

Modeling UHECRs from sources to detection

source distribution

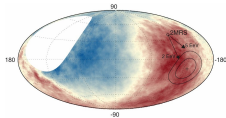
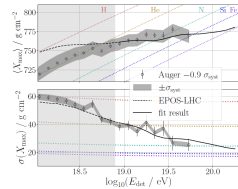
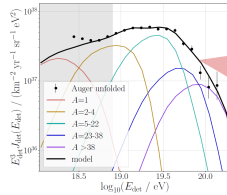


model

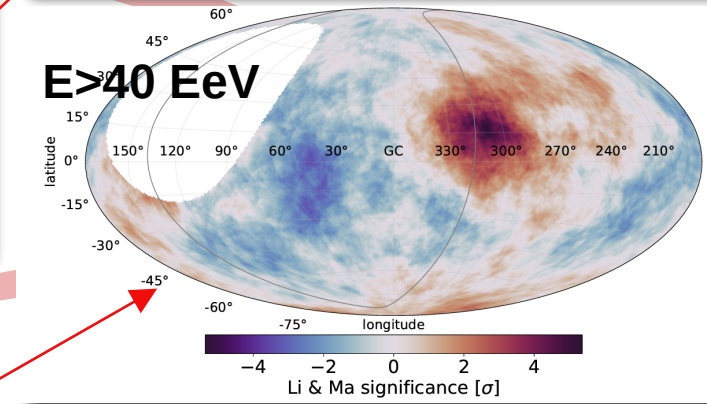
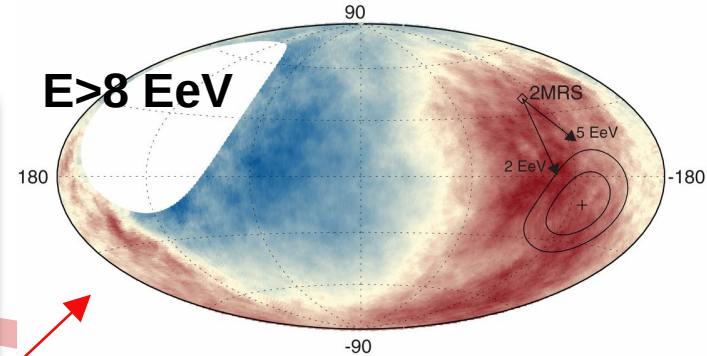
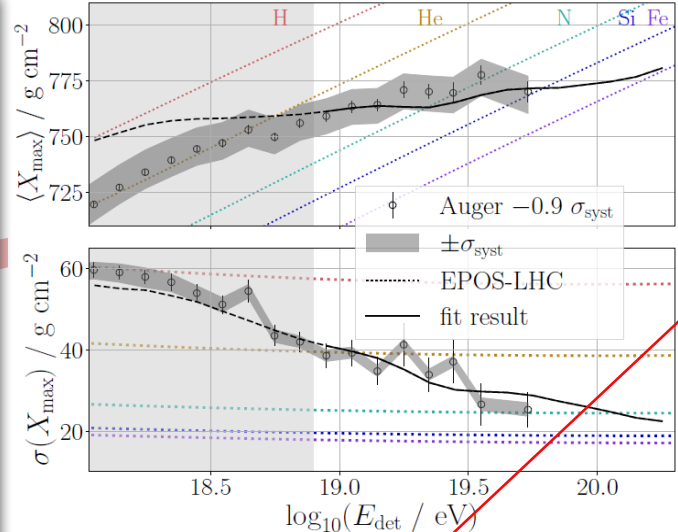
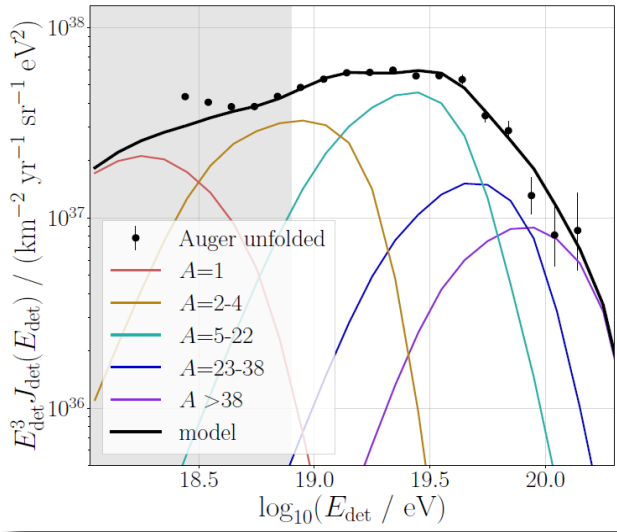
parameter inference

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



Modeling UHECR sources



compare to data

- energy spectrum
- mass composition (often X_{max})
- arrival directions (events or large-scale / smaller scale anisotropies or correlations)
- (multimessenger)

Modeling UHECRs from sources to detection

source distribution

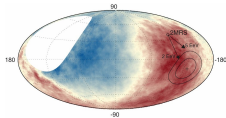
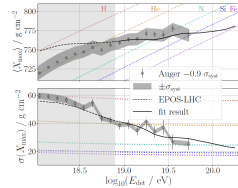
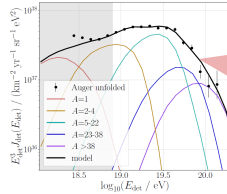


model

parameter inference

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)

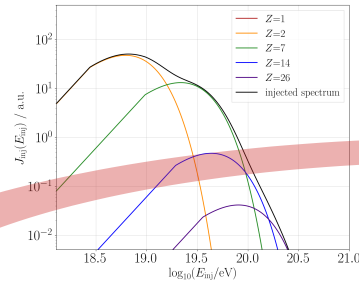


Modeling UHECRs from sources to detection

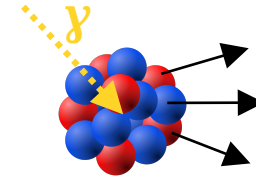
source distribution



injection

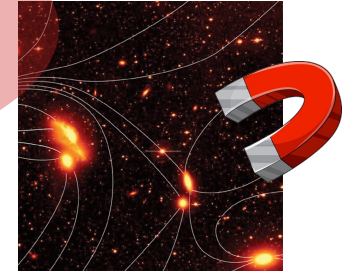


propagation through extragalactic space



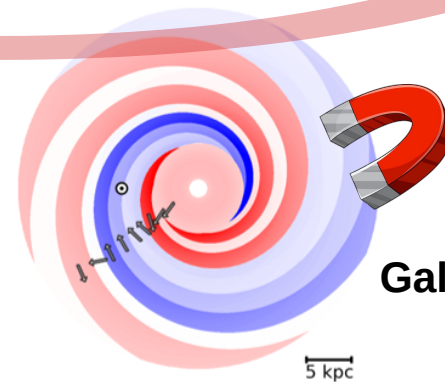
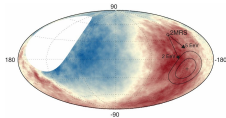
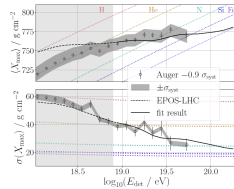
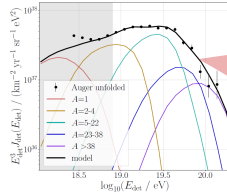
SimProp
SIRENTE
CR/Propa

extragalactic magnetic fields



compare to data

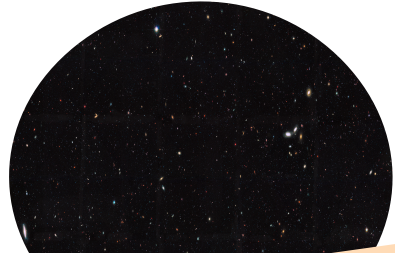
- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



Galactic magnetic fields

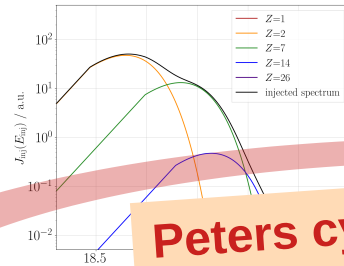
Combined fit of spectrum and composition

source distribution



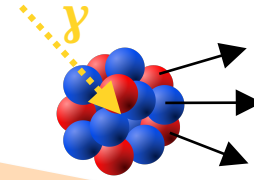
homogeneous

injection



Peters cycle

propagation through extragalactic space



1-dimensional

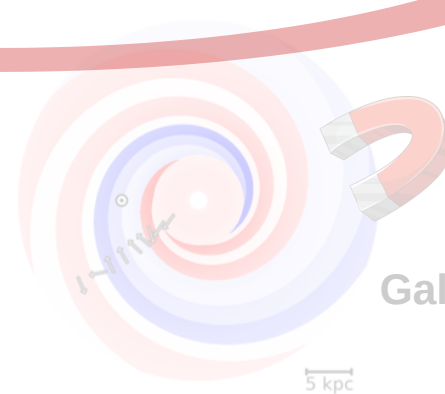
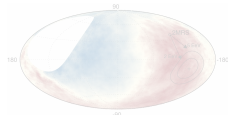
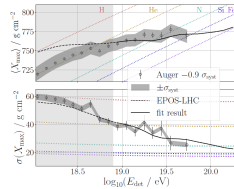
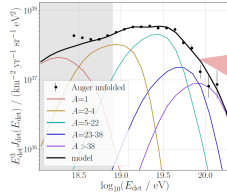


extragalactic magnetic fields



compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)

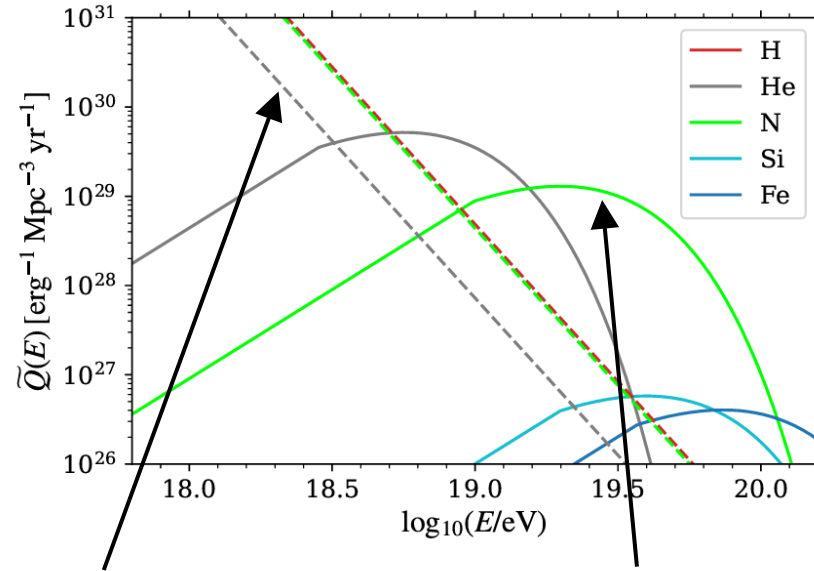
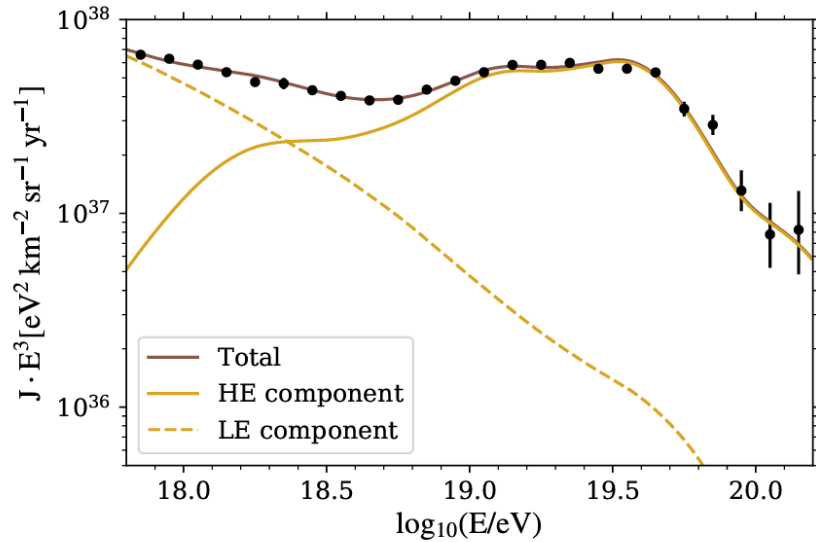


Galactic magnetic fields

Combined fit of spectrum and composition

- two populations of homogeneous sources
- Peters cycle injection

$$\tilde{Q}_A(E) = \underbrace{\tilde{Q}_{0A}}_{\text{element contributions}} \left(\frac{E}{E_0} \right)^{\underbrace{-\gamma}_{\text{spectral index}}} \begin{cases} 1, & E \leq Z_A \underbrace{R_{\text{cut}}}_{\text{rigidity cutoff}} \\ \exp\left(1 - \frac{E}{Z_A R_{\text{cut}}}\right), & E > Z_A R_{\text{cut}} \end{cases}$$



low-energy component:

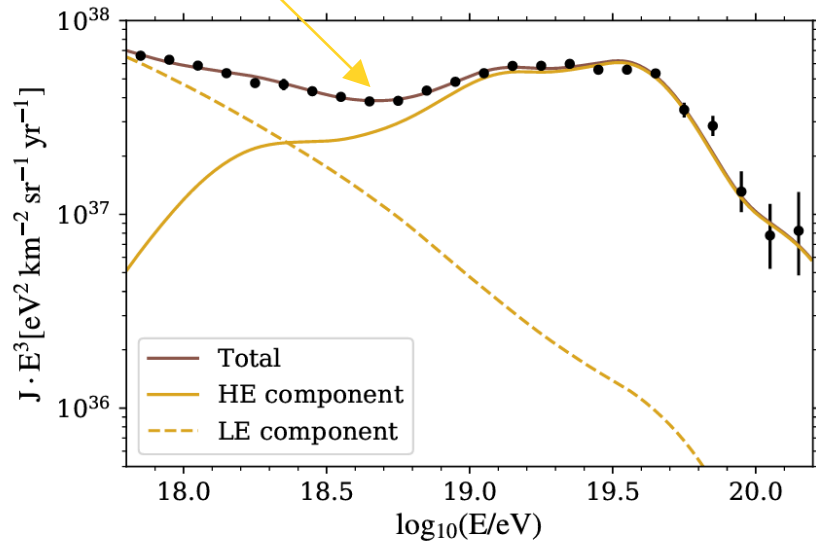
- He+N, very soft spectrum
- rigidity cutoff unconstrained

high-energy component:

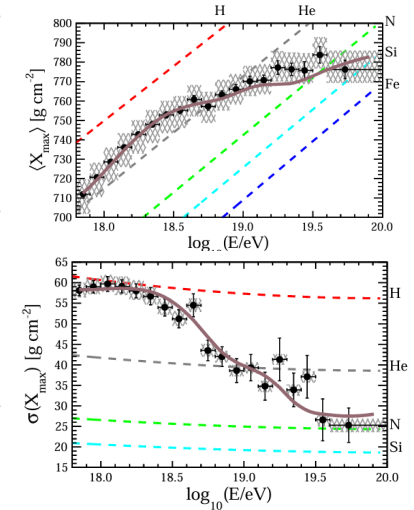
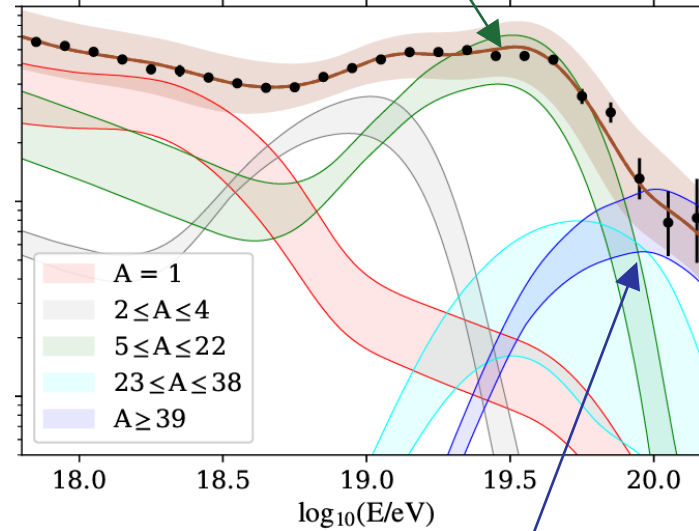
- very hard spectrum $\gamma < 0$
- low rigidity cutoff $O(1 \text{ EeV})$

Combined fit of spectrum and composition

ankle: transition between populations



conclusions stable with regards to systematic effects



composition becomes heavier → **no light elements at highest energies** 😞

➔ but, maybe secondaries from in-source interactions or another population, see e.g.

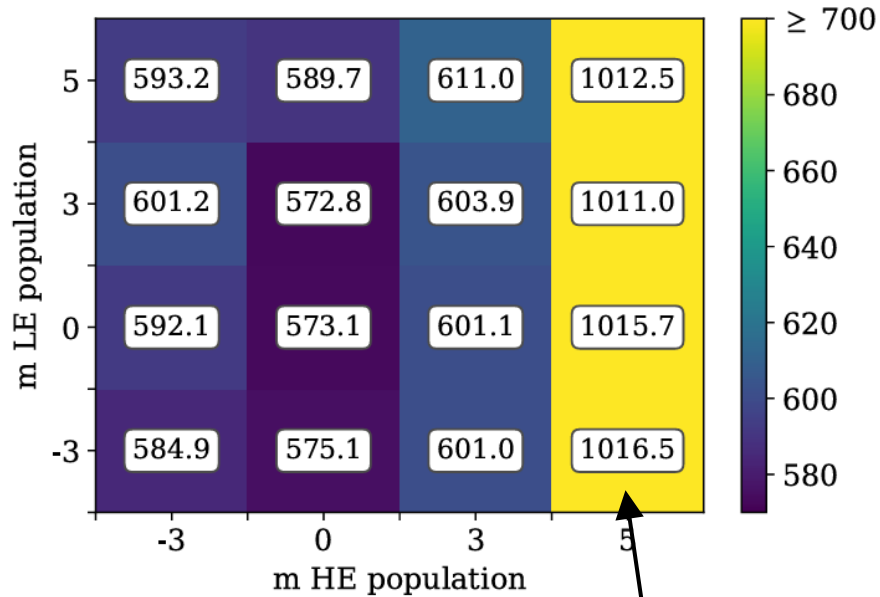
Unger, Farrar, Anchordoqui PRD 92 123001 (2015),

Muzio, Unger, Farrar PRD 100 103008 (2019)

Ehlert, van Vliet, Oikonomou, Winter JCAP 02 022 (2024) ...

Combined fit of spectrum and composition

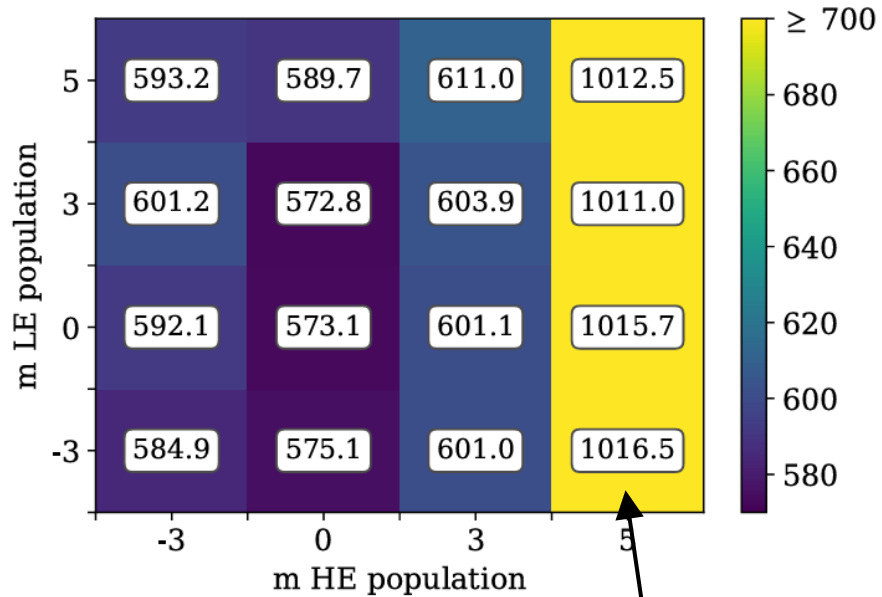
test cosmological source evolution $\psi(z) \propto (1+z)^m$



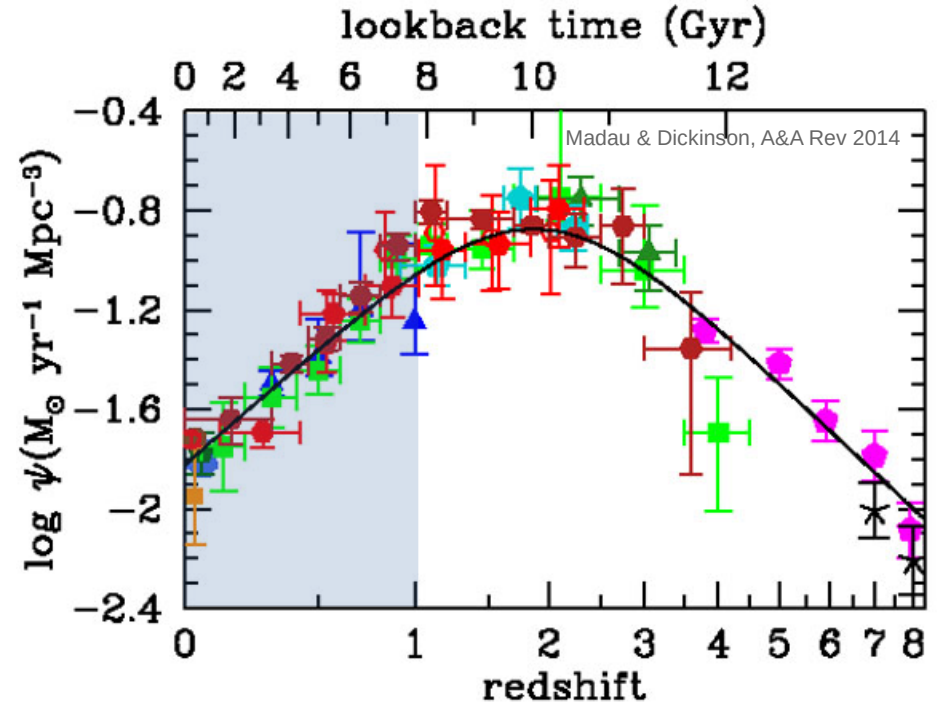
strong evolution of
high-energy population
disfavored

Combined fit of spectrum and composition

test cosmological source evolution $\psi(z) \propto (1+z)^m$

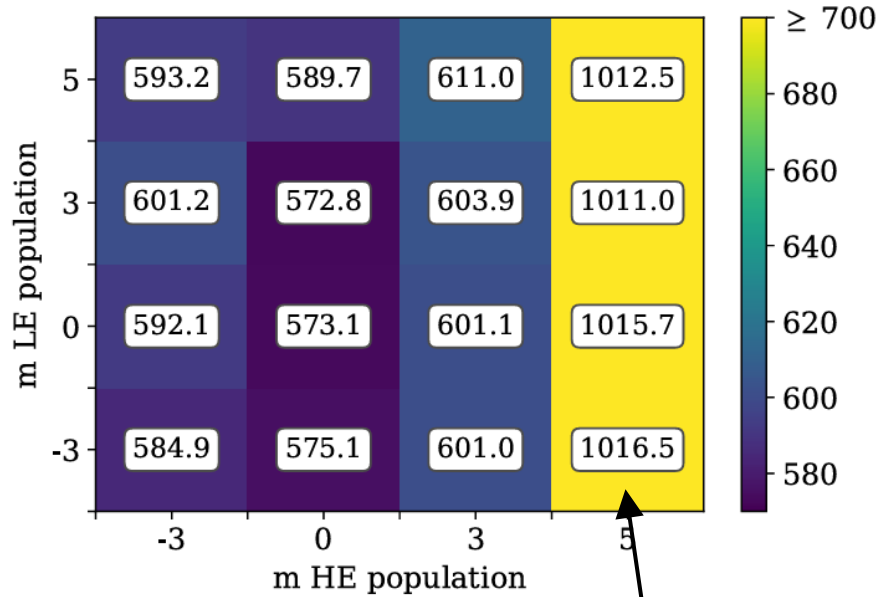


strong evolution of
high-energy population
disfavored

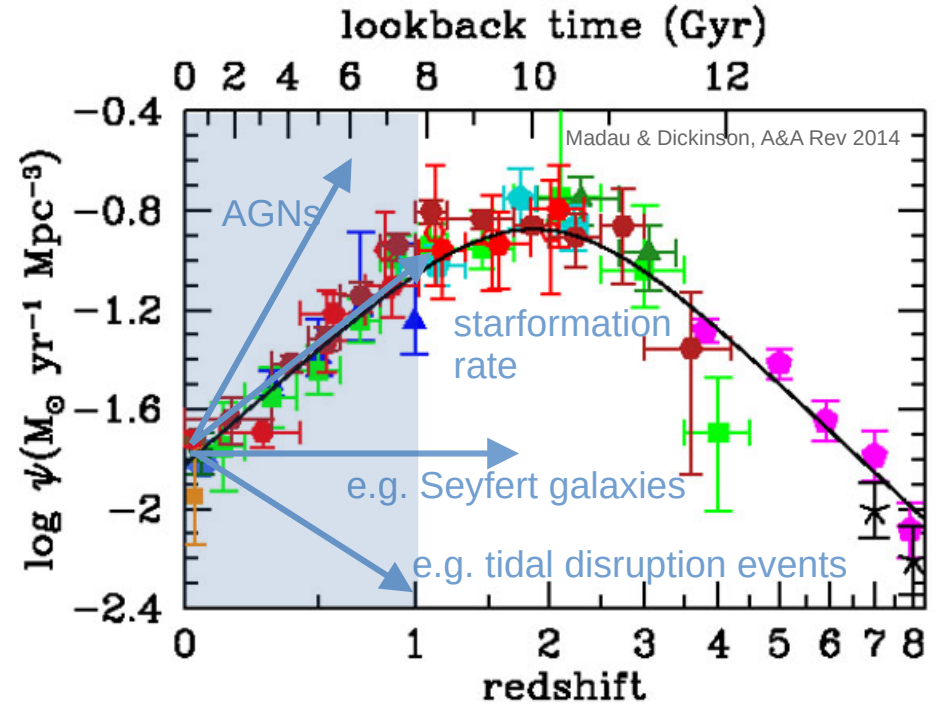


Combined fit of spectrum and composition

test cosmological source evolution $\psi(z) \propto (1+z)^m$



strong evolution of high-energy population disfavored



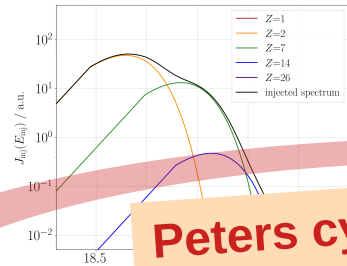
Variations of the injection at the source

source distribution



homogeneous

injection



Peters cycle

propagation through



SimProp
SIRENTE

Propa

spectral index

rigidity cutoff

$$\tilde{Q}_A(E) = \tilde{Q}_{0A} \left(\frac{E}{E_0} \right)^{-\gamma} \begin{cases} 1, & E \leq Z_A R_{\text{cut}} \\ \exp\left(1 - \frac{E}{Z_A R_{\text{cut}}}\right), & E > Z_A R_{\text{cut}} \end{cases}$$

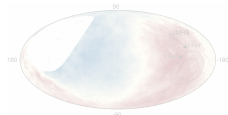
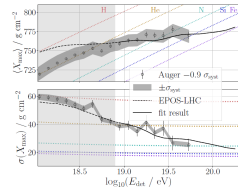
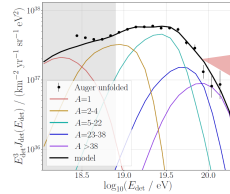
element contributions

extragalactic magnetic fields

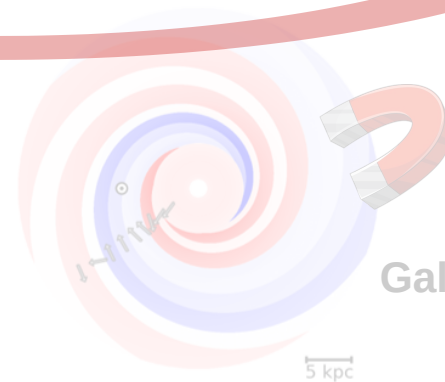


compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



Galactic magnetic fields



5 kpc

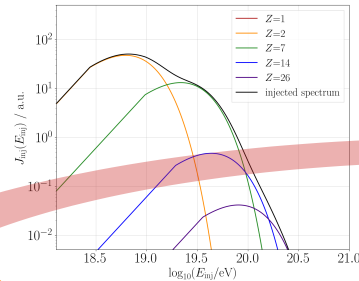
Variations of the injection at the source

source distribution



homogeneous

injection



propagation through

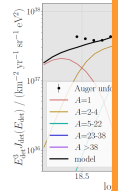
$$\tilde{Q}_A(E) = \underbrace{\tilde{Q}_{0A}}_{\text{element contributions}} \left(\frac{E}{E_0} \right)^{-\underbrace{\gamma}_{\text{spectral index}}} \begin{cases} 1, & E \leq Z_A \underbrace{R_{\text{cut}}}_{\text{rigidity cutoff}} \\ \exp\left(1 - \frac{E}{Z_A R_{\text{cut}}}\right), & E > Z_A R_{\text{cut}} \end{cases}$$

extragalactic magnetic fields

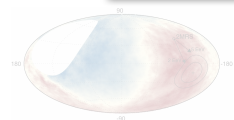


compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



- *Muzio, Anchordoqui, Unger, PRD 109 023006 (2024)*
 → explore **alternatives to Peters cycle** which might fit better
- *Ehlert, Oikonomou, Unger, PRD 107, 103045 (2023)*
 → explore **variations of maximum rigidity** and find that **sources must be very similar**
- *Eichmann, Kachelrieß, Oikonomou JCAP 07 006 (2022)*
 → explore **individual AGNs** with different properties in a combined fit



5 kpc

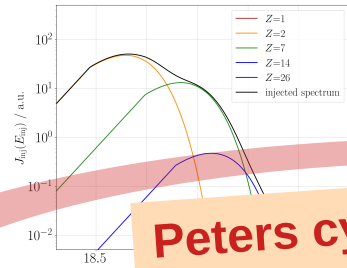
Combined fit including EGMF

source distribution



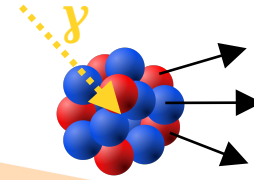
homogeneous

injection



Peters cycle

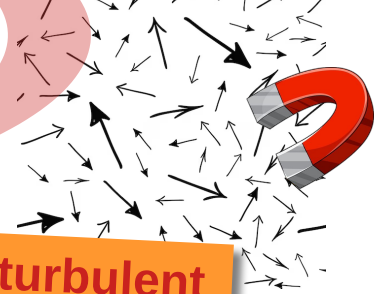
propagation through extragalactic space



1-dimensional



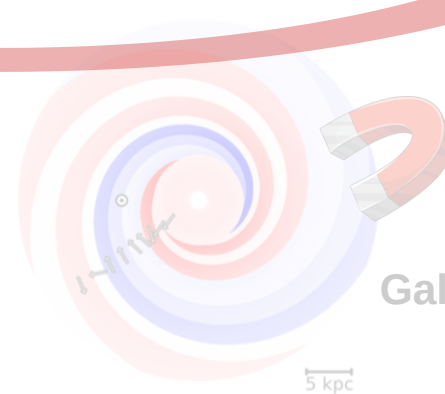
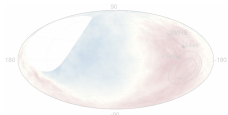
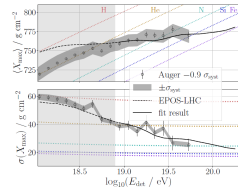
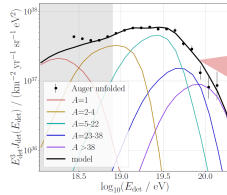
extragalactic magnetic fields



turbulent

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)

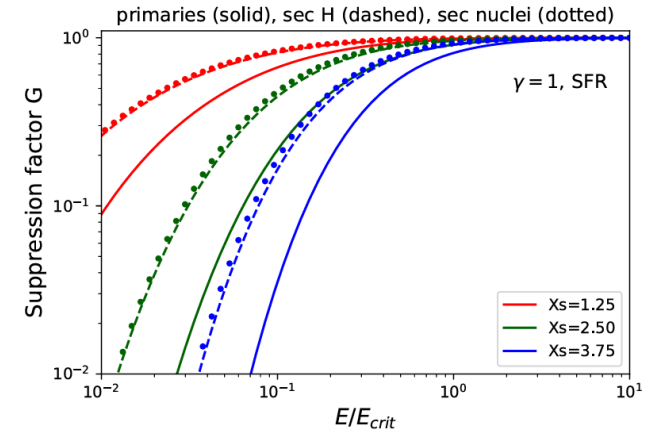
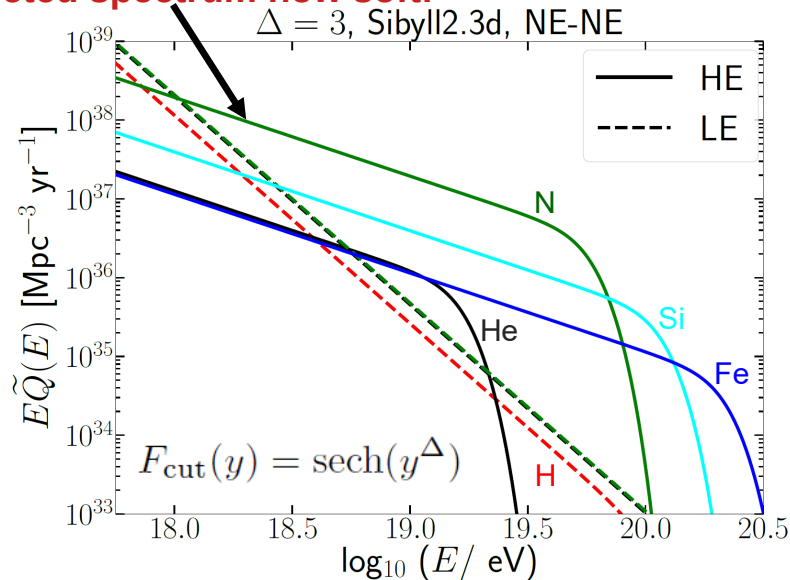


Galactic magnetic fields

Combined fit including EGMF

- extragalactic magnetic field can suppress lower energy particles (diffusion)
- include suppression factor G
 - +2 parameters (critical energy + norm. source density)

high-energy population
injected spectrum now soft!



EGMF can have strong effect on injection, but only for:

- steep injection cutoff
 - & source densities $< 10^{-3} \text{ Mpc}^{-3}$
 - & very strong field strengths $B \sim 10\text{-}200 \text{ nG}$ between nearest sources & Earth
- then: can reach $\gamma=2$

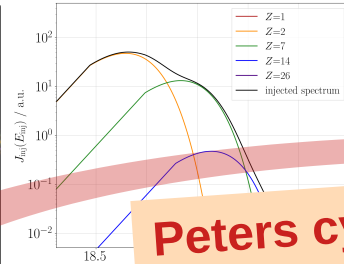
Combined fit including structured EGMF (to spectrum and composition)

source distribution



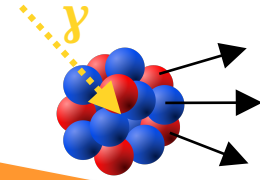
follows tracer

injection



Peters cycle

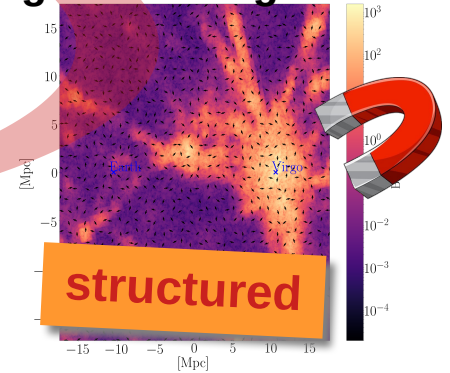
propagation through extragalactic space



SimProp
SIRENTE
CR/Propa

3-dimensional

extragalactic magnetic fields

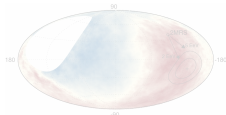
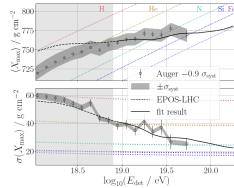
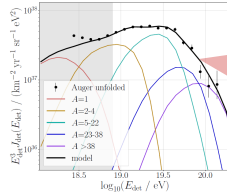


structured

problems: takes very long & not much is measured about EGMF, have to rely on simulations

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



Galactic magnetic fields

5 kpc

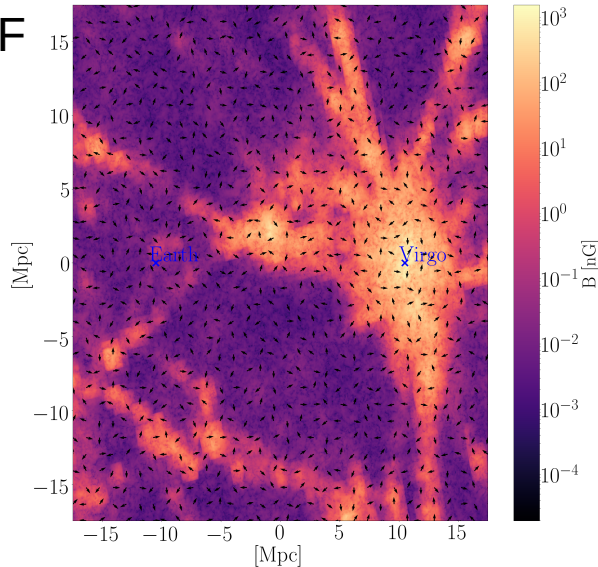
Combined fit including structured EGMF (to spectrum and composition)

D. Wittkowski for the Pierre Auger Collaboration
PoS ICRC 2017 563 (preliminary)

- sources follow 2MRs catalog of all galaxies with density $\sim 10^{-4} \text{ Mpc}^{-3}$

- structured EGMF (Dolag model)

Dolag, Grasso, Springel, Tkachev
JCAP 01 009 (2005)

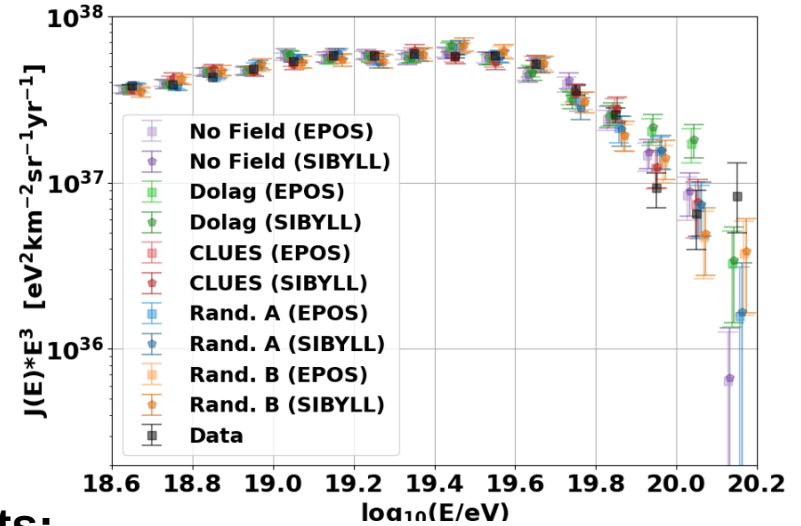


- **results:**

- injection parameters sensitive to EGMF
- softer injection with EGMF

Lundquist, Merten et al, arXiv:2407.06961

- sources roughly homogeneous (FR0 galaxies with density $\sim 10^{-3} \text{ Mpc}^{-3}$)

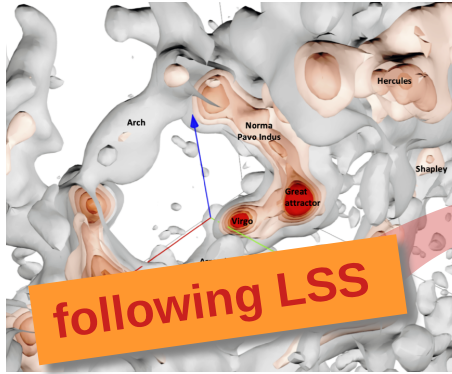


- **results:**

- can describe spectrum & composition with any EGMF model

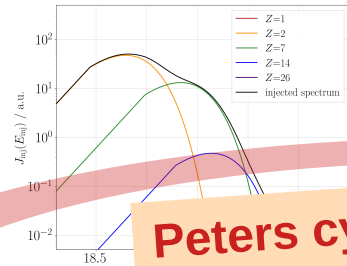
Include arrival directions: large-scale

source distribution



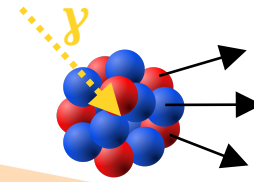
following LSS

injection



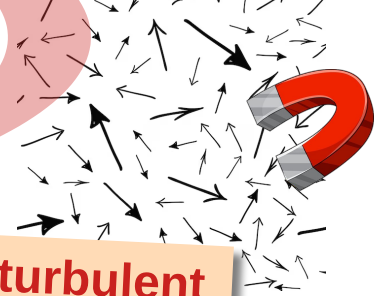
Peters cycle

propagation through extragalactic space



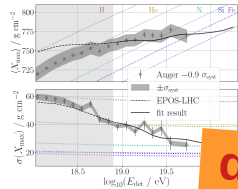
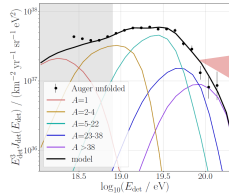
1-dimensional

extragalactic magnetic fields

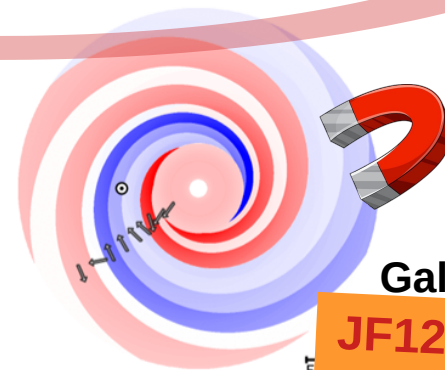
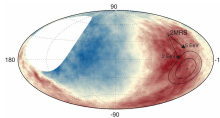


compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)

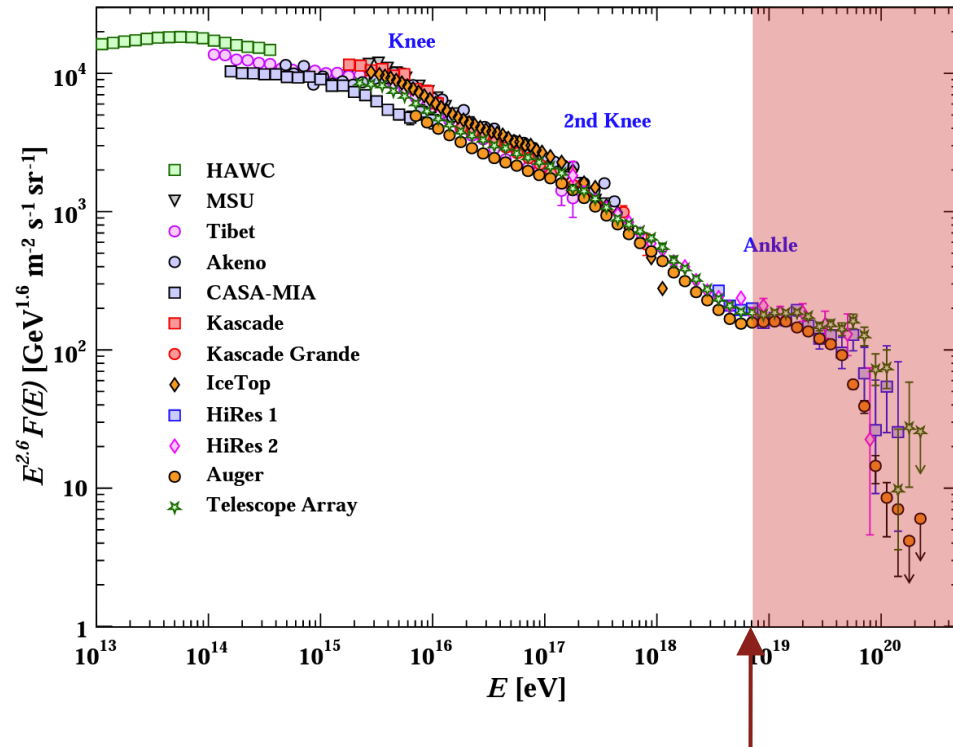


dipole
 $E > 8 \text{ EeV}$

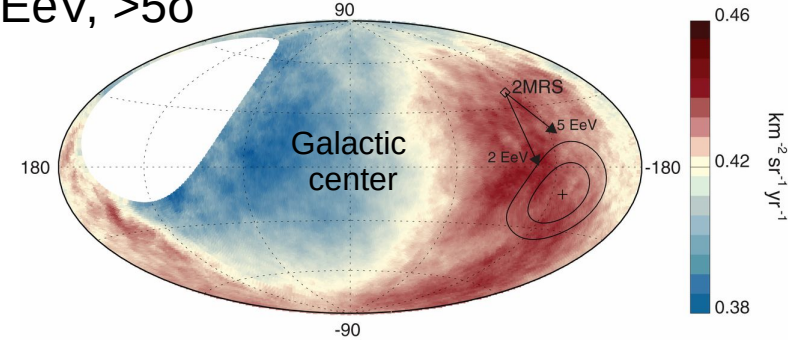


JF12

Arrival directions $E > 8 \text{ EeV}$

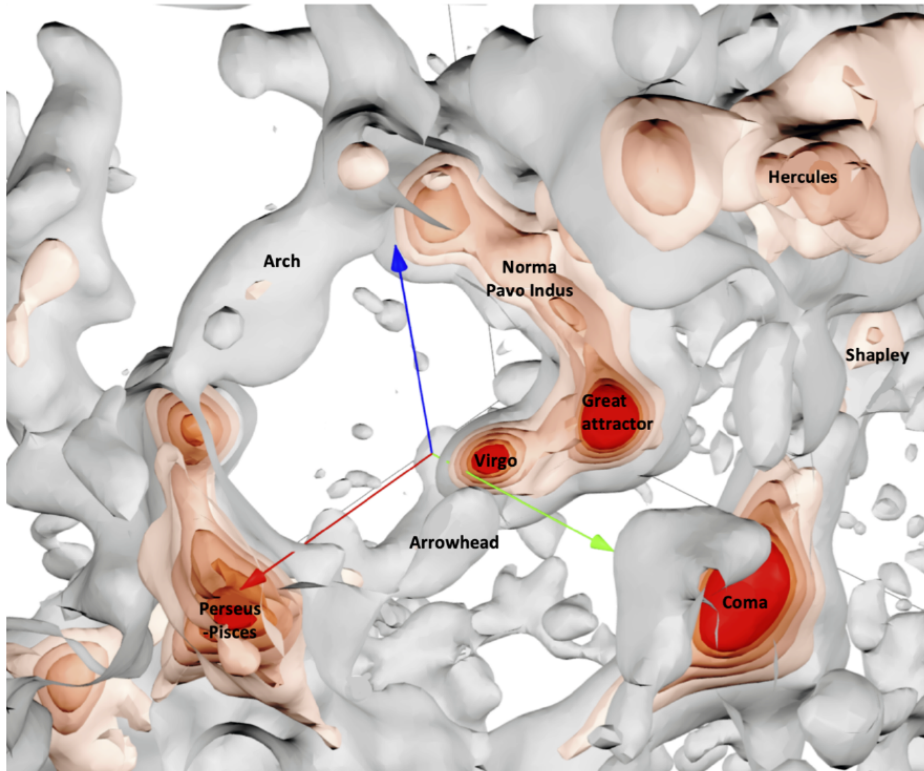


dipole $> 8 \text{ EeV}, >5\sigma$



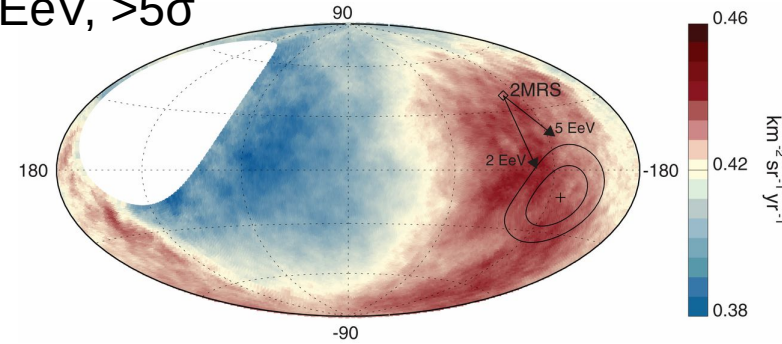
- amplitude $\sim 7\%$, rising with the energy
- no significant quadrupole or higher moments
- phase shifts from Galactic center to anticenter
- \rightarrow **sources extragalactic!**

UHECR flux from Large Scale Structure



extragalactic matter density

dipole > 8 EeV, $>5\sigma$



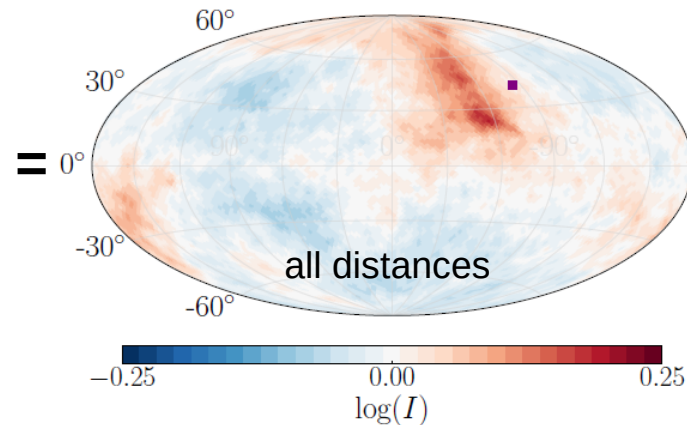
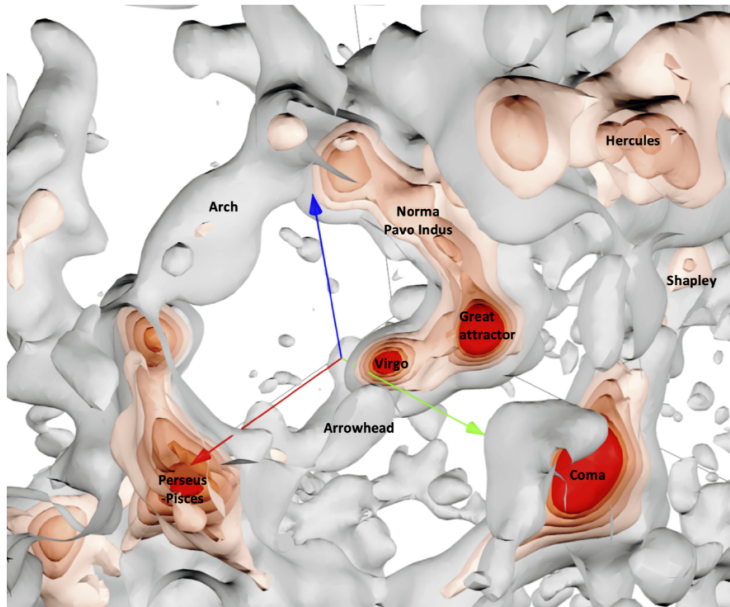
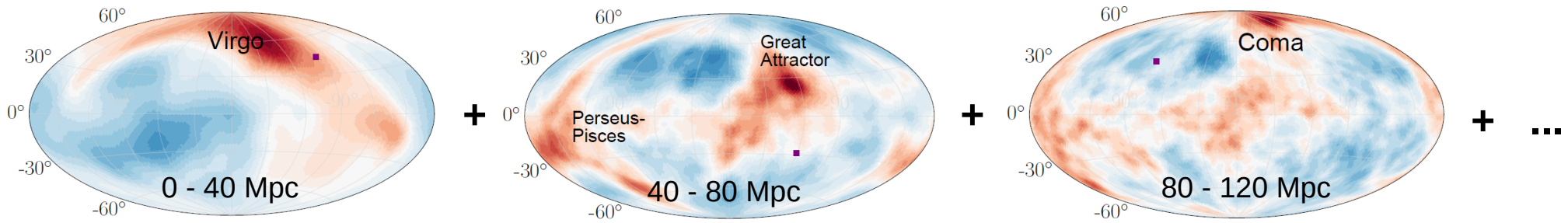
dipole can be explained by
extragalactic sources following the
large-scale structure of the universe

+ deflection by Galactic magnetic field

e.g. Ding, Globus, Farrar ApJL 913 L13 (2021)
Globus, Piran, Hoffman, Carlesi, Pomaredo MNRAS 484 (2019)
Allard, Aublin, Baret, Parizot A&A 664 A120 (2022)

...

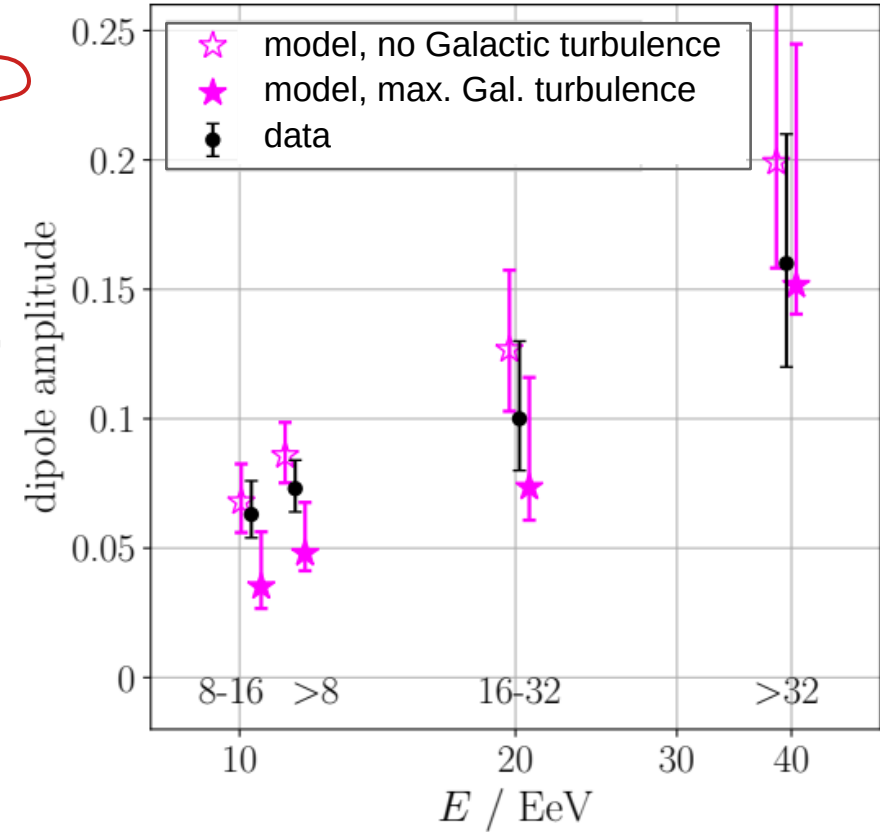
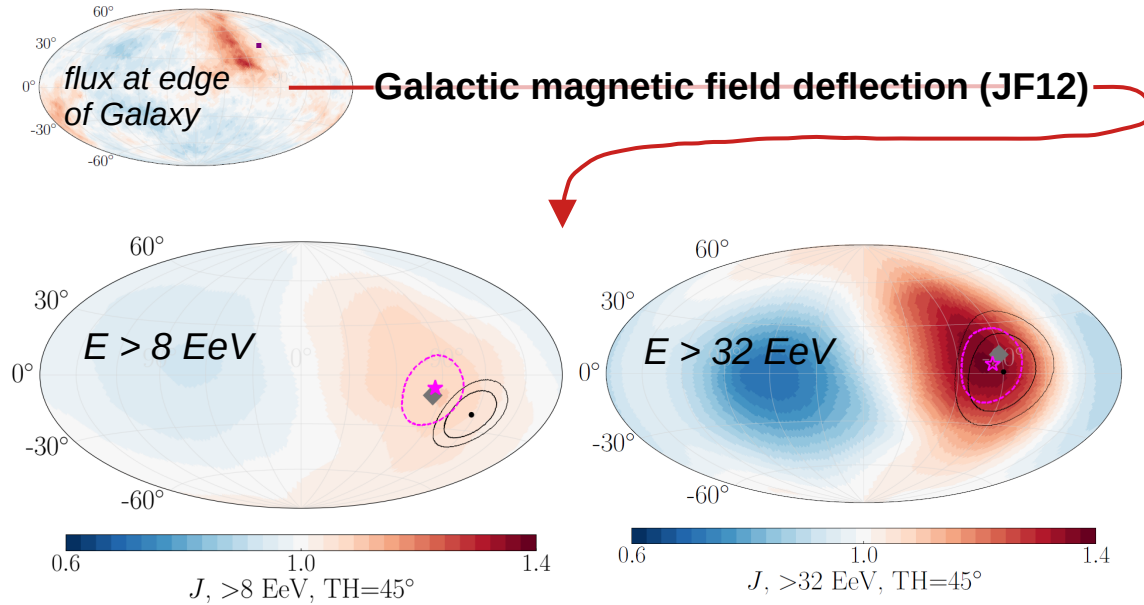
UHECR flux from Large Scale Structure



expected flux at the
edge of our Galaxy

„illumination“

Measurements at Earth (after Galactic magnetic field)



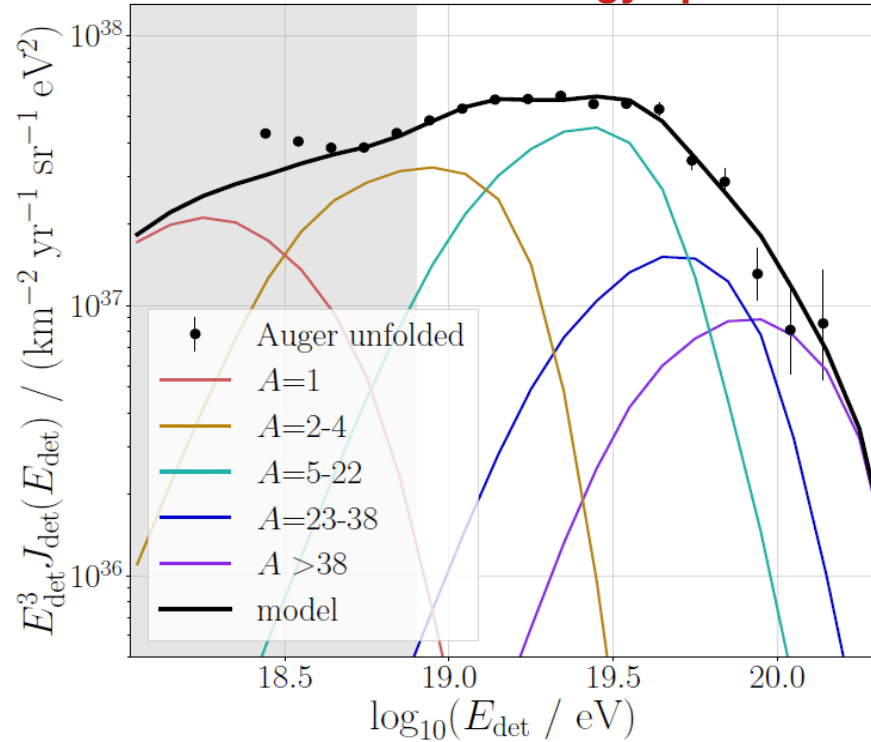
- dipole direction not perfect at lower energy
→ update of GMF model?

later

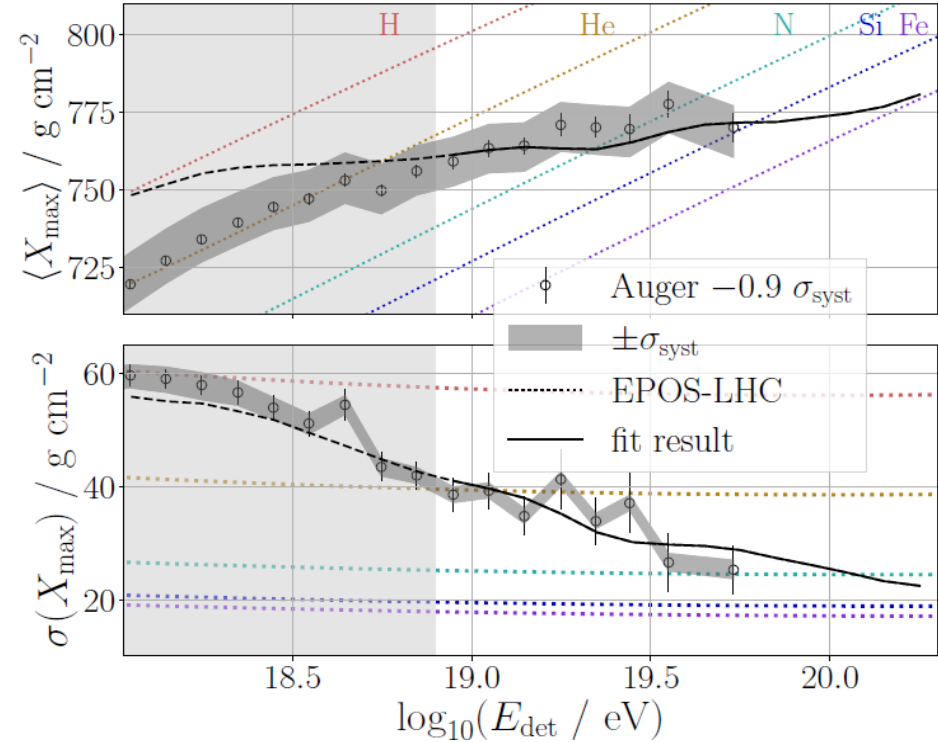
- dipole amplitude + energy evolution ✓

Measurements at Earth (after Galactic magnetic field)

energy spectrum ✓

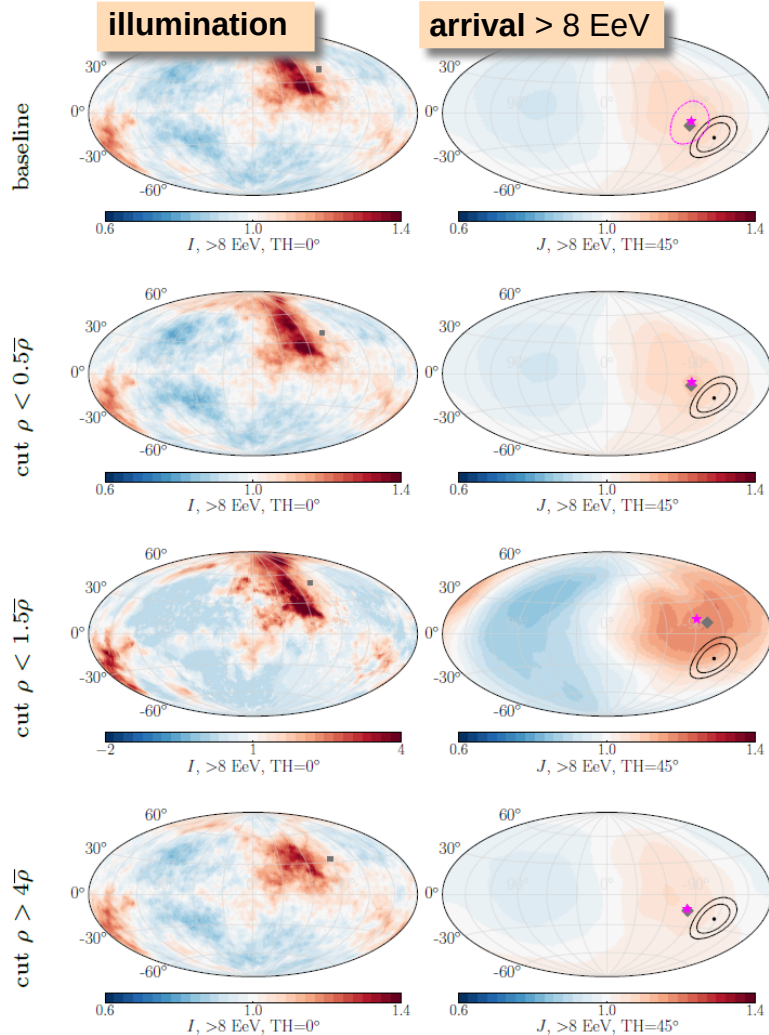


mass composition ✓



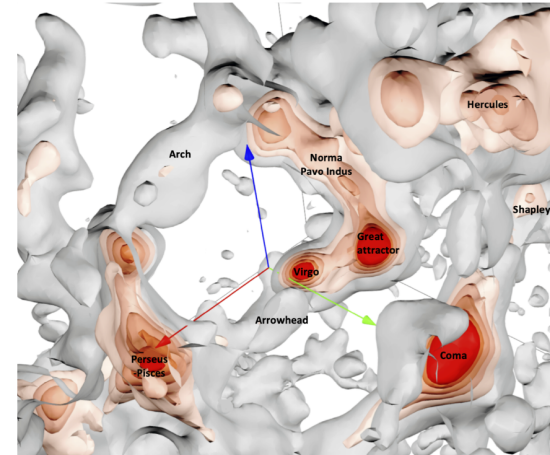
LSS model can describe spectrum, composition and arrival directions. What else can we learn...?

Bias between matter density and UHECR sources

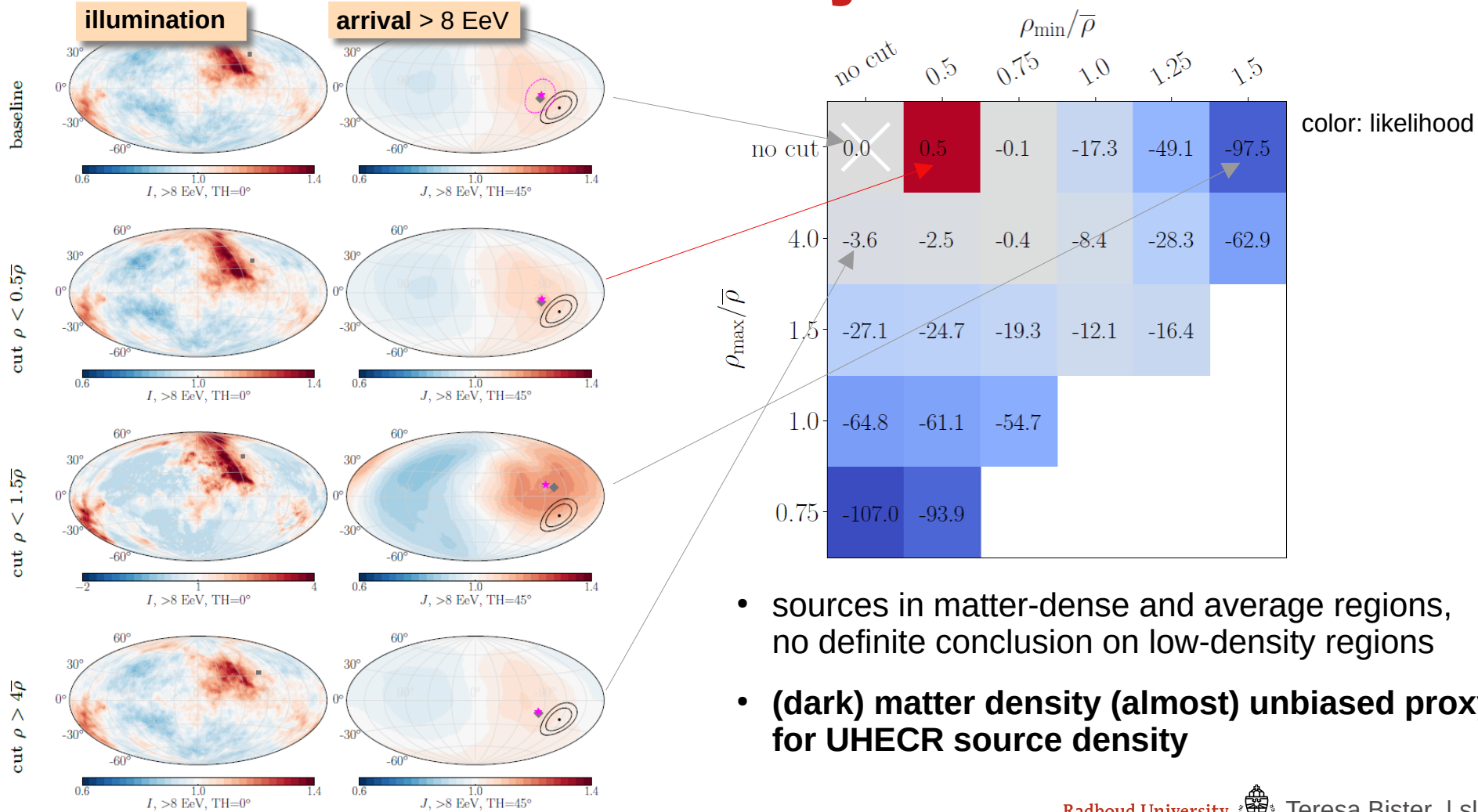


Is there a **bias** between the UHECR source distribution and the (dark) matter distribution / LSS?

→ simple test:
cut away densest / least dense regions of LSS



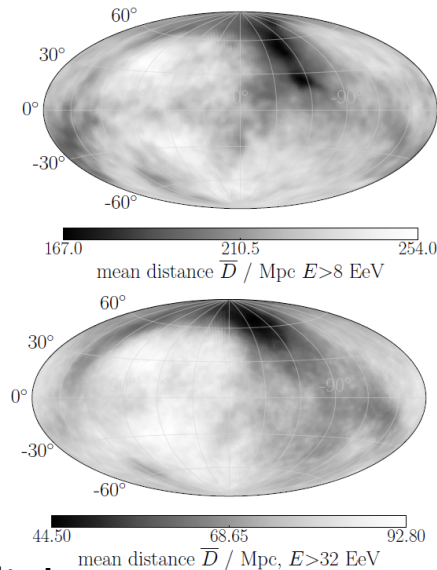
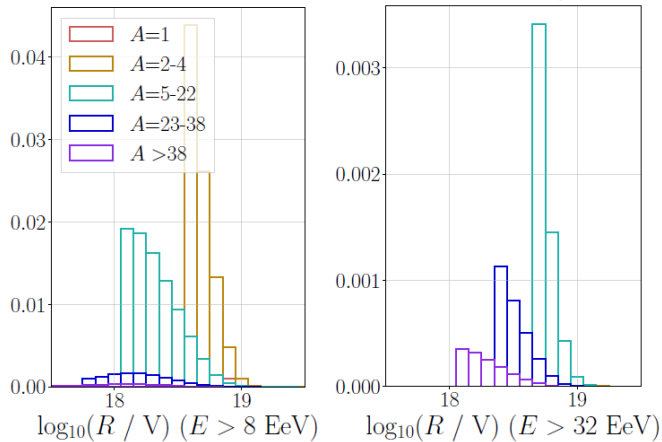
Bias between matter density and UHECR sources



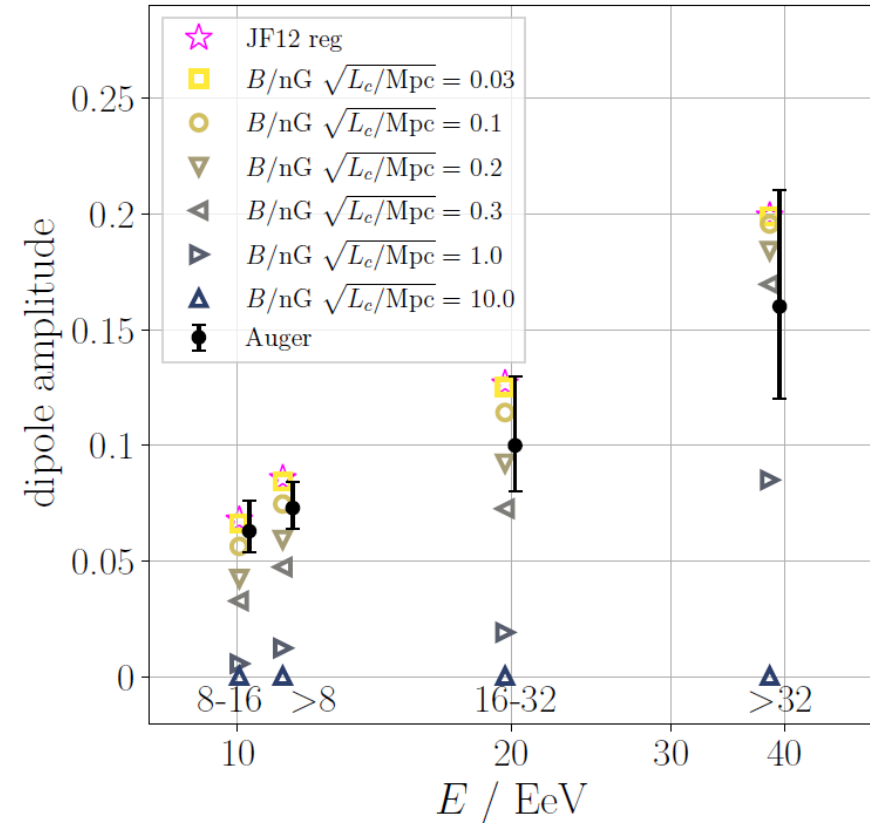
Extragalactic magnetic field effect?

- extragalactic magnetic field „smears out“ arrival directions
- cannot be too strong to not decrease dipole amplitude

$$\delta\theta = 2.9^\circ \frac{B}{\text{nG}} \frac{10 \text{ EeV}}{E/Z} \frac{\sqrt{D L_c}}{\text{Mpc}}$$

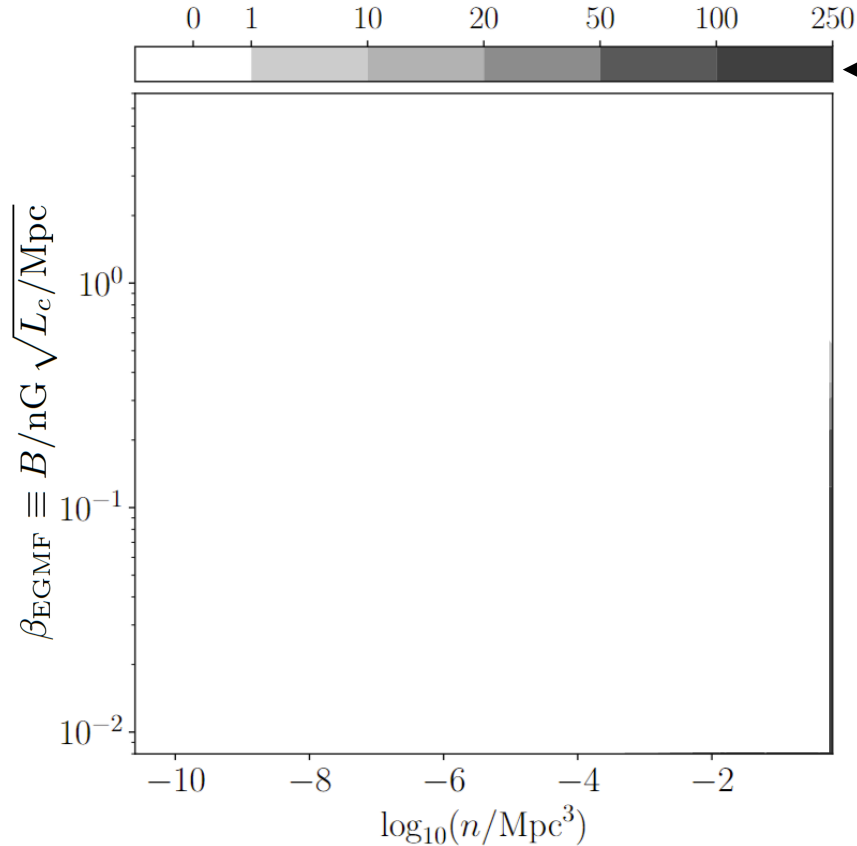


but - opposing effect:
sparser source number density!



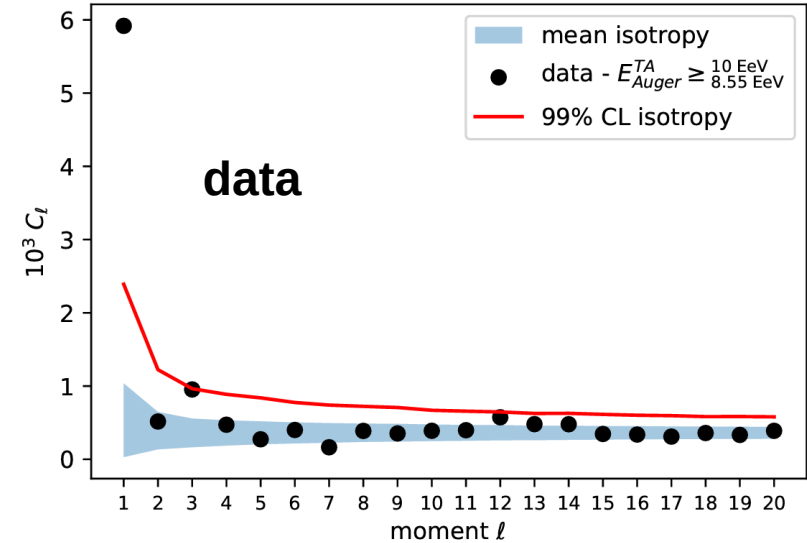
Source density and extragalactic magnetic field

extragalactic
magnetic
field



source number density

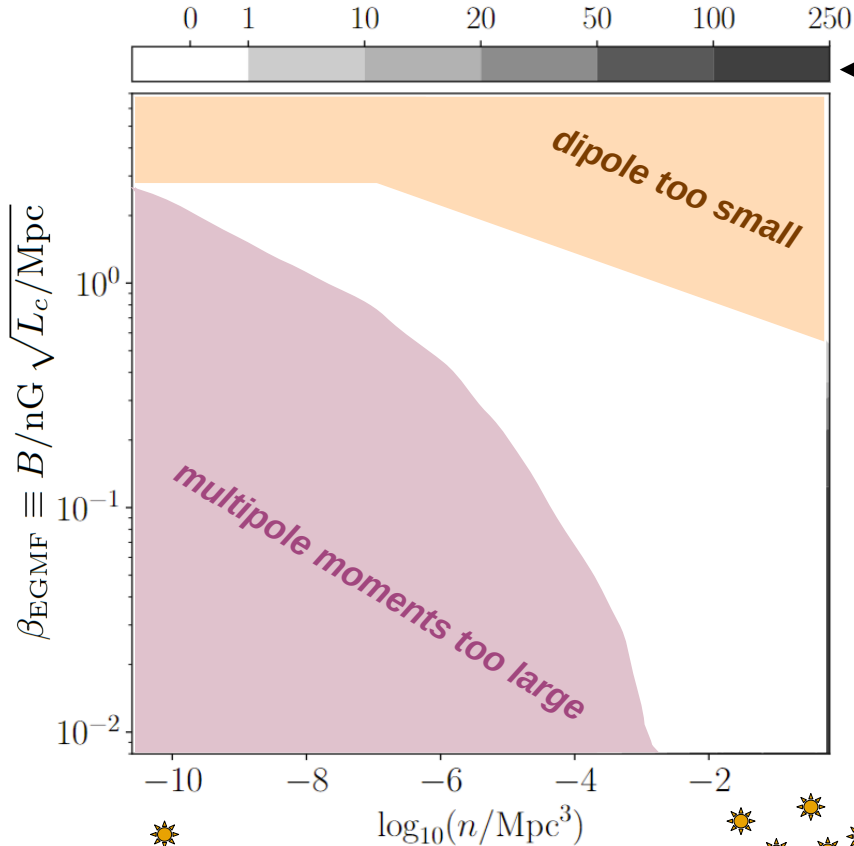
„How many of 1000 random simulations have a large enough dipole and small enough higher multipole moments?“



Source density and extragalactic magnetic field



extragalactic
magnetic
field



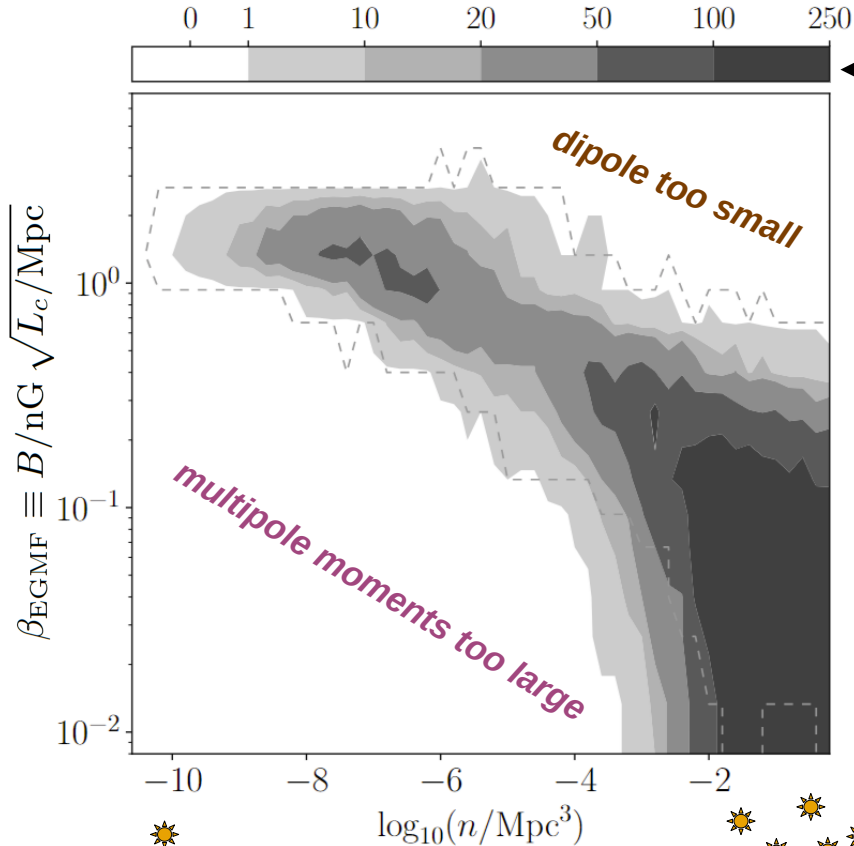
„How many of 1000 random simulations have a large enough dipole and small enough higher multipole moments?“

source number density
„cosmic variance“

Source density and extragalactic magnetic field



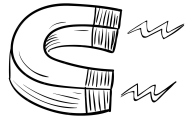
extragalactic
magnetic
field



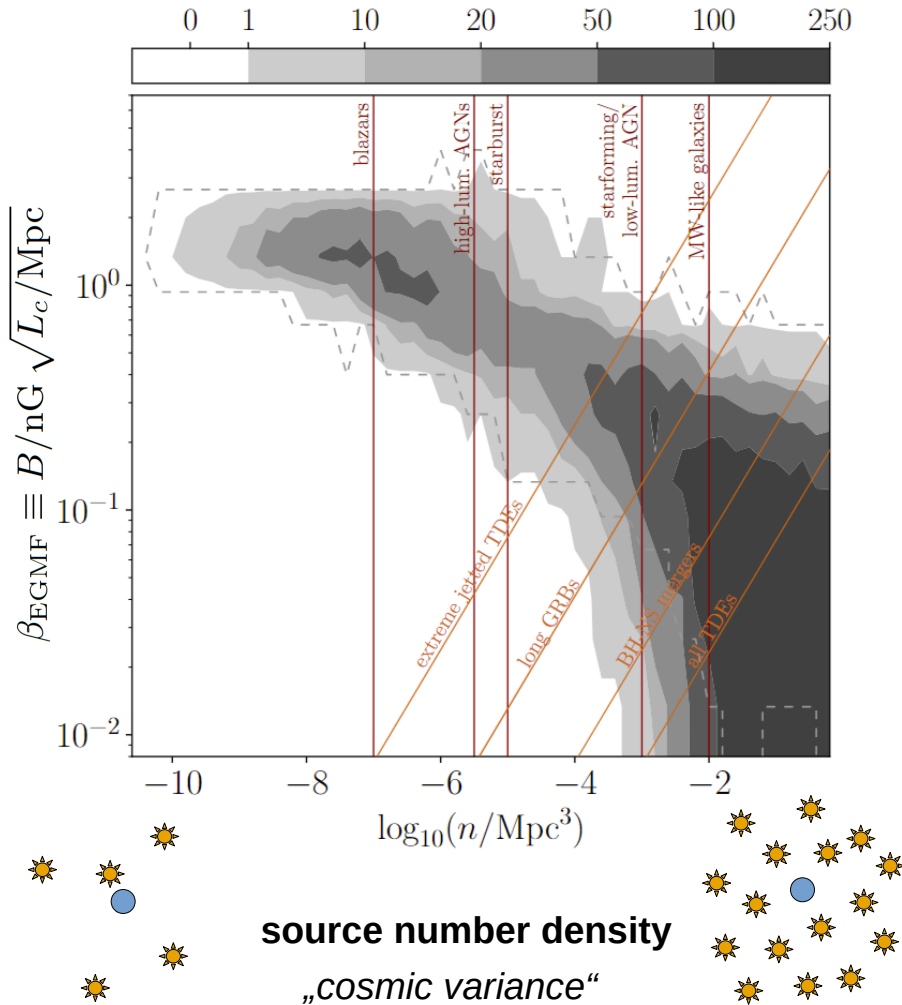
„How many of 1000 random simulations have a large enough dipole and small enough higher multipole moments?“

source number density
„cosmic variance“

Source density and extragalactic magnetic field



extragalactic
magnetic
field



- **rare sources**
(e.g. starbursts) ↔ **strong EGMF**
- max. 3 nG Mpc^{1/2}



- **negligible EGMF**
↔ sources must be **common**, (e.g. Milky-Way-like galaxies)

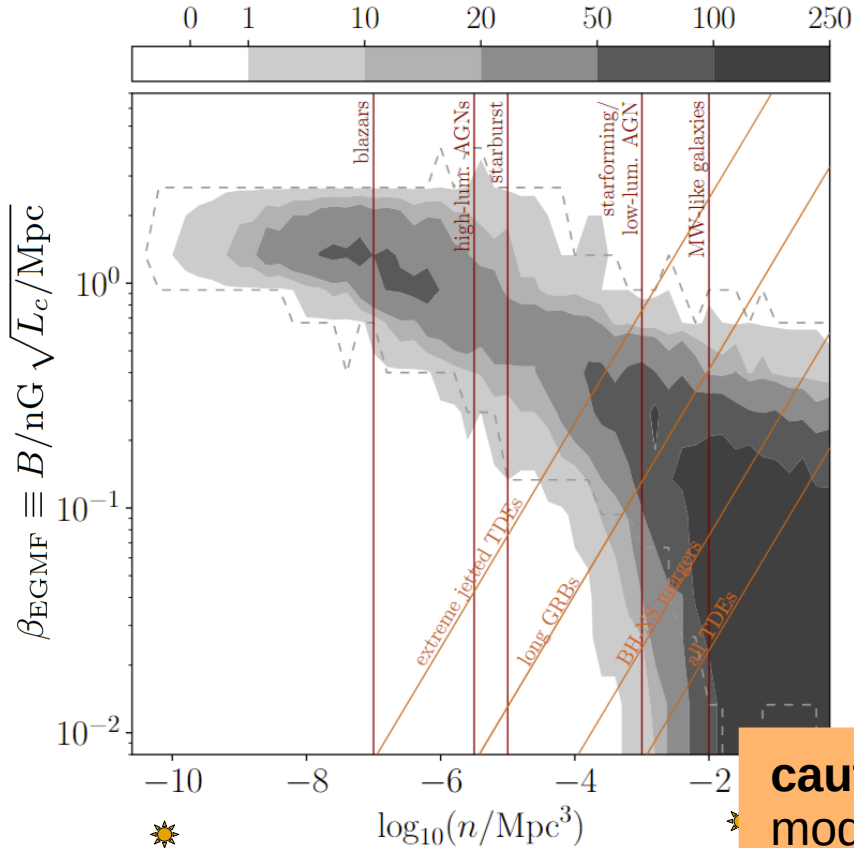


- or: **frequent** in case of **transients**
like BH-NS mergers,
tidal disruption
events



Source density and extragalactic magnetic field

extragalactic
magnetic
field



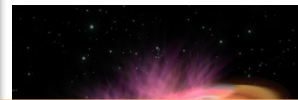
source number density
„cosmic variance“

→ rare sources
(e.g. starbursts) ↔
strong EGMF
→ max. 3 nG Mpc^{1/2}

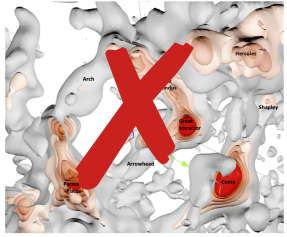
→ negligible EGMF
↔ sources must be
common, (e.g. Milky-
Way-like galaxies)

→ or: **frequent** in case
of transients

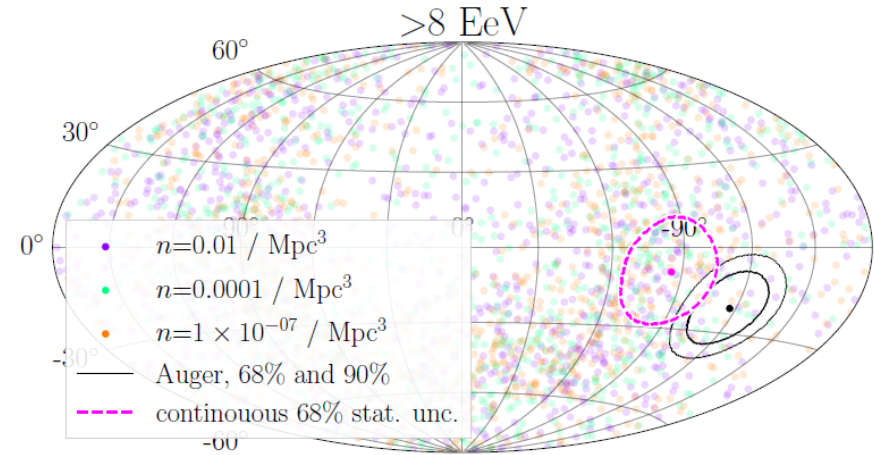
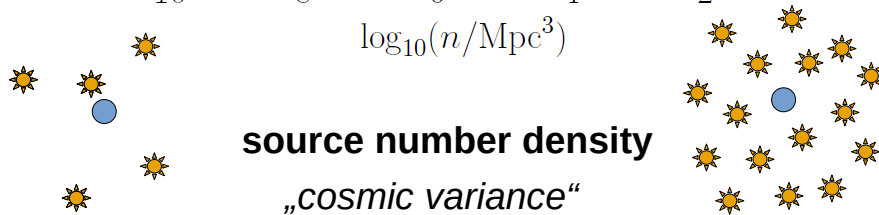
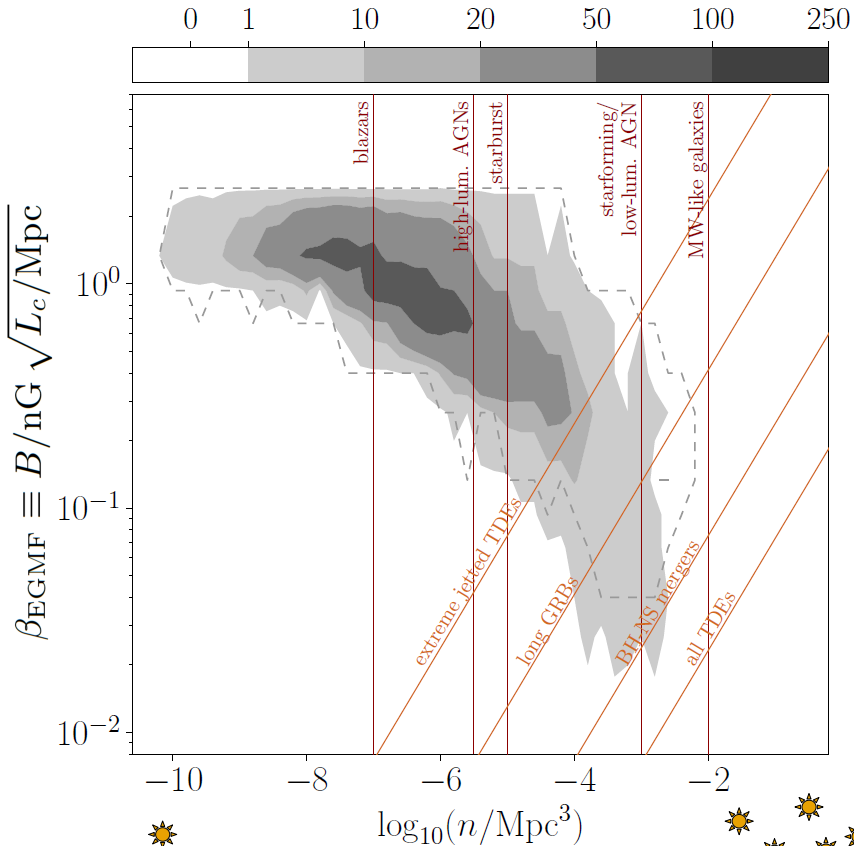
caution: dependencies on coherent GMF
model, random GMF part, EGMF simplification,
uncertainties on source distribution...



Homogeneous source distribution?



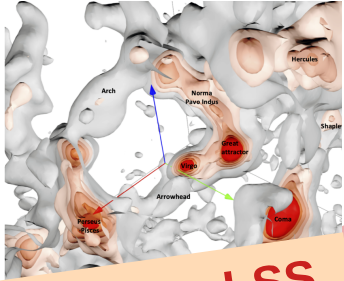
extragalactic
magnetic
field



- homogeneous distribution less likely, only for rare sources and considerable EGMF
- dipole direction not predictable

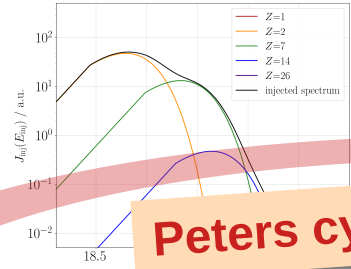
New models for the Galactic magnetic field

source distribution



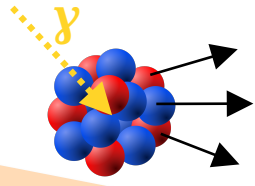
following LSS

injection



Peters cycle

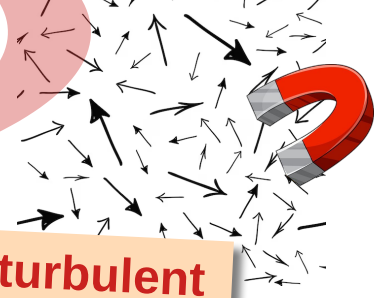
propagation through extragalactic space



1-dimensional



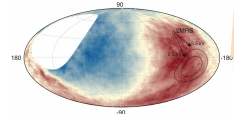
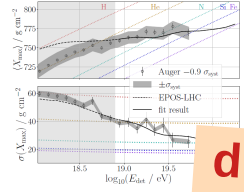
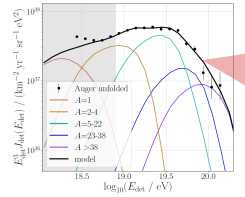
extragalactic magnetic fields



turbulent

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)



dipole
E > 8 EeV

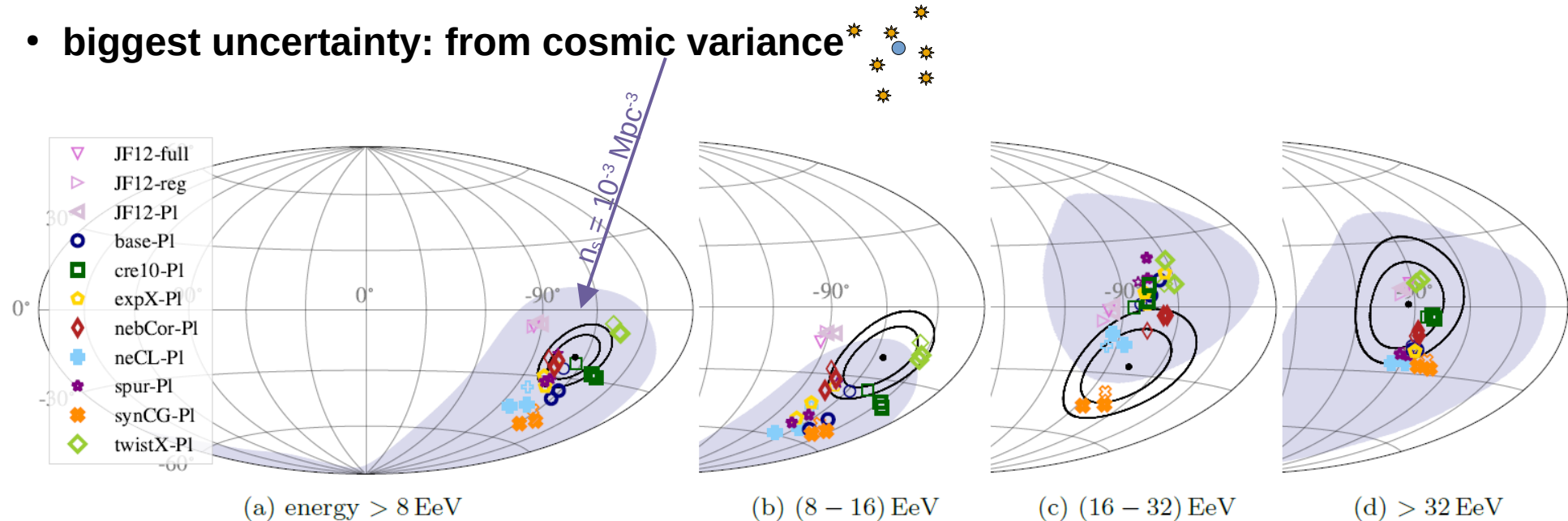


Galactic magnetic fields
new UF23 models

Dipole directions

predict **dipole direction** for 8 new GMF models (+Planck random field):

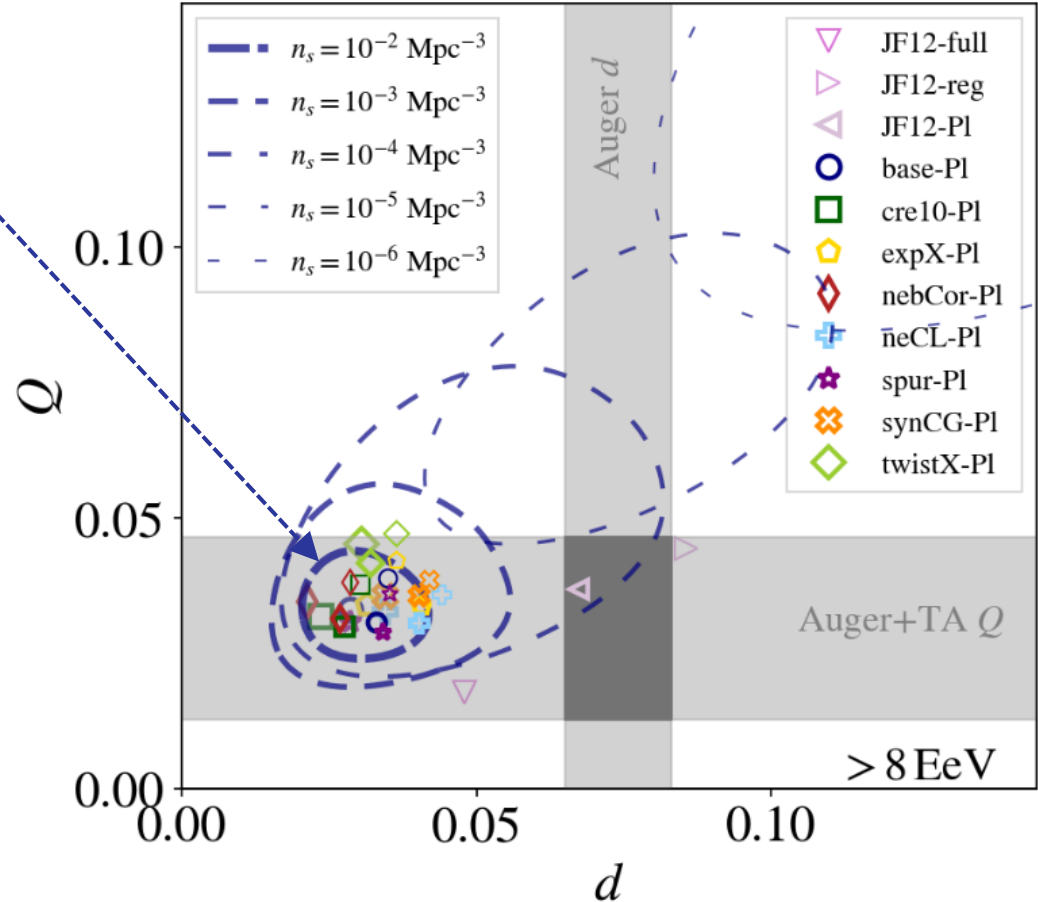
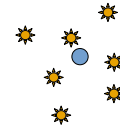
- models quite similar → cannot reject any model
→ good news: GMF uncertainty does not obstruct conclusions on sources 😊
- random field part has minor influence on dipole direction
- **biggest uncertainty: from cosmic variance**



Dipole & Quadrupole amplitudes

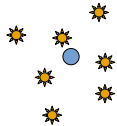
dipole & quadrupole amplitudes:

- cosmic variance again dominates over differences between models
- quadrupole amplitude of all UF23 model comparable to JF12 + Planck



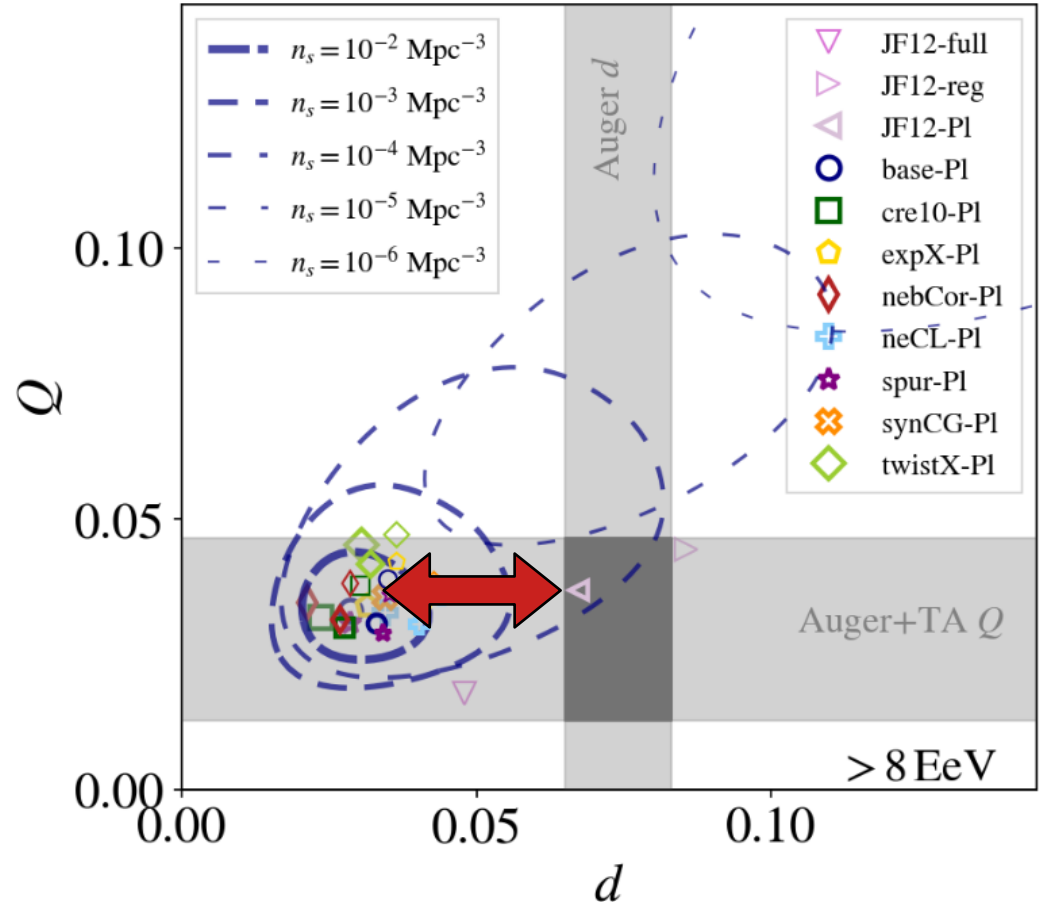
Dipole & Quadrupole amplitudes

dipole & quadrupole amplitudes:

- cosmic variance again dominates over differences between models 
- quadrupole amplitude of all UF23 model comparable to JF12 + Planck

but: dipole amplitude significantly smaller!

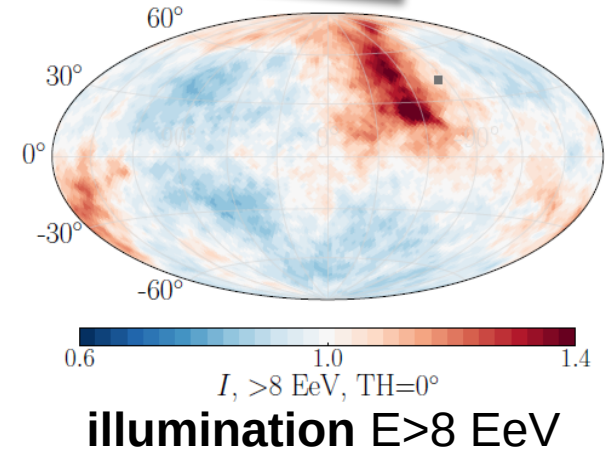
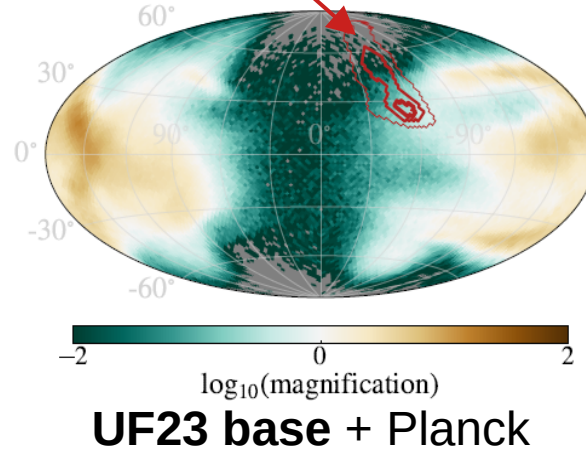
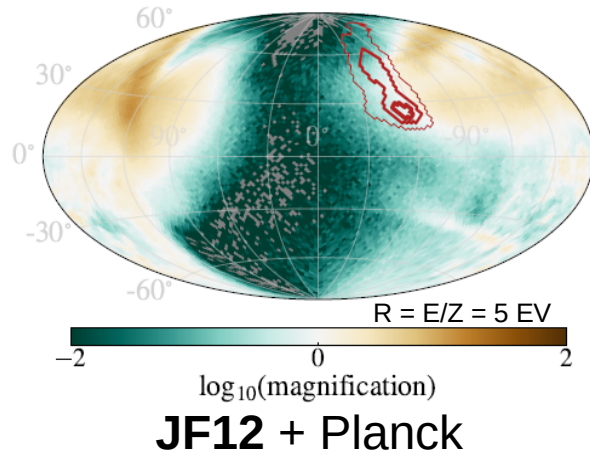
- now need approximately $10^{-3} \text{ Mpc}^{-3} < n < 10^{-5} \text{ Mpc}^{-3}$ for compatibility
- continuous model incompatible!



Why is the dipole amplitude so small with UF23?

- highest flux illumination is **demagnified** by **all UF23 models**, different to JF12

magnification =
flux with GMF divided by flux
without GMF, from every direction

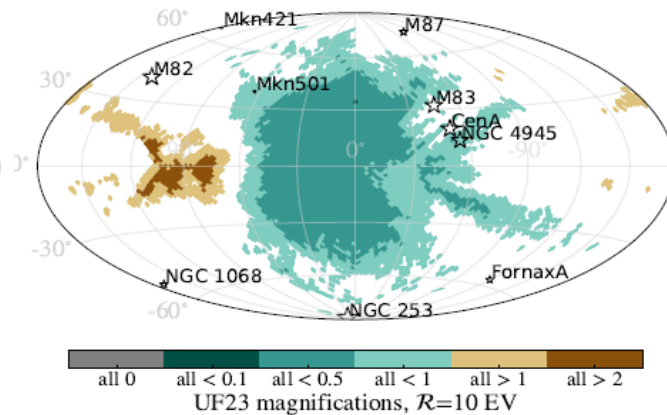
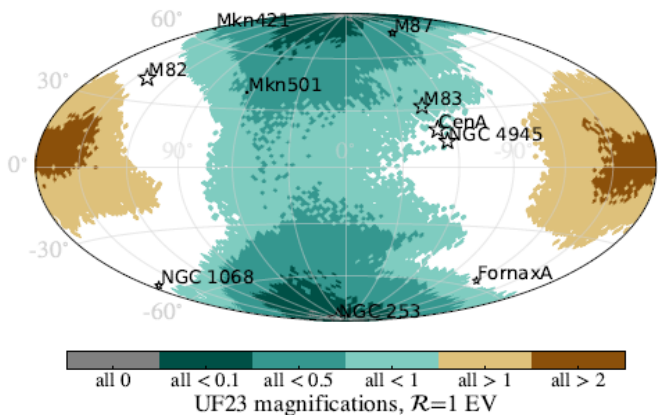
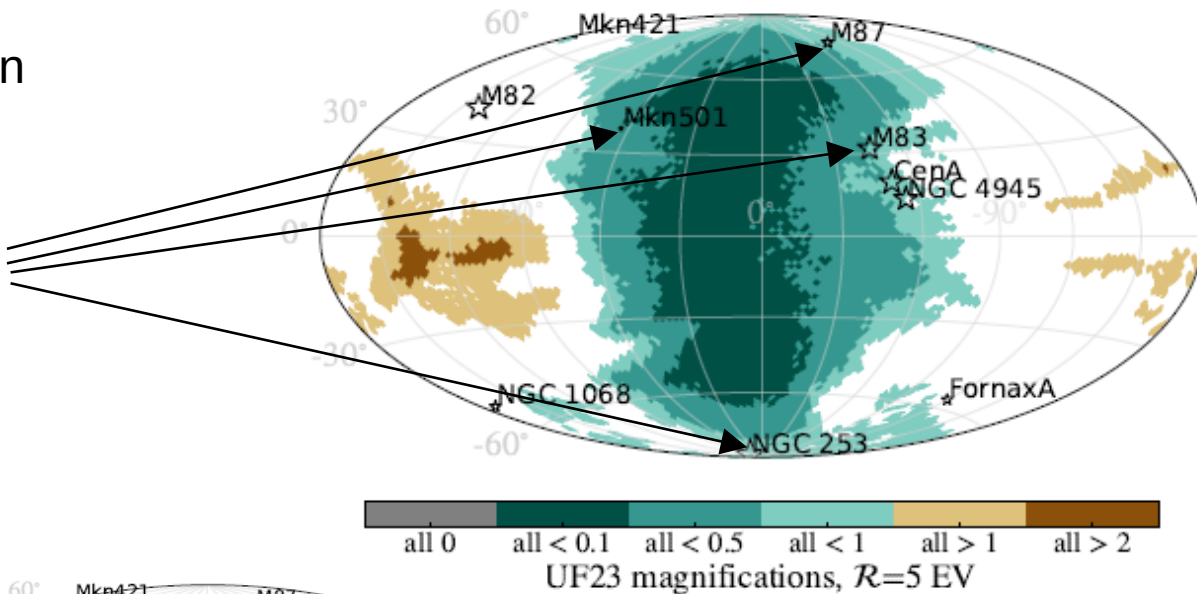


- magnification has huge influence on dipole amplitude!**
 - due to uncertainties on LSS model + random magnetic field model + EGMF:
 - source density etc. with large uncertainties
 - future: sensitivity to probe LSS model, GMF...

Magnification maps for different rigidities

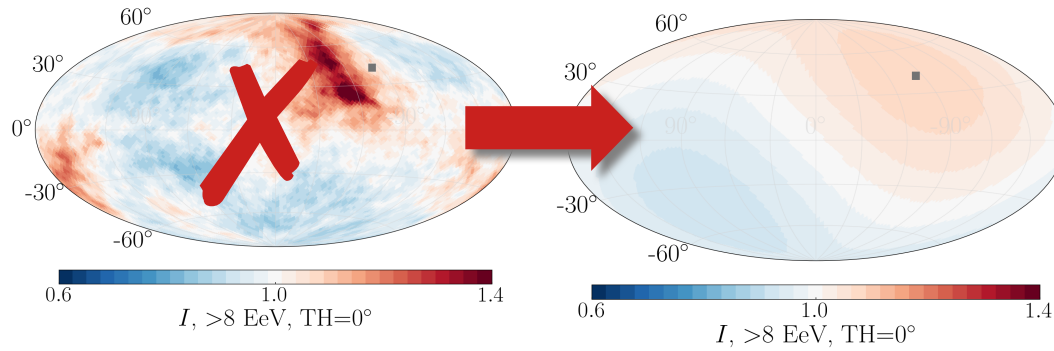
consequence of demagnification in UF23 models:

- many source candidates in central demagnification area
- might not see many CRs from them, at least not with rigidity $R = E/Z < 5$ EV



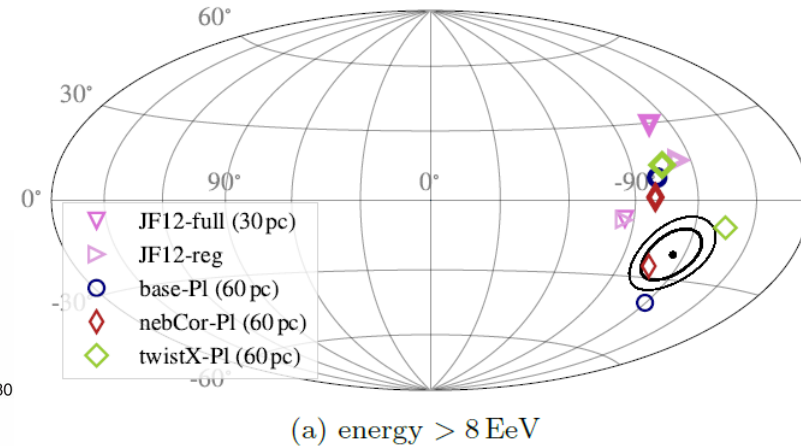
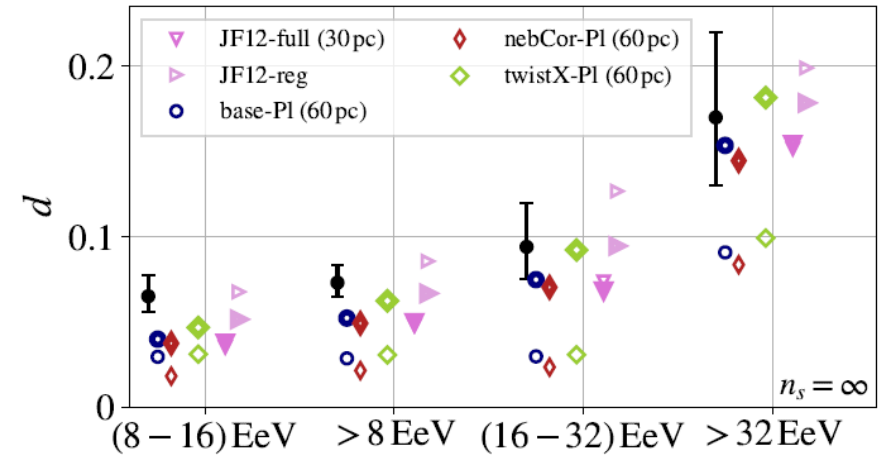
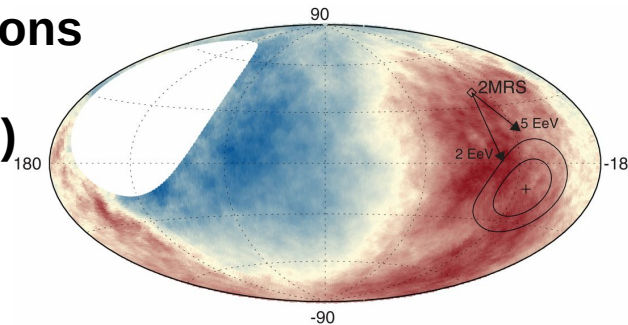
Dipolar illumination

replace the illumination by dipole component:



→ consequence of sensitive interplay between illumination & magnification

→ quite different predictions of amplitude (factor 2) & direction (by 20° - 60°)



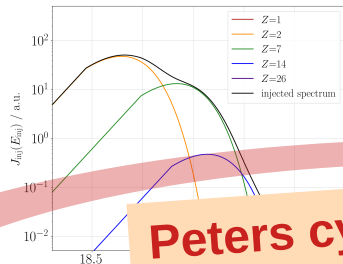
Higher energies - smaller-scale anisotropies

source distribution



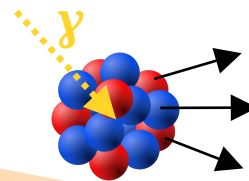
homogeneous + catalog

injection



Peters cycle

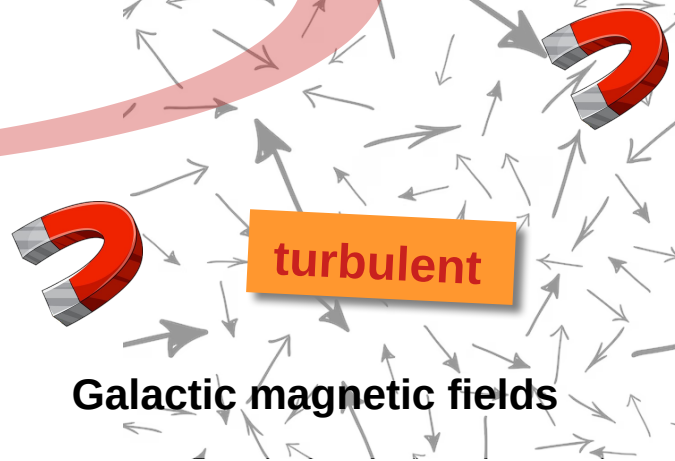
propagation through extragalactic space



SimProp SIRENTE
 CR/Propa

1-dimensional

extragalactic magnetic fields

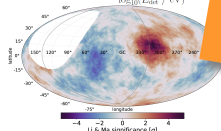
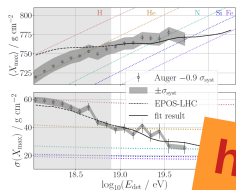
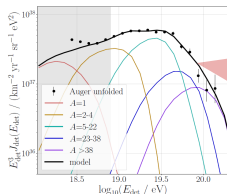


turbulent

Galactic magnetic fields

compare to data

- energy spectrum
- mass composition
- arrival directions
- (multimessenger)

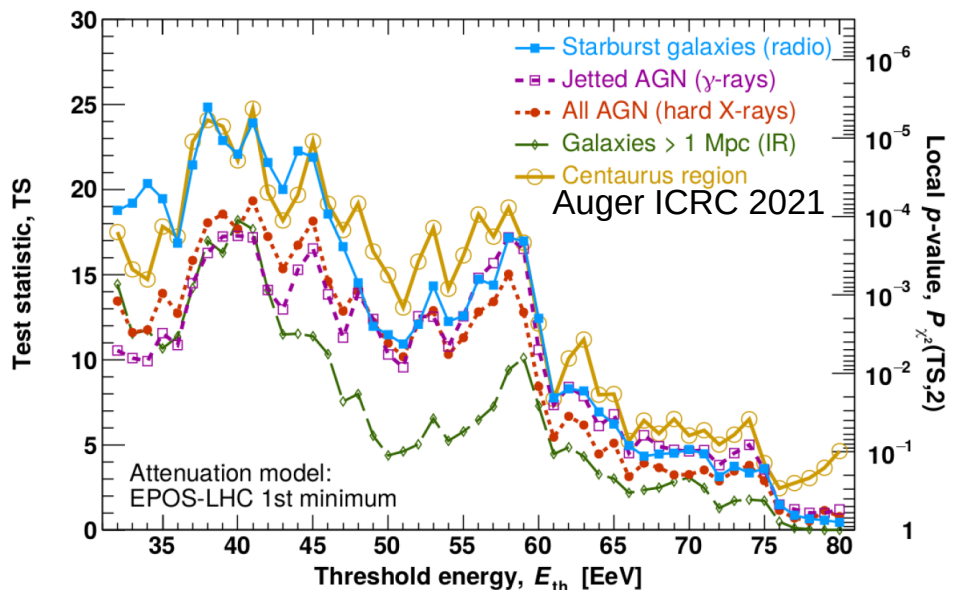
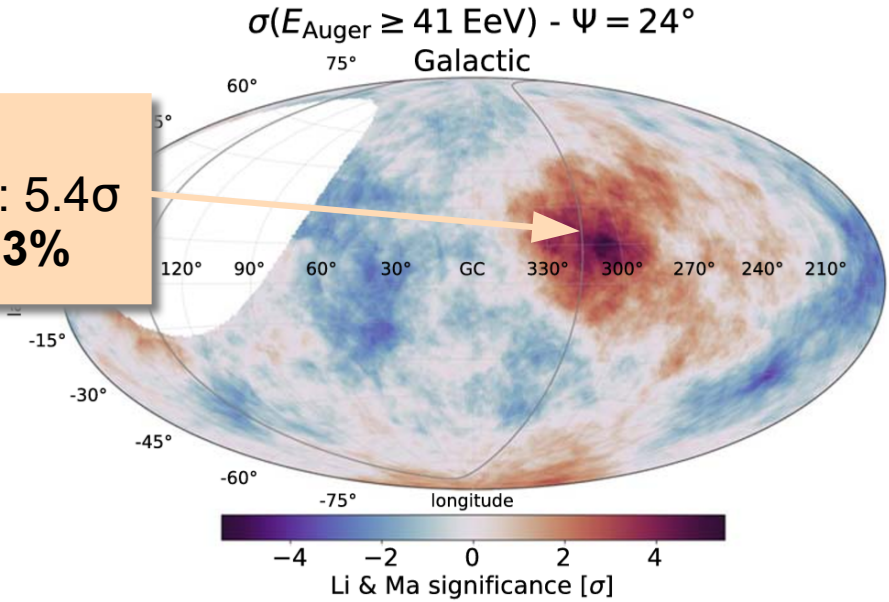


higher energies
 E > 20 EeV

Small-scale anisotropies

- **blind search** over 1° pixels
- 2 scan parameters:
 - energy threshold
 $32 \text{ EeV} \leq E_{\text{th}} \leq 80 \text{ EeV}$
 - circular tophat window
 $1^\circ \leq \psi \leq 30^\circ$

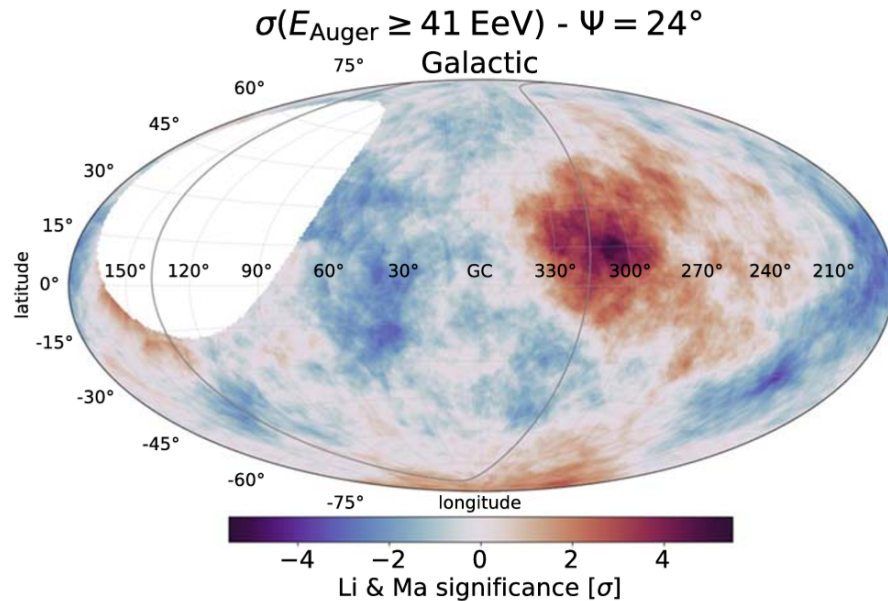
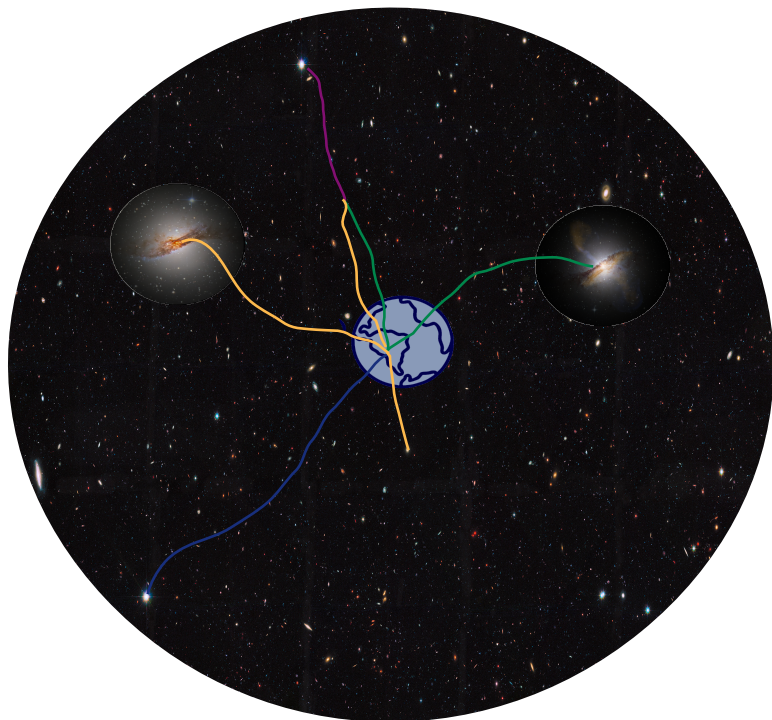
local Li-Ma
significance: 5.4σ
post-trial **p=3%**



- large trial factor due to whole-sky scan
→ comparison to source candidates
- **currently 4.2σ correlation with catalog of starburst galaxies, 3.3σ with γ -AGNs, 4.0σ with Centaurus A**

Model for higher energies

- based on correlations of arrival directions with nearby candidates (SBGs, Centaurus A, γ -AGNs)
- model: homogeneous background sources + nearby candidates

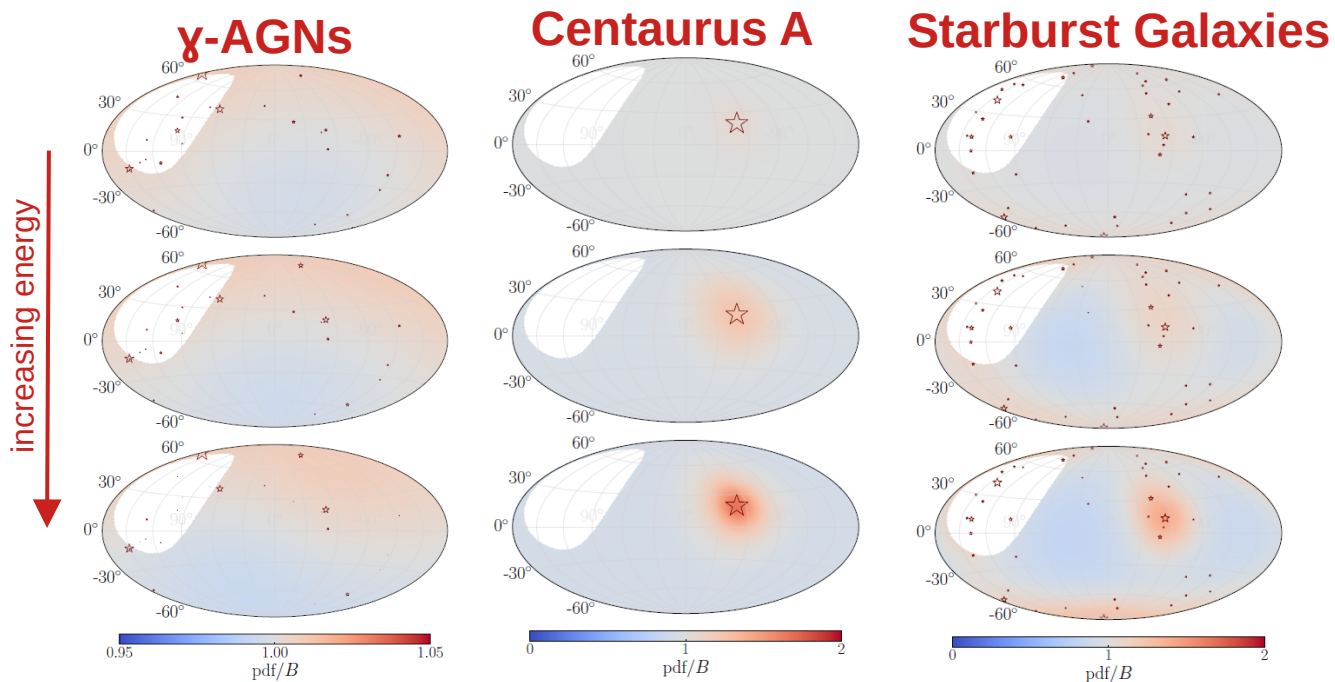
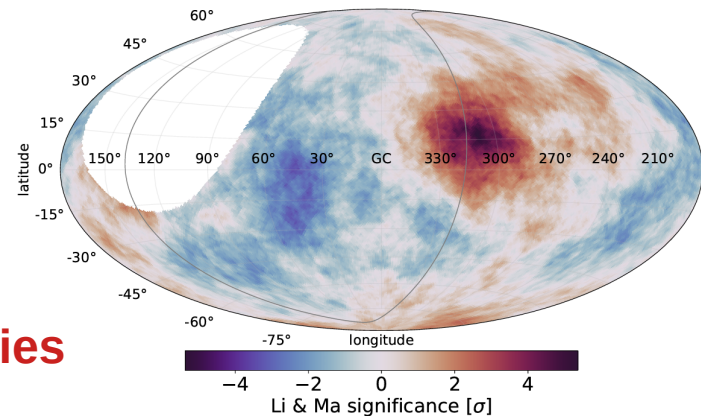


- fit to energy spectrum, shower depth distributions, arrival directions in energy bins

- instead of magnetic field models:
rigidity-dependent blurring $\delta = \frac{\delta_0}{R/10 \text{ EV}}$
 $R=E/Z$

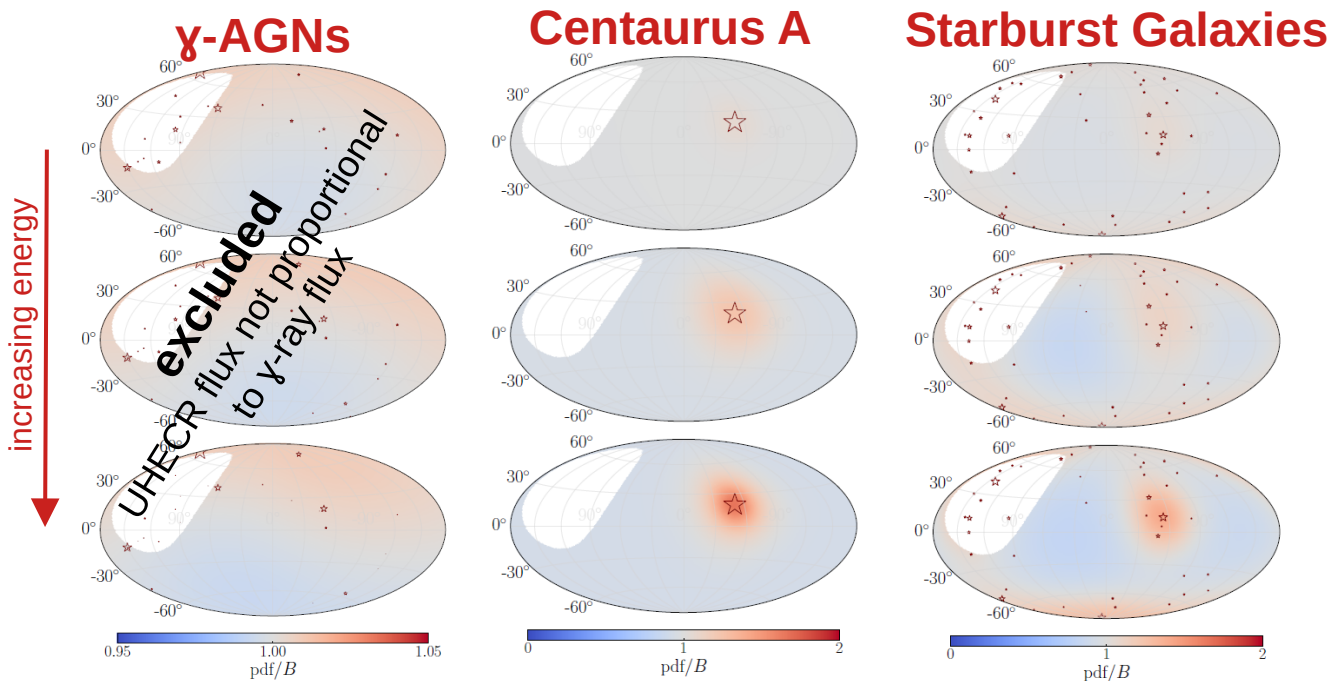
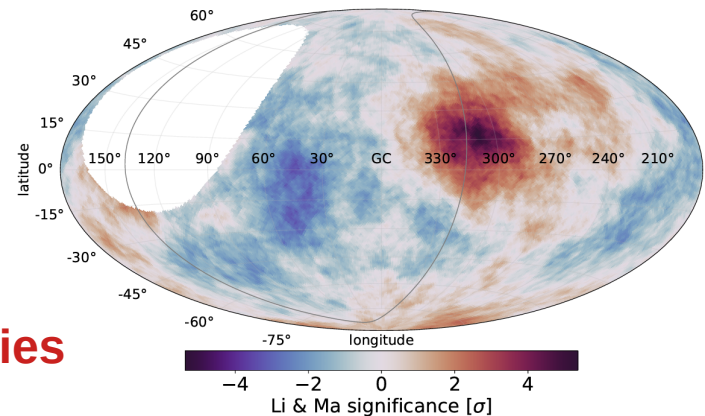
Modeled arrival directions

- based on correlations of arrival directions with nearby candidates (SBGs, Centaurus A, γ -AGNs)
- model: homogeneous background sources + nearby candidates



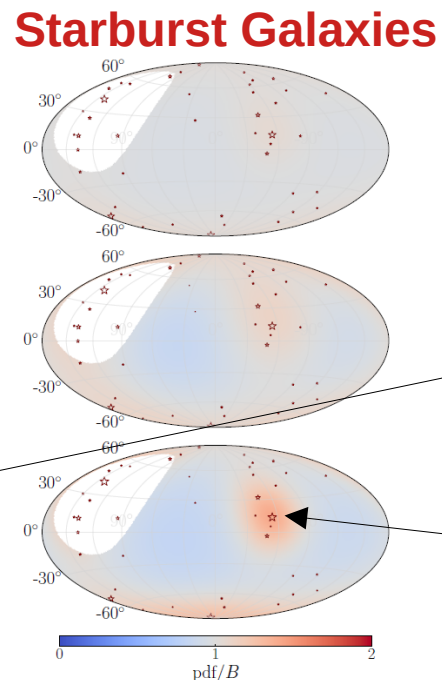
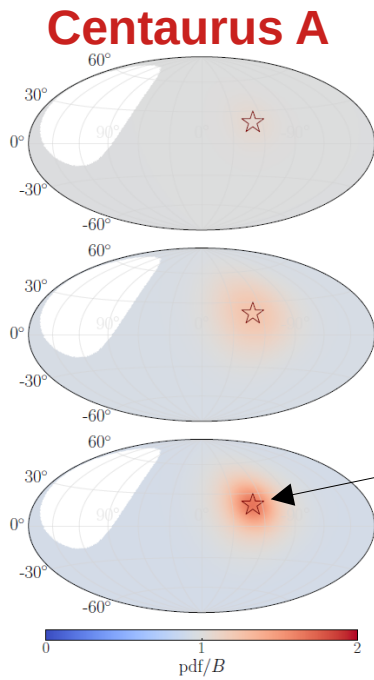
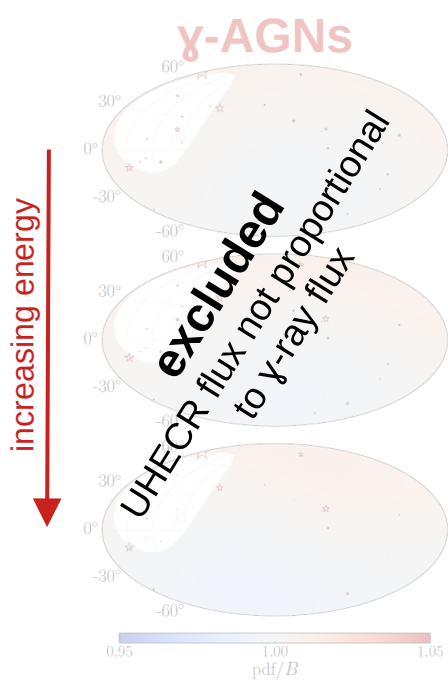
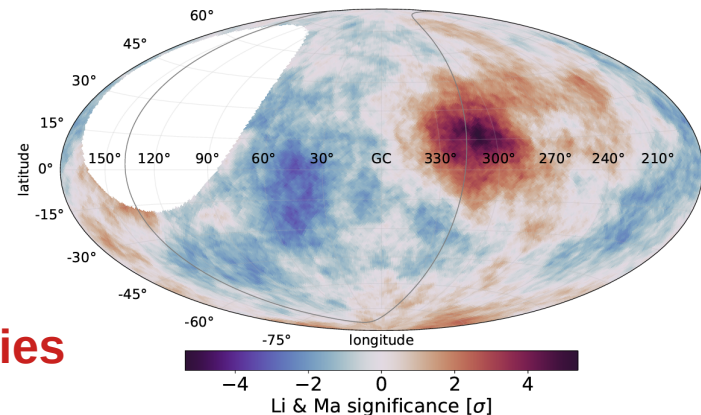
Modeled arrival directions

- based on correlations of arrival directions with nearby candidates (SBGs, Centaurus A, γ -AGNs)
- model: homogeneous background sources + nearby candidates



Modeled arrival directions

- based on correlations of arrival directions with nearby candidates (SBGs, Centaurus A, γ -AGNs)
- model: homogeneous background sources + nearby candidates

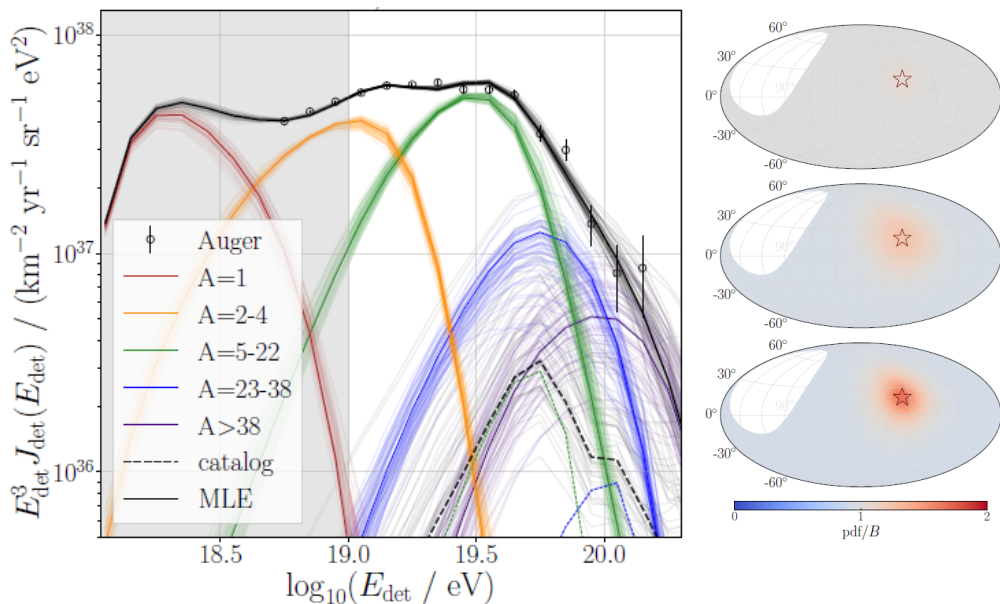


- starburst galaxy model favored with **4.5 σ** significance over homogeneous model!
- mostly due to Centaurus A / NGC 4945 region

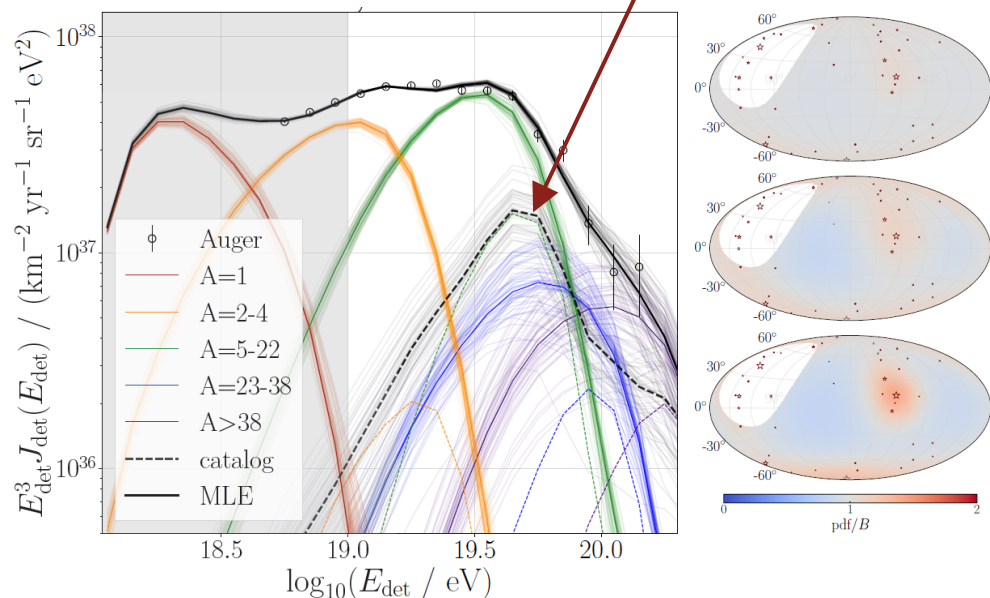
Model predictions

- **best-fit:** hard injection spectrum $dN/dE \sim E^{-1}$, nitrogen-dominated, 20° magnetic field blurring for proton with 10 EeV
- signal fraction $\sim 20\%$ from SBGs, 3% from Centaurus region (at 40 EeV, increases with E)
- independent of evolution & systematic effects

Centaurus A

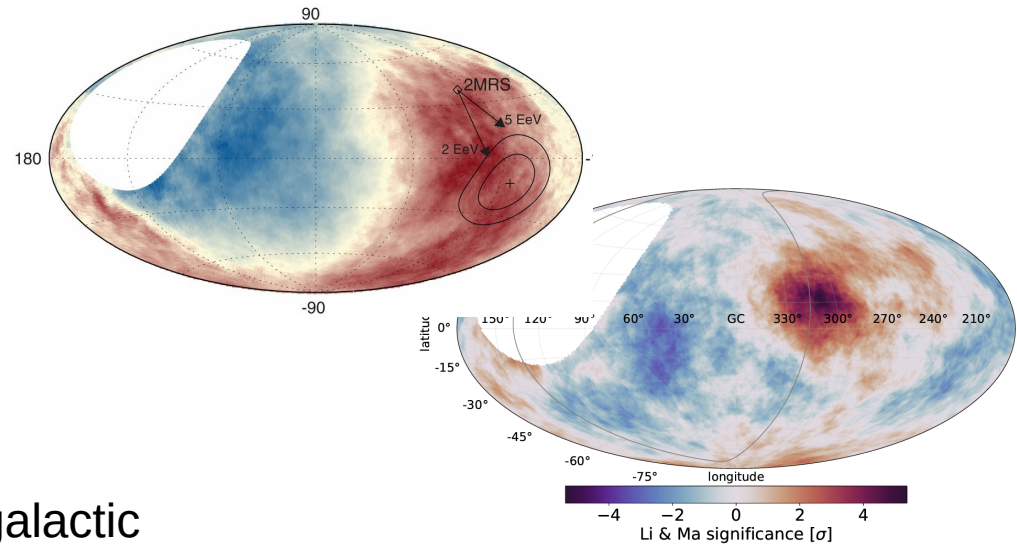


Starburst Galaxies



Conclusions

- progress in search for UHECR sources
 - need careful modeling of source distribution, propagation, magnetic fields...
- **> 8 EeV: sources most likely follow large-scale structure**
- can infer information on Galactic & extragalactic magnetic fields & source number density
- **> 40 EeV: individual source candidates describe data**
- like starburst galaxies, Centaurus A, $\sim 4.5\sigma$ significance
- **promising future:** detector upgrades underway (AugerPrime & TAx4), better composition differentiation, novel machine learning data...



Backup

Best-fit parameters

	Cen A, $m = 0$ (flat)		Cen A, $m = 3.4$ (SFR)		SBG, $m = 3.4$ (SFR)	
	posterior	MLE	posterior	MLE	posterior	MLE
γ	$-0.89^{+0.37}_{-0.33}$	-0.65	$-1.19^{+0.45}_{-0.39}$	-1.41	$-1.02^{+0.43}_{-0.36}$	-1.25
$\log_{10}(R_{\text{cut}}/V)$	$18.20^{+0.04}_{-0.05}$	18.23	$18.21^{+0.04}_{-0.05}$	18.20	$18.24^{+0.04}_{-0.06}$	18.22
f_0	$0.07^{+0.01}_{-0.05}$	0.029	$0.07^{+0.01}_{-0.05}$	0.031	$0.19^{+0.07}_{-0.11}$	0.23
$\delta_0/^\circ$	$30.5^{+2.0}_{-20.2}$	14.4	$27.4^{+4.2}_{-17.0}$	14.3	$18.8^{+5.9}_{-3.6}$	21.9
I_{H}	$5.8^{+2.9}_{-2.6} \times 10^{-2}$	4.2×10^{-4}	$1.2^{+0.2}_{-1.2} \times 10^{-2}$	3.0×10^{-4}	$1.2^{+0.1}_{-1.2} \times 10^{-2}$	1.0×10^{-4}
I_{He}	$2.7^{+0.4}_{-0.4} \times 10^{-1}$	3.5×10^{-1}	$9.9^{+3.8}_{-2.9} \times 10^{-2}$	1.2×10^{-1}	$1.1^{+0.3}_{-0.4} \times 10^{-1}$	1.4×10^{-1}
I_{N}	$5.6^{+0.4}_{-0.4} \times 10^{-1}$	5.0×10^{-1}	$6.7^{+0.7}_{-0.7} \times 10^{-1}$	6.8×10^{-1}	$7.2^{+0.6}_{-0.6} \times 10^{-1}$	7.3×10^{-1}
I_{Si}	$9.0^{+3.9}_{-3.4} \times 10^{-2}$	1.4×10^{-1}	$1.5^{+0.5}_{-0.6} \times 10^{-1}$	1.6×10^{-1}	$1.2^{+0.5}_{-0.5} \times 10^{-1}$	9.8×10^{-2}
I_{Fe}	$2.3^{+0.9}_{-1.2} \times 10^{-2}$	1.8×10^{-2}	$5.1^{+1.5}_{-1.8} \times 10^{-2}$	4.4×10^{-2}	$4.7^{+1.3}_{-1.7} \times 10^{-2}$	3.8×10^{-2}
ν_E/σ	$-1.24^{+0.68}_{-0.50}$	-1.35	$0.23^{+0.42}_{-0.60}$	0.13	$0.35^{+0.44}_{-0.65}$	0.40
$\nu_{X_{\text{max}}}/\sigma$	$-0.94^{+0.29}_{-0.24}$	-0.97	$-1.60^{+0.30}_{-0.25}$	-1.45	$-1.55^{+0.26}_{-0.25}$	-1.33
$\log b$	-254.6 ± 0.1		-264.5 ± 0.2		-258.6 ± 0.2	
D_{sys}		2.8		2.1		1.9
D_E ($N_J = 14$)		13.6		21.9		25.3
$D_{X_{\text{max}}}$ ($N_{X_{\text{max}}} = 74$)		107.4		113.6		112.7
D		123.8		137.7		139.9
$\log \mathcal{L}_{\text{ADs}}$		9.4		9.5		13.5
$\log \mathcal{L}$		-228.51		-235.3		-232.4

Test statistic

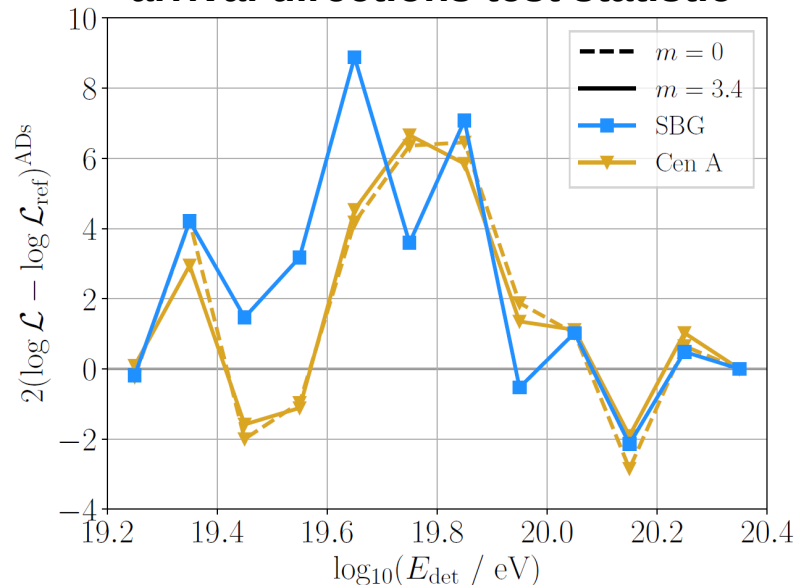
compare likelihood to ref. model (just background sources):

	SBG	Cen A (<i>flat</i>)	Cen A (<i>SFR</i>)
TS_{tot}	25.6	17.3	19.1
TS_E	-4.5	-1.4	-1.1
$TS_{X_{\text{max}}}$	2.0	0.2	1.0
TS_{ADs}	27.1	18.7	19.0

SBG model has highest TS = 25.6 \leftrightarrow 4.5 σ

- including experimental systematic effects
- increase compared to AD-only correlation
- Centaurus region contributes dominant part: **TS~20**
- (E-dependent) arrival directions most important

arrival directions test statistic



- sum over E bins gives total TS
- peaks could be from He, N, Si
 - but: large uncertainties

Test statistic

	Cen A, $m = 0.0$		Cen A, $m = 3.4$		SBG, $m = 3.4$		γ AGN, $m = 5.0$		γ AGN+EGMF**, $m = 5.0$	
	+ syst		+ syst		+ syst		+ syst		+ syst	
TS_{tot}	22.8	17.3	22.2	19.1	27.6	25.6	23.9*	9.8*	34.3*	33.2*
TS_E	-0.1	-1.4	-0.4	-1.1	-5.2	-4.5	26.8	3.9	18.2	8.4
$TS_{X_{\text{max}}}$	1.9	0.2	1.8	1.0	6.2	2.0	-0.8	6.4	4.4	14.7
TS_{ADs}	20.9	18.7	20.8	19.0	26.6	27.1	-2.1	-3.0	11.7	8.6

$$TS_{\text{tot}} = \sum_{\text{obs}=E, X_{\text{max}}, \text{ADs}} 2(\log \mathcal{L}^{m=x} - \log \mathcal{L}_{\text{ref}}^{m=x})^{\text{obs}}$$

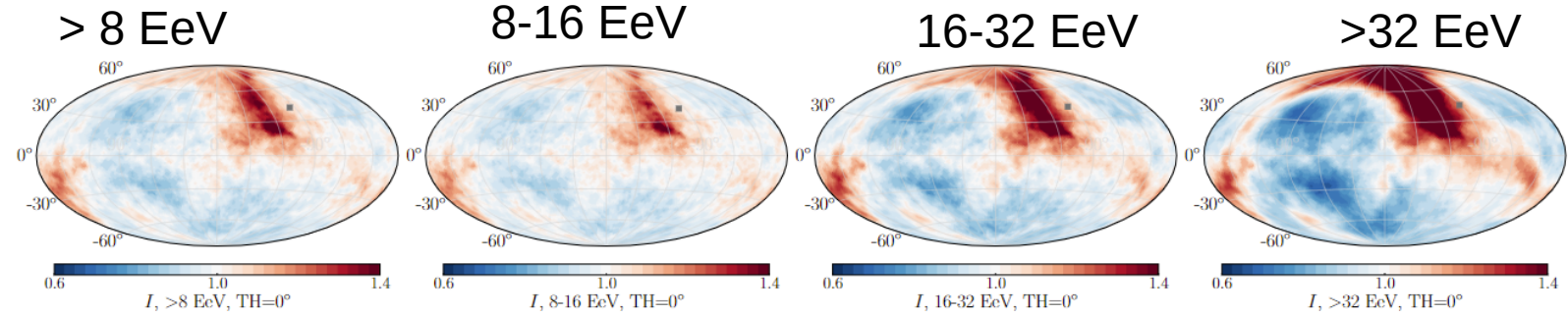
$$\mathcal{L}_{X_{\text{max}}} = \prod_{\tilde{e}} n^{\tilde{e}}! \prod_x \frac{(\mu^{\tilde{e},x})^{n^{\tilde{e},x}}}{n^{\tilde{e},x}!}$$

$$\log \mathcal{L}_E = \sum_e \left(n^e \log(\mu^e) - \log(n^e!) - \mu^e \right)$$

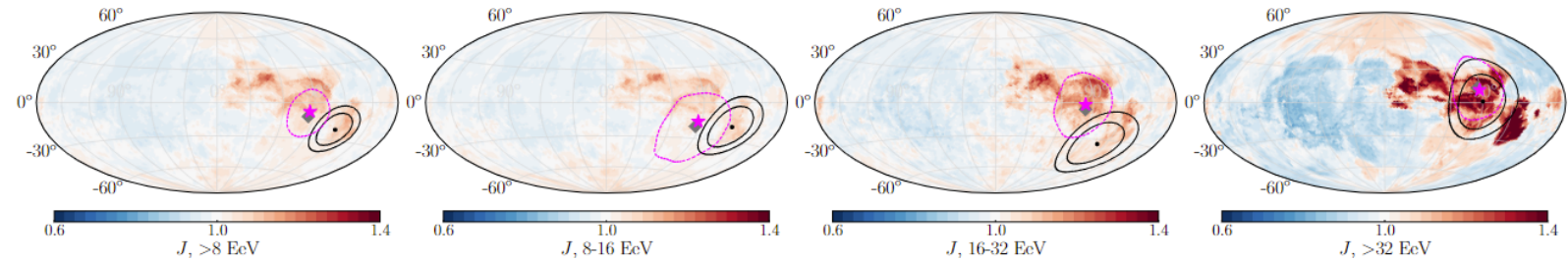
$$\mathcal{L}_{\text{ADs}} = \prod_e \prod_p (\text{pdf}^{e,p})^{n^{e,p}}$$

Dipole direction predictions

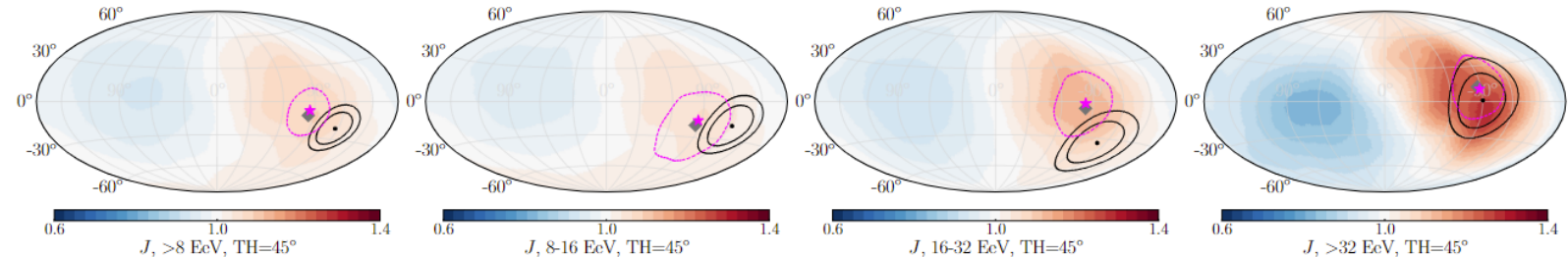
illumination



arrival directions



arrival directions
45° tophat

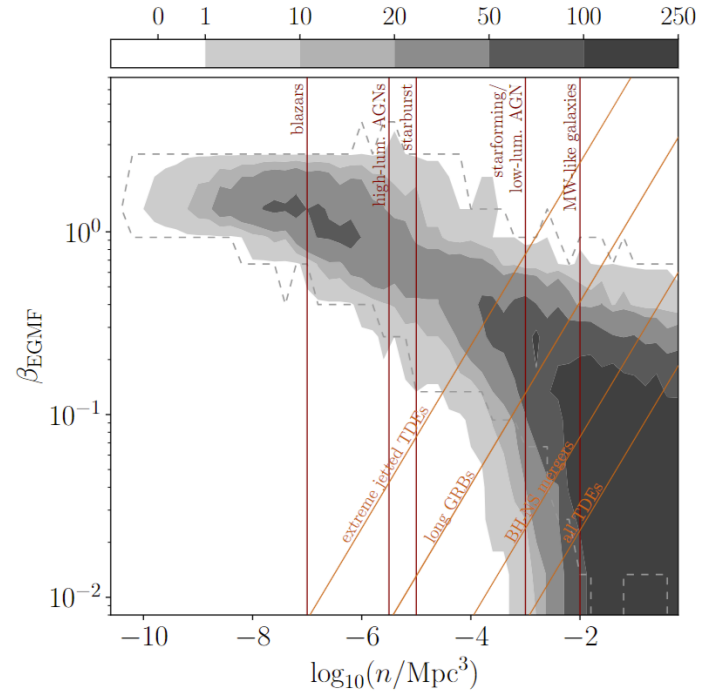
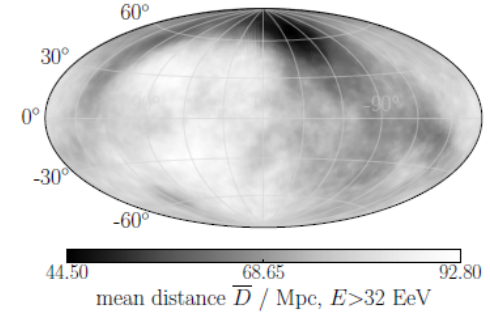
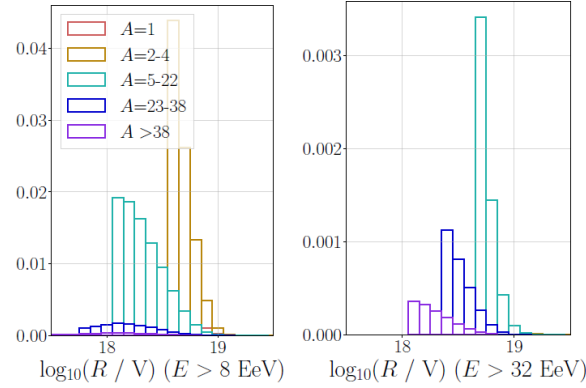


EGMF and transients

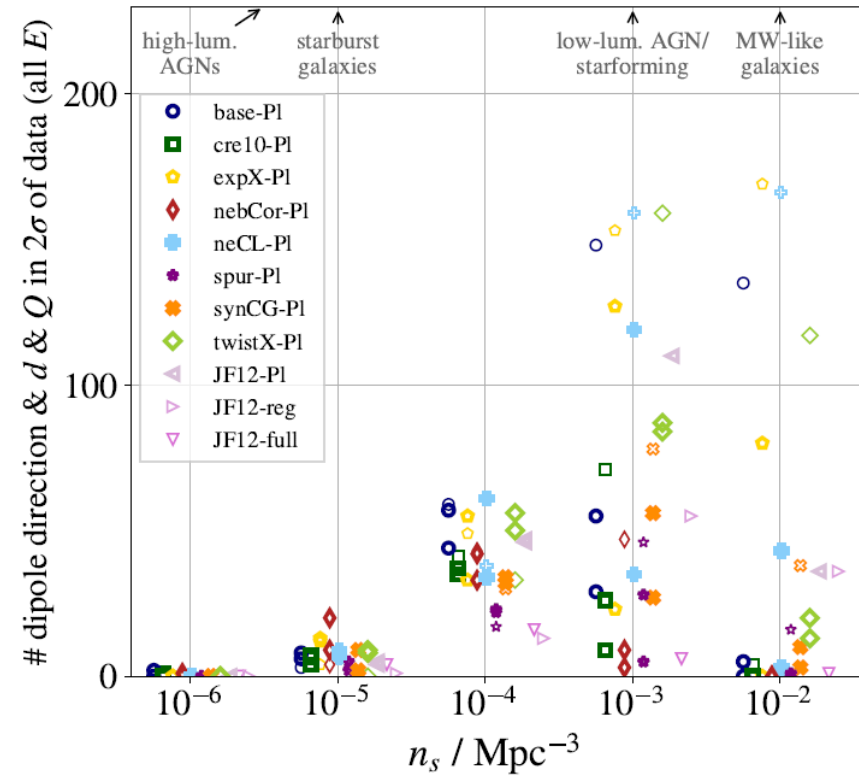
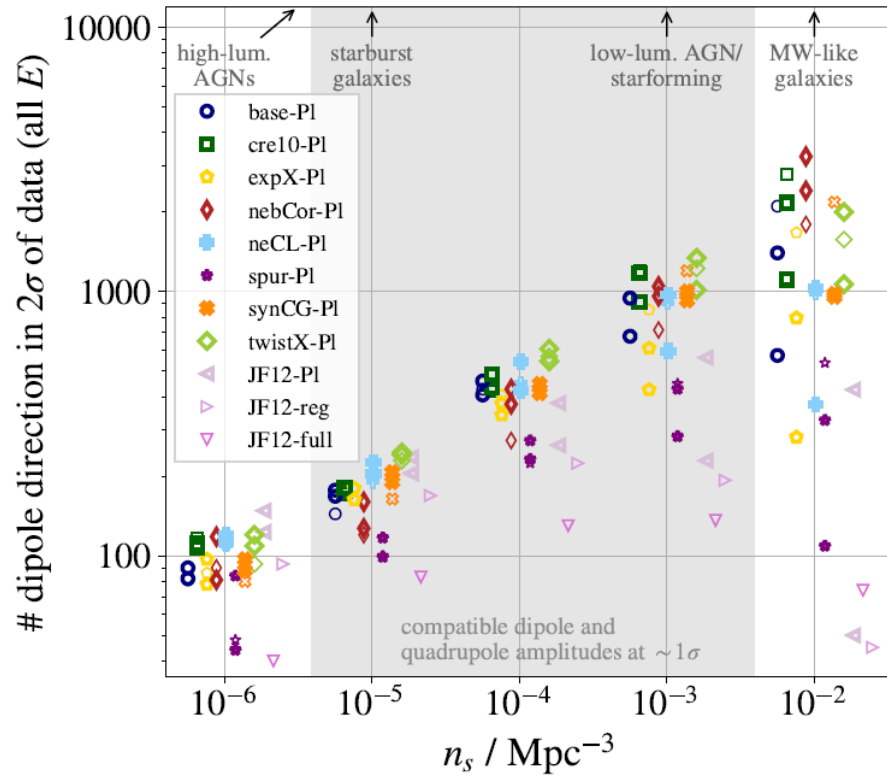
$$\delta\theta = 2.9^\circ \frac{B}{\text{nG}} \frac{10 \text{ EV}}{E/Z} \frac{\sqrt{D L_c}}{\text{Mpc}} = 2.9^\circ \beta_{\text{EGMF}} \frac{10 \text{ EV}}{E/Z} \sqrt{\frac{\bar{D}}{\text{Mpc}}}$$

$$n_{\text{eff}} \approx \Gamma \tau_{\text{eff}}$$

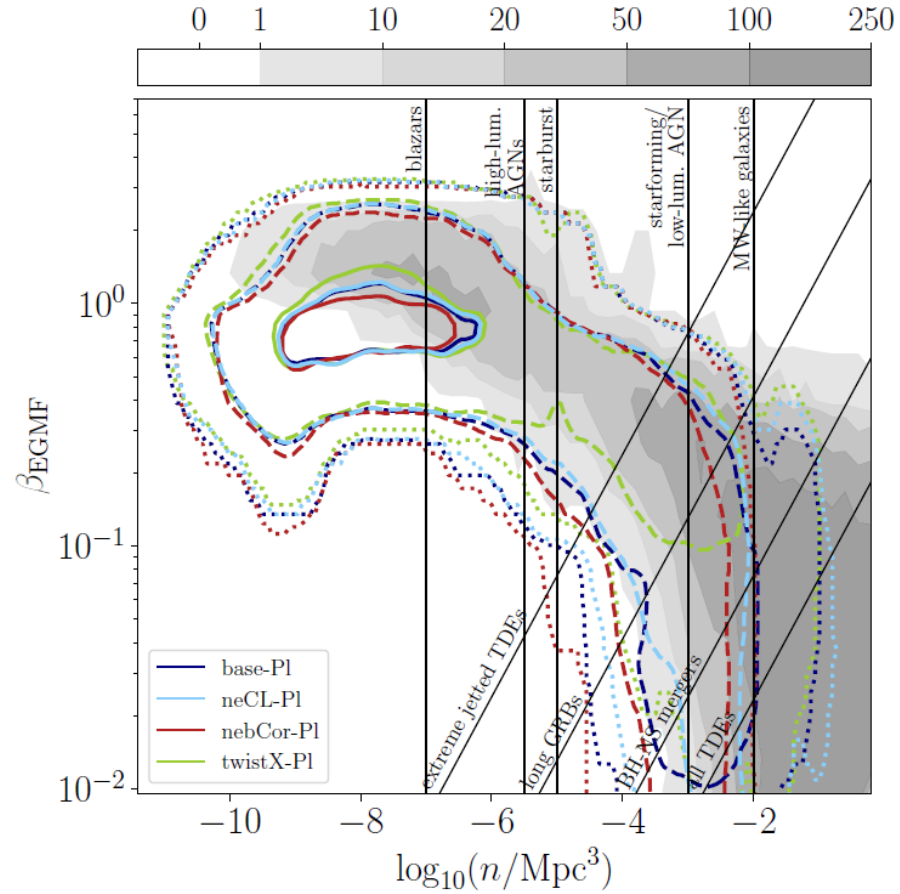
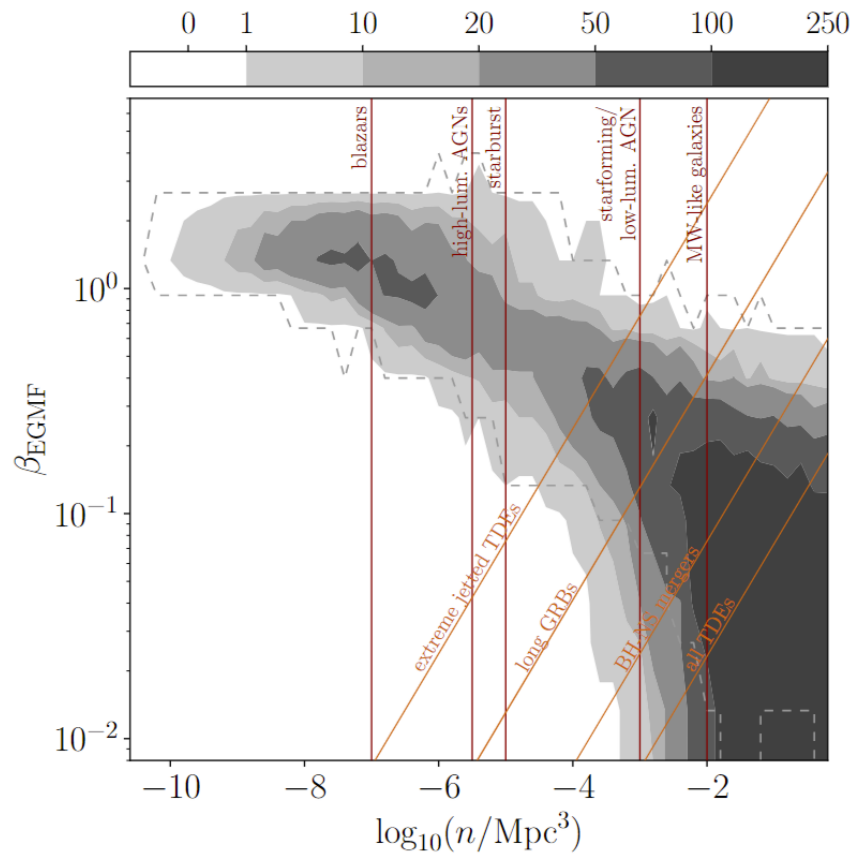
$$\tau_{\text{eff}} = 0.14 \left(\frac{D}{\text{Mpc}} \frac{\text{EV}}{R} \beta_{\text{EGMF}} \right)^2 \text{ Myr} = 34 \beta_{\text{EGMF}}^2 \text{ Myr}$$



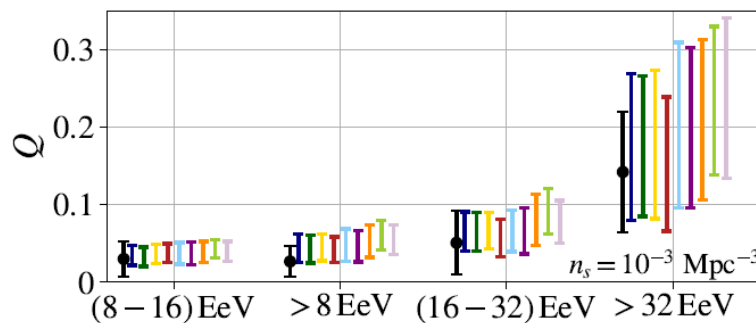
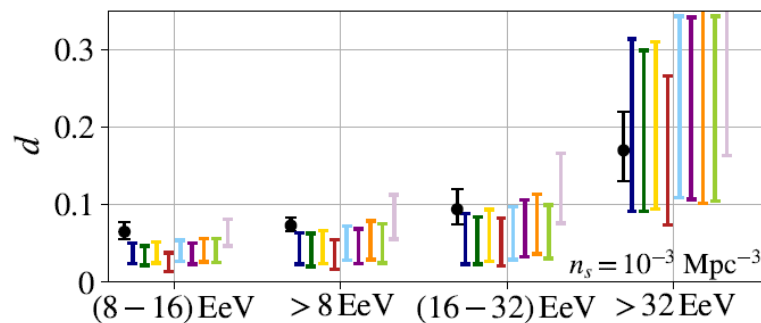
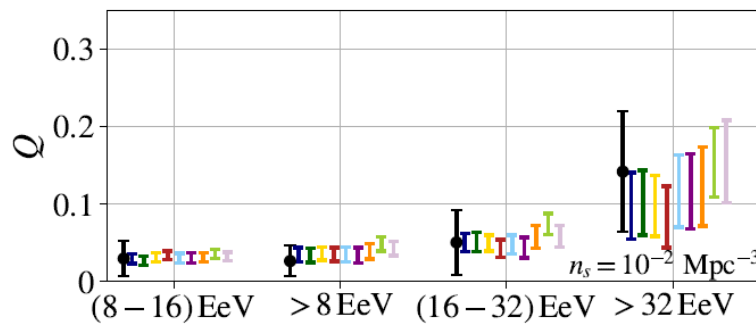
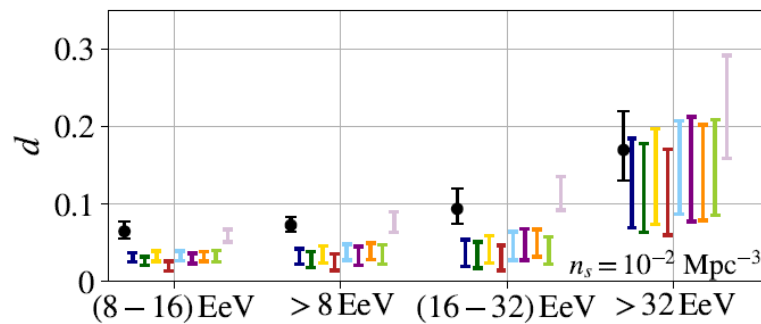
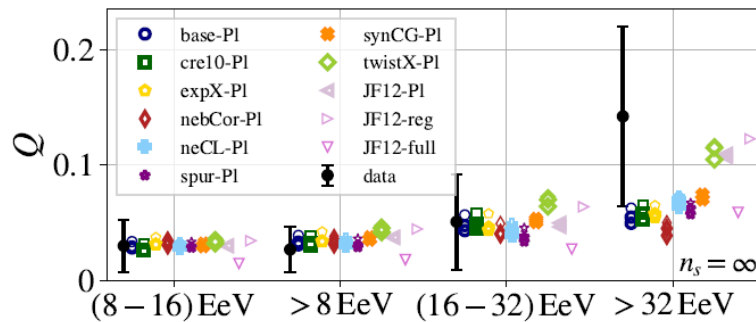
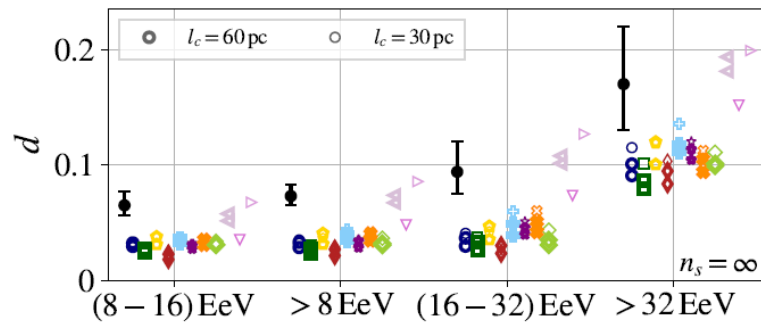
UF23 models - which ones are favored?



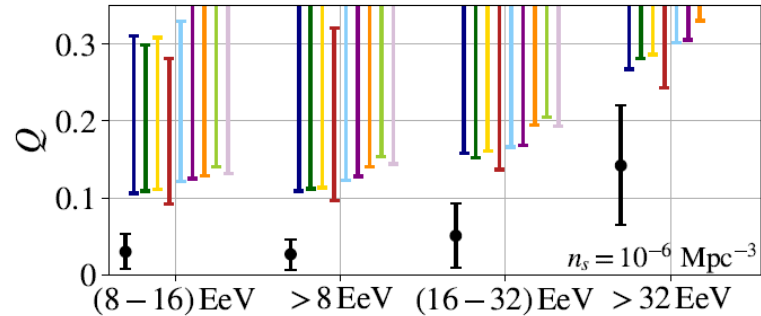
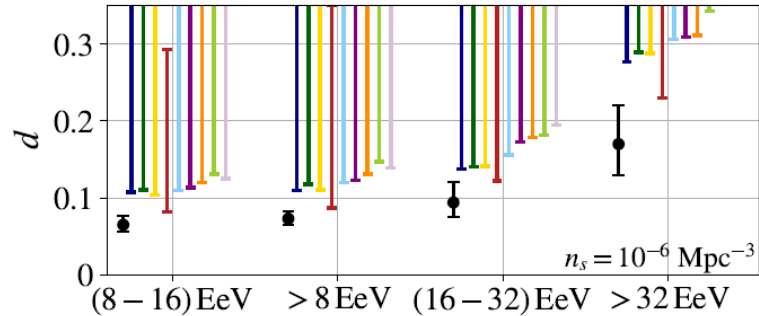
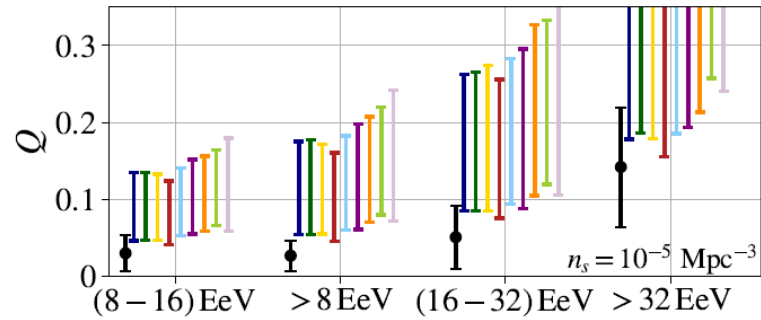
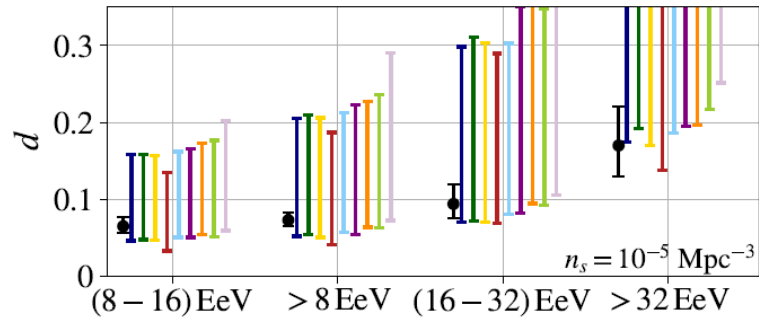
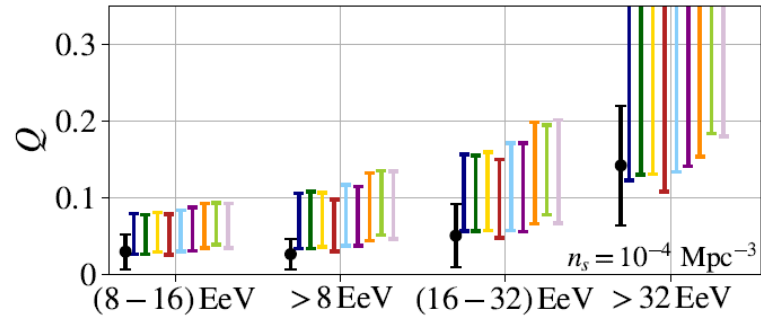
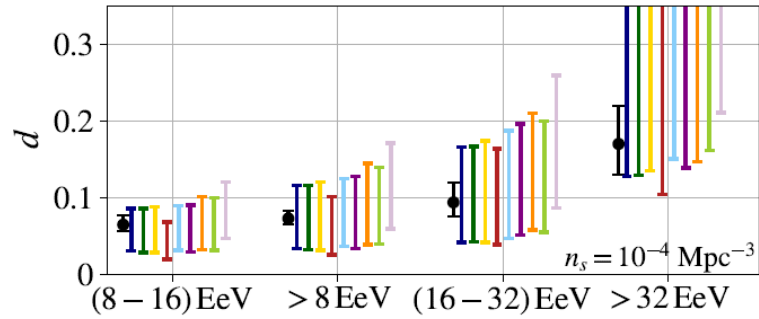
UF23 models: EGMF



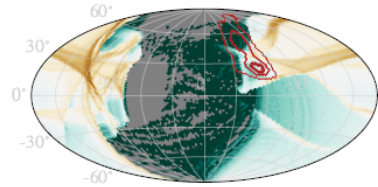
UF23 models: dipole & quadrupole



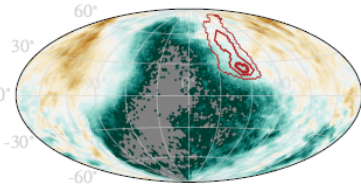
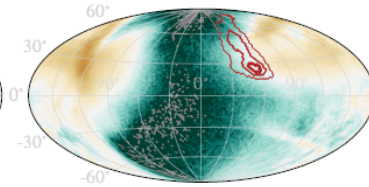
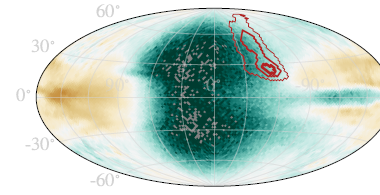
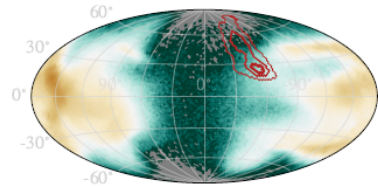
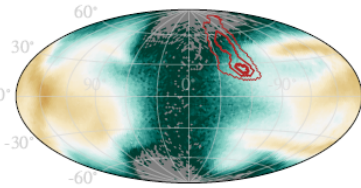
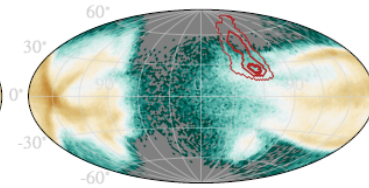
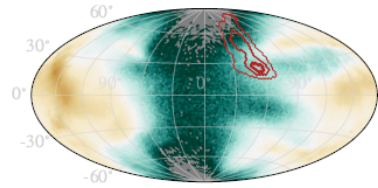
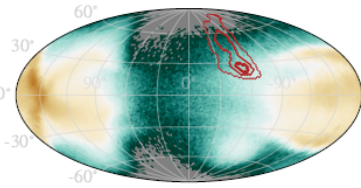
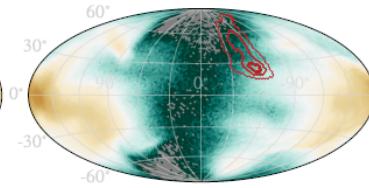
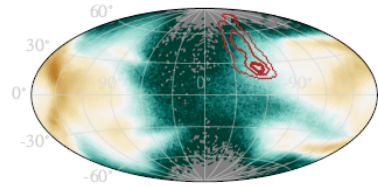
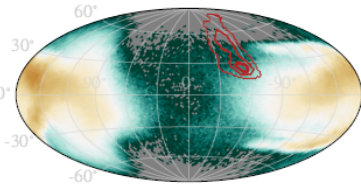
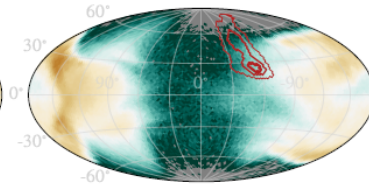
UF23 models: dipole & quadrupole



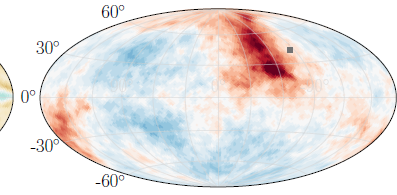
UF23 models: all magnification maps



(a) JF12-reg (compare to [30])

(b) JF12-full $l_c = 30$ pc (compare to [30])(c) JF12 + Planck $l_c = 60$ pc(m) UF23 twistX + Planck $l_c = 60$ pc(d) UF23 base + Planck $l_c = 60$ pc(e) UF23 base + Planck $l_c = 60$ pc,
2nd realization(f) UF23 base + Planck $l_c = 30$ pc(g) UF23 cre10 + Planck $l_c = 60$ pc(h) UF23 expX + Planck $l_c = 60$ pc(i) UF23 nebCor + Planck $l_c = 60$ pc(j) UF23 neCL + Planck $l_c = 60$ pc(k) UF23 spur + Planck $l_c = 60$ pc(l) UF23 synCG + Planck $l_c = 60$ pc

Color bar for magnification maps (a)-(m): $\log_{10}(\text{magnification})$ ranging from -2 to 2.

(n) "Illumination" map I
from Bister&Farrar (2024)